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Mark Scheme (Results)

## Summer 2016

Pearson Edexcel GCE in Core Mathematics 1 (6663/01)

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## PEARSON EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

1. The total number of marks for the paper is 75
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of $M$ marks)
- Marks should not be subdivided.


## 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- d... or dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper or ag- answer given
- $\square$ or d... The second mark is dependent on gaining the first mark

4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft.
5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
6. If a candidate makes more than one attempt at any question:

- If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
- If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.

7. Ignore wrong working or incorrect statements following a correct answer.

## General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

## Method mark for solving 3 term quadratic:

## 1. Factorisation

$\left(x^{2}+b x+c\right)=(x+p)(x+q)$, where $p q|=|c|$, leading to $\mathrm{x}=\ldots$
$\left(a x^{2}+b x+c\right)=(m x+p)(n x+q)$, where $p q|=|c|$ and $| m n|=|a|$, leading to $\mathrm{x}=\ldots$

## 2. Formula

Attempt to use the correct formula (with values for $a, b$ and $c$ ).

## 3. Completing the square

Solving $x^{2}+b x+c=0: \quad\left(x \pm \frac{b}{2}\right)^{2} \pm q \pm c=0, \quad q \neq 0$, leading to $\mathrm{x}=\ldots$

## Method marks for differentiation and integration:

## 1. Differentiation

Power of at least one term decreased by 1. ( $x^{n} \rightarrow x^{n-1}$ )

## 2. Integration

Power of at least one term increased by 1. $\left(x^{n} \rightarrow x^{n+1}\right)$

## Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

Method mark for quoting a correct formula and attempting to use it, even if there are small errors in the substitution of values.

Where the formula is not quoted, the method mark can be gained by implication from correct working with values, but may be lost if there is any mistake in the working.

## Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

| Question Number | Scheme | Notes | Marks |
| :---: | :---: | :---: | :---: |
| 1 |  | $\int\left(2 x^{4}-\frac{4}{\sqrt{x}}+3\right) \mathrm{d} x$ |  |
|  | $\frac{2}{5} x^{5}-\frac{4}{\frac{1}{2}} x^{\frac{1}{2}}+3 x$ | M1: $x^{n} \rightarrow x^{n+1}$. One power increased by 1 but not for just $+c$. This could be for $3 \rightarrow 3 x$ or for $x^{n} \rightarrow x^{n+1}$ on what they think $\frac{1}{\sqrt{x}}$ is as a power of $x$. | M1A1A1 |
|  |  | A1: One of these 3 terms correct. Allow un-simplified e.g. $\frac{2 x^{4+1}}{4+1},-\frac{4 x^{-\frac{1}{2}+1}}{-\frac{1}{2}+1}, 3 x^{1}$ |  |
|  |  | A1: Two of these 3 terms correct. Allow un-simplified e.g. $\frac{2 x^{4+1}}{4+1},-\frac{4 x^{-\frac{1}{2}+1}}{-\frac{1}{2}+1}, 3 x^{1}$ |  |
|  | $=\frac{2}{5} x^{5}-8 x^{\frac{1}{2}}+3 x+c$ | Complete fully correct simplified expression appearing all on one line with constant. Allow 0.4 for $\frac{2}{5}$. <br> Do not allow $3 x^{1}$ for $3 x$ <br> Allow $\sqrt{x}$ or $x^{0.5}$ for $x^{\frac{1}{2}}$ | A1 |
|  | Ignore any spurious integral signs and ignore subsequent working following a fully correct answer. |  |  |
|  |  |  | [4] |
|  |  |  | 4 marks |

