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Surname	Other names
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Pearson Edexcel
International
Advanced Level

Centre Number

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Candidate Number

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Mathematics

International Advanced Level

Pure Mathematics P4

Sample Assessment Materials for first teaching September 2018

Time: 1 hour 30 minutes

Paper Reference

WMA14/01

You must have:

Mathematical Formulae and Statistical Tables, calculator

Total Marks

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Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for algebraic manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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Answer ALL questions. Write your answers in the spaces provided.

1. Use the binomial series to find the expansion of

$$\frac{1}{(2 + 5x)^3} \quad |x| < \frac{2}{5}$$

in ascending powers of x , up to and including the term in x^3

Give each coefficient as a fraction in its simplest form.

(6)

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Question 1 continued

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Q1

(Total for Question 1 is 6 marks)

2. A curve C has the equation

$$x^3 + 2xy - x - y^3 - 20 = 0$$

(a) Find $\frac{dy}{dx}$ in terms of x and y . **(5)**

(b) Find an equation of the tangent to C at the point $(3, -2)$, giving your answer in the form $ax + by + c = 0$, where a , b and c are integers. **(2)**

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3.

$$f(x) = \frac{1}{x(3x - 1)^2} = \frac{A}{x} + \frac{B}{(3x - 1)} + \frac{C}{(3x - 1)^2}$$

(a) Find the values of the constants A , B and C **(4)**

(b) (i) Hence find $\int f(x) \, dx$

(ii) Find $\int_1^2 f(x) \, dx$, giving your answer in the form $a + \ln b$, where a and b are constants. **(6)**

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Question 3 continued

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Question 5 continued

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Question 5 continued

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Q5

(Total for Question 5 is 8 marks)

6. Prove by contradiction that, if a, b are positive real numbers, then $a + b \geq 2\sqrt{ab}$ (4)

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Question 6 continued

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Q6

(Total for Question 6 is 4 marks)

7.

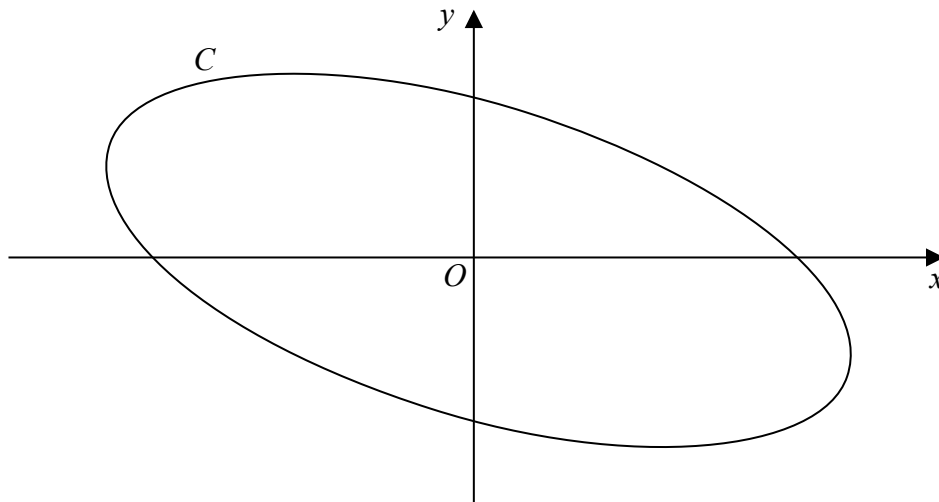


Figure 3

Figure 3 shows a sketch of the curve C with parametric equations

$$x = 4 \cos \left(t + \frac{\pi}{6} \right) \quad y = 2 \sin t \quad 0 \leq t \leq 2\pi$$

(a) Show that

$$x + y = 2\sqrt{3} \cos t \tag{3}$$

(b) Show that a cartesian equation of C is

$$(x + y)^2 + ay^2 = b$$

where a and b are integers to be found.

(2)

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Question 7 continued

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(Total for Question 7 is 5 marks)

Q7

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8. Water is being heated in a kettle. At time t seconds, the temperature of the water is $\theta^\circ\text{C}$.

The rate of increase of the temperature of the water at time t is modelled by the differential equation

$$\frac{d\theta}{dt} = \lambda(120 - \theta) \quad \theta \leq 100$$

where λ is a positive constant.

Given that $\theta = 20$ when $t = 0$

- (a) solve this differential equation to show that

$$\theta = 120 - 100e^{-\lambda t} \tag{8}$$

When the temperature of the water reaches 100°C , the kettle switches off.

- (b) Given that $\lambda = 0.01$, find the time, to the nearest second, when the kettle switches off. (3)

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9. With respect to a fixed origin O , the line l_1 is given by the equation

$$\mathbf{r} = \begin{pmatrix} 8 \\ 1 \\ -3 \end{pmatrix} + \mu \begin{pmatrix} -5 \\ 4 \\ 3 \end{pmatrix}$$

where μ is a scalar parameter.

The point A lies on l_1 where $\mu = 1$

- (a) Find the coordinates of A .

(1)

The point P has position vector $\begin{pmatrix} 1 \\ 5 \\ 2 \end{pmatrix}$

The line l_2 passes through the point P and is parallel to the line l_1

- (b) Write down a vector equation for the line l_2

(2)

- (c) Find the exact value of the distance AP .

Give your answer in the form $k\sqrt{2}$, where k is a constant to be found.

(2)

The acute angle between AP and l_2 is θ

- (d) Find the value of $\cos \theta$

(3)

A point E lies on the line l_2

Given that $AP = PE$,

- (e) find the area of triangle APE ,

(2)

- (f) find the coordinates of the two possible positions of E .

(5)