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| Question Number | Scheme | Notes | Marks |
| :---: | :---: | :---: | :---: |
| 2 | $\begin{aligned} & 9^{3 x+1}=\text { for example } \\ & 3^{2(3 x+1)} \text { or }\left(3^{2}\right)^{3 x+1} \text { or }\left(3^{(3 x+1)}\right)^{2} \text { or } 3^{3 x+1} \times 3^{3 x+1} \\ & \text { or }(3 \times 3)^{3 x+1} \text { or } 3^{2} \times\left(3^{2}\right)^{3 x} \text { or }\left(9^{\frac{1}{2}}\right)^{y} \text { or } 9^{\frac{1}{2} y} \\ & \text { or } y=2(3 x+1) \end{aligned}$ | Expresses $9^{3 x+1}$ correctly as a power of 3 or expresses $3^{y}$ correctly as a power of 9 or expresses $y$ correctly in terms of $x$ <br> (This mark is not for just $3^{2}=9$ ) | M1 |
|  | $=3^{6 x+2}$ or $y=6 x+2$ or $a=6, b=2$ | Cao (isw if necessary) | A1 |
|  | Providing there is no incorrect work, all Correct answer only Special case: $3^{6 x+1}$ | $w$ sight of $6 x+2$ to score both marks mplies both marks <br> ly scores M1A0 |  |
|  |  |  | [2] |
|  | Alternative | sing logs |  |
|  | $9^{3 x+1}=3^{y} \Rightarrow \log 9^{3 x+1}=\log 3^{y}$ |  |  |
|  | $(3 x+1) \log 9=y \log 3$ | Use power law correctly on both sides | M1 |
|  | $y=\frac{\log 9}{\log 3}(3 x+1)$ |  |  |
|  | $y=6 x+2$ | cao | A1 |
|  |  |  | 2 marks |

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| Question Number | Scheme | Notes | Marks |
| :---: | :---: | :---: | :---: |
| 3.(a) | $\sqrt{50}-\sqrt{18}=5 \sqrt{2}-3 \sqrt{2}$ | $\sqrt{50}=5 \sqrt{2}$ or $\sqrt{18}=3 \sqrt{2}$ and the other term in the form $k \sqrt{2}$. This mark may be implied by the correct answer $2 \sqrt{2}$ | M1 |
|  | $=2 \sqrt{2}$ | Or $a=2$ | A1 |
|  |  |  | [2] |
| $\begin{gathered} \text { (b) } \\ \text { WAY } 1 \end{gathered}$ | $\frac{12 \sqrt{3}}{\sqrt{50}-\sqrt{18}}=\frac{12 \sqrt{3}}{2 " 2 \sqrt{2}}$ | Uses part (a) by replacing denominator by their $a \sqrt{2}$ where $a$ is numeric. This is all that is required for this mark. | M1 |
|  | $=\frac{12 \sqrt{3}}{" 2 " \sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}}=\frac{12 \sqrt{6}}{4}$ | Rationalises the denominator by a correct method e.g. multiplies numerator and denominator by $k \sqrt{2}$ to obtain a multiple of $\sqrt{6}$. Note that multiplying numerator and denominator by $2 \sqrt{2}$ or $-2 \sqrt{2}$ is quite common and is acceptable for this mark. May be implied by a correct answer. <br> This is dependent on the first M1. | dM1 |
|  | $=3 \sqrt{6}$ or $b=3, c=6$ | Cao and cso | A1 |
|  |  |  | [3] |
| $\begin{gathered} \text { (b) } \\ \text { WAY } 2 \end{gathered}$ | $\begin{aligned} & \frac{12 \sqrt{3}}{\sqrt{50}-\sqrt{18}} \times \frac{\sqrt{50}+\sqrt{18}}{\sqrt{50}+\sqrt{18}} \\ & \text { or } \\ & \frac{12 \sqrt{3}}{5 \sqrt{2}-3 \sqrt{2}} \times \frac{5 \sqrt{2}+3 \sqrt{2}}{5 \sqrt{2}+3 \sqrt{2}} \end{aligned}$ | For rationalising the denominator by a correct method i.e. multiplying numerator and denominator by $k(\sqrt{50}+\sqrt{18})$ | M1 |
|  | $\frac{60 \sqrt{6}+36 \sqrt{6}}{50-18}$ | For replacing numerator by $\alpha \sqrt{6}+\beta \sqrt{6}$. This is dependent on the first M1 and there is no need to consider the denominator for this mark. | dM1 |
|  | $=3 \sqrt{6}$ or $b=3, c=6$ | Cao and cso | A1 |
|  |  |  | [3] |
| $\begin{gathered} \text { (b) } \\ \text { WAY } 3 \end{gathered}$ | $\frac{12 \sqrt{3}}{\sqrt{50}-\sqrt{18}}=\frac{12 \sqrt{3}}{2 " 2 \sqrt{2}}$ | Uses part (a) by replacing denominator by their $a \sqrt{2}$ where $a$ is numeric. This is all that is required for this mark. | M1 |
|  | $=\frac{12 \sqrt{3}}{2 \sqrt{2}}=\frac{6 \sqrt{3}}{\sqrt{2}}=\frac{\sqrt{108}}{\sqrt{2}}=\sqrt{54}=\sqrt{9} \sqrt{6}$ | Cancels to obtain a multiple of $\sqrt{6}$. This is dependent on the first M1. | dM1 |
|  | $=3 \sqrt{6}$ Or $b=3, c=6$ | Cao and cso | A1 |
|  |  |  | [3] |
| $\begin{gathered} \text { (b) } \\ \text { WAY } 4 \end{gathered}$ | $\frac{12 \sqrt{3}}{\sqrt{50}-\sqrt{18}}=\frac{12 \sqrt{3}}{" 2 " \sqrt{2}}$ | Uses part (a) by replacing denominator by their $a \sqrt{2}$ where $a$ is numeric. This is all that is required for this mark. | M1 |
|  | $\left.\left(\frac{12 \sqrt{3}}{12}\right)^{2}\right)^{2}=\frac{432}{8}$ |  |  |
|  | $\sqrt{54}=\sqrt{9} \sqrt{6}$ | Obtains a multiple of $\sqrt{6}$. This is dependent on the first M1. | dM1 |
|  | $=3 \sqrt{6}$ Or $b=3, c=6$ | Cao and cso (do not allow $\pm 3 \sqrt{6}$ ) | A1 |
|  |  |  | 5 marks |


| Question <br> Number |  | Notes | Marks |
| :--- | :--- | :--- | :--- |
| 4.(a) |  | Note original points are $A(-2,4)$ and $B(3,-8)$ <br> Similar shape to given figure passing <br> through the origin. A cubic shape with a <br> maximum in the second quadrant and a <br> minimum in the 4, quadrant. <br> There must be evidence of a change in at <br> least one of the $y$-coordinates <br> (inconsistent changes in the y-coordinates <br> are acceptable) but not the $x-$ <br> coordinates. | B1 |


| Question <br> Number | Scheme | Notes | Marks |
| :---: | :---: | :---: | :---: |
|  | WAY 1 |  |  |
| 5. | $\begin{gathered} y=-4 x-1 \\ \Rightarrow(-4 x-1)^{2}+5 x^{2}+2 x=0 \end{gathered}$ | Attempts to makes $y$ the subject of the linear equation and substitutes into the other equation. Allow slips e.g. substituting $y=-4 x+1$ etc. | M1 |
|  | $21 x^{2}+10 x+1=0$ | Correct 3 term quadratic (terms do not need to be all on the same side). <br> The " $=0$ " may be implied by subsequent work. | A1 |
|  | $(7 x+1)(3 x+1)=0 \Rightarrow(x=)-\frac{1}{7},-\frac{1}{3}$ | dM1: Solves a 3 term quadratic by the usual rules (see general guidance) to give at least one value for $x$. Dependent on the first method mark. | dM1 A1 |
|  |  | A1: $(x=)-\frac{1}{7},-\frac{1}{3}$ (two separate correct exact answers). Allow exact equivalents e.g. $(x=)-\frac{6}{42},-\frac{14}{42}$ |  |
|  | $y=-\frac{3}{7}, \quad \frac{1}{3}$ | M1: Substitutes to find at least one $y$ value (Allow substitution into their rearranged equation above but not into an equation that has not been seen earlier). You may need to check here if there is no working and $x$ values are incorrect. | M1 A1 |
|  |  | A1: $y=-\frac{3}{7}, \frac{1}{3}$ (two correct exact answers) Allow exact equivalents e.g. $y=-\frac{18}{42}, \frac{14}{42}$ |  |
|  | Coordinates do not need to be paired |  |  |
|  | Note that if the linear equation is explicitly rearranged to $y=4 x+1$, this gives the correct answers for $x$ and possibly for $y$. In these cases, if it is not already lost, deduct the final A1. |  |  |
|  |  |  | [6] |
|  | WAY 2 |  |  |
|  | $\begin{gathered} x=-\frac{1}{4} y-\frac{1}{4} \\ \Rightarrow y^{2}+5\left(-\frac{1}{4} y-\frac{1}{4}\right)^{2}+2\left(-\frac{1}{4} y-\frac{1}{4}\right)=0 \end{gathered}$ | Attempts to makes $x$ the subject of the linear equation and substitutes into the other equation. Allow slips in the rearrangement as above. | M1 |
|  | $\frac{21}{16} y^{2}+\frac{1}{8} y-\frac{3}{16}=0\left(21 y^{2}+2 y-3=0\right)$ | Correct 3 term quadratic (terms do not need to be all on the same side). <br> The " $=0$ " may be implied by subsequent work. | A1 |
|  | $(7 y+3)(3 y-1)=0 \Rightarrow(y=)-\frac{3}{7}, \frac{1}{3}$ | dM1: Solves a 3 term quadratic by the usual rules (see general guidance) to give at least one value for $y$. Dependent on the first method mark. | dM1 A1 |
|  |  | A1: $(y=)-\frac{3}{7}, \frac{1}{3}$ (two separate correct exact answers). Allow exact equivalents e.g. $(y=)-\frac{18}{42}, \frac{14}{42}$ |  |
|  | $X=-\frac{1}{7},-\frac{1}{3}$ | M1: Substitutes to find at least one $x$ value (Allow substitution into their rearranged equation above but not into an equation that has not been seen earlier). You may need to check here if there is no working and $y$ values are incorrect. | M1 A1 |
|  |  | A1: $x=-\frac{1}{7},-\frac{1}{3}$ (two correct exact answers) Allow exact equivalents e.g. $x=-\frac{6}{42},-\frac{14}{42}$ |  |
|  | Coordinates do not need to be paired |  |  |
|  | Note that if the linear equation is explicitly rearranged to $x=(y+1) / 4$, this gives the correct answers for $y$ and possibly for $x$. In these cases, if it is not already lost, deduct the final A1. |  |  |
|  |  |  | [6] |
|  |  |  | 6 marks |


| Question Number | Scheme | Notes | Marks |
| :---: | :---: | :---: | :---: |
|  | $a_{1}=4, a_{n+1}=5-k a_{n}, n \ldots 1$ |  |  |
| 6. (a) | $\begin{gathered} a_{2}=5-k a_{1}=5-4 k \\ a_{3}=5-k a_{2}=5-k(5-4 k) \end{gathered}$ | M1: Uses the recurrence relation correctly at least once. This may be implied by $a_{2}=5-4 k$ or by the use of $a_{3}=5-k\left(\text { their } a_{2}\right)$ | M1A1 |
|  |  | A1: Two correct expressions - need not be simplified but must be seen in (a). <br> Allow $a_{2}=5-k 4$ and $a_{3}=5-5 k+k^{2} 4$ <br> Isw if necessary for $a_{3}$. |  |
|  |  |  | [2] |
| (b) | $\sum_{r=1}^{3}(1)=1+1+1$ | Finds $1+1+1$ or 3 somewhere in their solution (may be implied by e.g. $5+6-4 k$ $+6-5 k+4 k^{2}$ ). Note that $5+6-4 k+6-5 k+4 k^{2}$ would score B1 and the M1 below. | B1 |
|  | $\sum_{r=1}^{3} a_{r}=4+" 5-4 k "+" 5-5 k+4 k^{2} "$ | Adds 4 to their $a_{2}$ and their $a_{3}$ where $a_{2}$ and $a_{3}$ are functions of $k$. The statement as shown is sufficient. | M1 |
|  | $\sum_{r=1}^{3}\left(1+a_{r}\right)=17-9 k+4 k^{2}$ | Cao but condone ' $=0$ ' after the expression | A1 |
|  | Allow full marks in (b) for correct answer only |  |  |
|  |  |  | [3] |
| (c) | 500 | cao | B1 |
|  |  |  | [1] |
|  |  |  | 6 marks |


| Question Number | Scheme | Notes | Marks |
| :---: | :---: | :---: | :---: |
| 7. | $y=3 x^{2}+6 x^{\frac{1}{3}}+\frac{2 x^{3}-7}{3 \sqrt{x}}$ |  |  |
|  | $\frac{2 x^{3}-7}{3 \sqrt{x}}=\frac{2 x^{3}}{3 \sqrt{x}}-\frac{7}{3 \sqrt{x}}=\frac{2}{3} x^{\frac{5}{2}}-\frac{7}{3} x^{-\frac{1}{2}}$ | Attempts to split the fraction into 2 terms and obtains either $\alpha X^{\frac{5}{2}}$ or $\beta X^{-\frac{1}{2}}$. This may be implied by a correct power of $x$ in their differentiation of one of these terms. But beware of $\beta x^{-\frac{1}{2}}$ coming from $\frac{2 x^{3}-7}{3 \sqrt{x}}=2 x^{3}-7+3 x^{-\frac{1}{2}}$ | M1 |
|  | $x^{n} \rightarrow x^{n-1}$ | Differentiates by reducing power by one for any of their powers of $x$ | M1 |
|  | $\left(\frac{\mathrm{d} y}{\mathrm{~d} x}=\right) 6 x+2 x^{-\frac{2}{3}}+\frac{5}{3} x^{\frac{3}{2}}+\frac{7}{6} x^{-\frac{3}{2}}$ | A1: $6 x$. Do not accept $6 x^{1}$. Depends on second M mark only. Award when first seen and isw. | A1A1A1A1 |
|  |  | A1: $2 x^{-\frac{2}{3}}$. Must be simplified so do not accept e.g. $\frac{2}{1} x^{-\frac{2}{3}}$ but allow $\frac{2}{\sqrt[3]{x^{2}}}$. Depends on second M mark only. Award when first seen and isw. |  |
|  |  | A1: $\frac{5}{3} x^{\frac{3}{2}}$. Must be simplified but allow e.g. $1 \frac{2}{3} x^{1.5}$ or e.g. $\frac{5}{3} \sqrt{x^{3}}$. Award when first seen and isw. |  |
|  |  | A1: $\frac{7}{6} x^{-\frac{3}{2}}$. Must be simplified but allow e.g. $1 \frac{1}{6} x^{-1 \frac{1}{2}}$ or e.g. $\frac{7}{6 \sqrt{x^{3}}}$. Award when first seen and isw. |  |
|  | In an otherwise fully correct solution, penalise the presence of $+\mathbf{c}$ by deducting the final A1 |  |  |
|  |  |  | [6] |
|  | Use of Quotient Rule: First M1 and final A1A1 (Other marks as above) |  |  |
|  | $\frac{\mathrm{d}\left(\frac{2 x^{3}-7}{3 \sqrt{x}}\right)}{\mathrm{d} x}=\frac{3 \sqrt{x}\left(6 x^{2}\right)-\left(2 x^{3}-7\right) \frac{3}{2} x^{-\frac{1}{2}}}{(3 \sqrt{x})^{2}}$ | Uses correct quotient rule | M1 |
|  | $=\frac{10 x^{\frac{5}{2}}+7 x^{-\frac{1}{2}}}{6 x}$ | A1: Correct first term of numerator and correct denominator | A1A1 |
|  |  | A1: All correct as simplified as shown |  |
|  | So $\frac{\mathrm{d} y}{\mathrm{~d} x}=6 x+2 x^{-\frac{2}{3}}+\frac{10 x^{\frac{5}{2}}+7 x^{-\frac{1}{2}}}{6 x}$ scores full marks |  |  |
|  |  |  | 6 marks |

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| Question Number | Scheme | Notes | Marks |
| :---: | :---: | :---: | :---: |
| 8.(a) | $2 p x^{2}-6 p x+4 p "=" 3 x-7$ <br> or $y=2 p\left(\frac{y+7}{3}\right)^{2}-6 p\left(\frac{y+7}{3}\right)+4 p$ | Either: <br> Compares the given quadratic expression with the given linear expression using $<,>,=, \neq$ <br> (May be implied) <br> or Rearranges $y=3 x-7$ to make $x$ the subject and substitutes into the given quadratic | M1 |
|  | Examples$\begin{aligned} & -3 x+7(=0), \quad-2 p x^{2}+6 p x-4 p+3 x-7(=0) \\ & -)+4 p-y(=0), \quad 2 p y^{2}+(10 p-9) y+8 p(=0) \\ & y=2 p x^{2}-6 p x+4 p-3 x+7 \end{aligned}$ |  | dM1 |
|  | Moves all the terms to one side allowing sign errors only. Ignore $>0,<0,=0$ etc. The terms do not need to be collected. Dependent on the first method mark. |  |  |
|  | $\begin{gathered} \text { E.g. } \\ b^{2}-4 a c=(-6 p-3)^{2}-4(2 p)(4 p+7) \\ b^{2}-4 a c=(10 p-9)^{2}-4(2 p)(8 p) \end{gathered}$ | Attempts to use $b^{2}-4 a c$ with their $a, b$ and $c$ where $a= \pm 2 p, b= \pm(-6 p \pm 3)$ and $c= \pm(4 p \pm 7)$ or for the quadratic in $y$, $a= \pm 2 p, b= \pm(10 p \pm 9)$ and $c= \pm 8 p$. This could be as part of the quadratic formula or as $b^{2}<4 a c$ or as $b^{2}>4 a c$ or as $\sqrt{b^{2}-4 a c}$ etc. If it is part of the quadratic formula only look for use of $b^{2}-4 a c$. There must be no $x$ 's or $y$ 's. <br> Dependent on both method marks. | ddM1 |
|  | $4 p^{2}-20 p+9<0$ * | Obtains printed answer with no errors seen (Allow $0>4 p^{2}-20 p+9$ ) but this $<0$ must been seen at some stage before the last line. | A1* |
|  |  |  | [4] |
| (b) | $(2 p-9)(2 p-1)=0 \Rightarrow p=\ldots$ to obtain $p=$ | Attempt to solve the given quadratic to find 2 values for $p$. See general guidance. | M1 |
|  | $p=\frac{9}{2}, \quad \frac{1}{2}$ | Both correct. May be implied by e.g. $p<\frac{9}{2}, \quad p<\frac{1}{2}$. Allow equivalent values e.g. $4.5, \frac{36}{8}, 0.5$ etc. If they use the quadratic formula allow $\frac{20 \pm 16}{8}$ for this mark but not $\sqrt{256}$ for 16 and allow e.g. $\frac{5}{2} \pm 2$ if they complete the square. | A1 |
|  | $\frac{1}{2}<p<4 \frac{1}{2}$ <br> Allow equivalent values e.g. $\frac{36}{8}$ for $4 \frac{1}{2}$ | M1: Chooses 'inside’ region i.e. Lower Limit $<p<$ Upper Limit or e.g. Lower Limit $\leq p \leq$ Upper Limit | M1A1 |
|  |  | A1: Allow $p \in\left(\frac{1}{2}, 4 \frac{1}{2}\right)$ or just $\left(\frac{1}{2}, 4 \frac{1}{2}\right)$ and allow $p>\frac{1}{2}$ and $p<4 \frac{1}{2}$ and $4 \frac{1}{2}>p>\frac{1}{2}$ but $p>\frac{1}{2}, p<4 \frac{1}{2}$ scores M1A0 $\frac{1}{2}>p>4 \frac{1}{2}$ scores M0A0 |  |
|  | Allow working in terms of $\boldsymbol{x}$ in (b) but the answer must be in terms of $\boldsymbol{p}$ for the final A mark. |  | [4] |
|  |  |  | 8 marks |

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| Question Number | Scheme | Notes | Marks |
| :---: | :---: | :---: | :---: |
| 9.(a) | John; arithmetic series, $a=60, d=15$. |  |  |
|  | $\begin{gathered} 60+75+90=225^{*} \text { or } \\ S_{3}=\frac{3}{2}(120+(3-1)(15))=225^{*} \end{gathered}$ | Finds and adds the first 3 terms or uses sum of 3 terms of an AP and obtains the printed answer, with no errors. | B1 * |
|  | Beware: <br> The $\mathbf{1 2}{ }^{\text {th }}$ term of the sequence is $\mathbf{2 2 5}$ also so look out for $60+(12-1) \times 15=225$. This is B0. |  |  |
|  |  |  | [1] |
| (b) | $t_{9}=60+(n-1) 15=(\mathfrak{E}) 180$ | $\text { M1: Uses } 60+(n-1) 15 \text { with } n=8 \text { or } 9$ $\text { A1: }(\mathfrak{£}) 180$ | M1 A1 |
|  | Listing:M1: Uses $a=60$ and $d=15$ to select the $8^{\text {th }}$ or $9^{\text {th }}$ term (allow arithmetic slips)A1: (S) 180(Special case ( $£$ ) 165 only scores M1A0) |  |  |
|  | $S_{n}=\frac{n}{2}(120+(n-1)(15))$ <br> or $S_{n}=\frac{n}{2}(60+60+(n-1)(15))$ |  | [2] |
| (c) |  | Uses correct formula for sum of $n$ terms with $a=60$ and $d=15$ (must be a correct formula but ignore the value they use for $n$ or could be in terms of $n$ ) | M1 |
|  | $S_{n}=\frac{12}{2}(120+(12-1)(15))$ | Correct numerical expression | A1 |
|  | $=(£) 1710$ | cao | A1 |
|  | Listing: <br> M1: Uses $a=60$ and $d=15$ and finds the sum of at least 12 terms (allow arithmetic slips) <br> A2: (£) 1710 |  |  |
|  |  |  | [3] |
| (d) | $3375=\frac{n}{2}(120+(n-1)(15))$ | Uses correct formula for sum of $n$ terms with $a=60, d=15$ and puts $=3375$ | M1 |
|  | $6750=15 n(8+(n-1)) \Rightarrow 15 n^{2}+105 n=6750$ | Correct three term quadratic. E.g. $6750=105 n+15 n^{2}, \quad 3375=\frac{15}{2} n^{2}+\frac{105}{2} n$ <br> This may be implied by equations such as $6750=15 n(n+7)$ or $3375=\frac{15}{2}\left(n^{2}+7 n\right)$ | A1 |
|  | $n^{2}+7 n=25 \times 18$ * | Achieves the printed answer with no errors but must see the 450 or 450 in factorised form or e.g. 6750, 3375 in factorised form i.e. an intermediate step. | A1* |
|  |  |  | [3] |
| (e) | $n=18 \Rightarrow$ Aged 27 | M1: Attempts to solve the given quadratic or states $n=18$ | M1 A1 |
|  |  | A1: Age $=27$ or just 27 |  |
|  | Age $=27$ only scores both marks (i.e. $n=18$ need not be seen) |  |  |
|  | Note that (e) is not hence so allow valid attempts to solve the given equation for M1 |  |  |
|  |  |  | [2] |
|  |  |  | 11 marks |


| $n$ | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $u_{n}$ | 60 | 75 | 90 | 105 | 120 | 135 | 150 | 165 | 180 |
| $\mathrm{~S}_{n}$ | 60 | 135 | 225 | 330 | 450 | 585 | 735 | 900 | 1080 |
| Age | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |


| $n$ | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $u_{n}$ | 195 | 210 | 225 | 240 | 255 | 270 | 285 | 300 | 315 |
| $\mathrm{~S}_{n}$ | 1275 | 1485 | 1710 | 1950 | 2205 | 2475 | 2760 | 3060 | 3375 |
| Age | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | 27 |


| Question Number | Scheme |  | Note |  | Marks |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 10.(a) | $l_{1}:$ passes through $(0,2)$ and $(3,7) l_{2}$ : goes through $(3,7)$ and is perpendicular to $l_{1}$ |  |  |  |  |
|  | Gradient of $l_{1}$ is $\frac{7-2}{3-0}\left(=\frac{5}{3}\right)$ |  | $m\left(l_{1}\right)=\frac{7-2}{3-0}$. Allow un-simplified. <br> May be implied. |  | B1 |
|  | $m\left(l_{2}\right)=-1 \div$ their $\frac{5}{3}$ |  | Correct application of perpendicular gradient rule |  | M1 |
|  | $y-7="-\frac{3}{5} "(x-3)$ <br> or $y="-\frac{3}{5} " x+c, 7="-\frac{3}{5} "(3)+c \Rightarrow c=\frac{44}{5}$ |  | M1: Uses $y-7=m(x-3)$ with their changed gradient or uses $y=m x+c$ with $(3,7)$ and their changed gradient to find a value for $c$ A1 ft : Correct ft equation for their perpendicular gradient (this is dependent on both $\mathbf{M}$ marks) |  | M1A1ft |
|  | $3 x+5 y-44=0$ |  | Any positive or negative integer multiple. Must be seen in (a) and must include " $=0$ ". |  | A1 |
|  |  |  |  |  | [5] |
| (b) | When $y=0 \quad x=\frac{44}{3}$ |  | M1: Puts $y=0$ and finds a value for $x$ from their equation |  | M1 A1 |
|  |  |  | A1: $x=\frac{44}{3}\left(\right.$ or $14 \frac{2}{3}$ or 14.6$)$ or exact equivalent. ( $y=0$ not needed) |  |  |
|  | Condone $3 x-5 y-44=0$ only leading to the correct answer and condone coordinates written as ( $0,44 / 3$ ) but allow recovery in (c) |  |  |  |  |
|  |  |  |  |  | [2] |
| (c) | GENERAL APPROACH: |  |  |  |  |
|  | Correct attempt at finding the area of any one of the triangles or one of the trapezia but not just one rectangle. The correct pair of 'base' and 'height' must be used for a triangle and the correct formula used for a trapezium. If Pythagoras is required, then it must be used correctly with the correct end coordinates. <br> Note that the first three marks apply to their calculated coordinates e.g. their $\frac{44}{3}, \frac{44}{5},-\frac{6}{5}$ etc. But the given coordinates must be correct e.g. $(0,2)$ and $(3,7)$. |  |  |  | M1 |
|  | A correct numerical expression for the area of one triangle or one trapezium for their coordinates. |  |  |  | A1ft |
|  | Combines the correct areas together correctly for their chosen "way". Note that if correct numerical expressions for areas have been incorrectly simplified before combining them, then this M1 may still be given. Dependent on the first method mark. |  |  |  | dM1 |
|  | Correct numerical expression for the area of ORQP. The expressions must be fully correct for this mark i.e. no follow through. |  |  |  | A1 |
|  | Correct exact area e.g. $54 \frac{1}{3}, \frac{163}{3}, \frac{326}{6}, 54.3$ or any exact equivalent |  |  |  | A1 |
|  | Shape | Vertices | Numerical Expression | Exact Area |  |
|  | Triangle | TRQ | $\frac{1}{2} \times 7 \times\left(\frac{44}{3}-3\right)$ | $\frac{245}{6}$ |  |
|  | Triangle | SPO | $\frac{1}{2} \times \frac{6}{5} \times 2$ | $\frac{6}{5}$ |  |
|  | Triangle | PWQ | $\frac{1}{2} \times\left(\frac{44}{5}-2\right) \times 3$ | $\frac{51}{5}$ |  |
|  | Triangle | $P V Q$ | $\frac{1}{2} \times(7-2) \times 3$ | $\frac{15}{2}$ |  |


|  | Triangle | VWQ | $\frac{1}{2} \times\left(\frac{44}{5}-7\right) \times 3$ | $\frac{27}{10}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Triangle | QUR | $\frac{1}{2} \times\left(\frac{44}{3}-3\right) \times 7$ | $\frac{245}{6}$ |  |
|  | Triangle | PQR | $\frac{1}{2} \times \sqrt{34} \times \frac{7}{3} \times \sqrt{34}$ | $\frac{119}{3}$ |  |
|  | Triangle | PNQ | $\frac{1}{2} \times \frac{34}{3} \times 5$ | $\frac{85}{3}$ |  |
|  | Triangle | $O P Q$ | $\frac{1}{2} \times 2 \times 3$ | 3 |  |
|  | Triangle | OQR | $\frac{1}{2} \times \frac{44}{3} \times 7$ | $\frac{154}{3}$ |  |
|  | Triangle | OWR | $\frac{1}{2} \times \frac{44}{3} \times \frac{44}{5}$ | $\frac{968}{15}$ |  |
|  | Triangle | SQR | $\frac{1}{2} \times\left(\frac{44}{3}+\frac{6}{5}\right) \times 7$ | $\frac{833}{15}$ |  |
|  | Triangle | OPR | $\frac{1}{2} \times \frac{44}{3} \times 2$ | $\frac{44}{3}$ |  |
|  | Trapezium | OPQT | $\frac{1}{2}(2+7) \times 3$ | $\frac{27}{2}$ |  |
|  | Trapezium | OPNR | $\frac{1}{2} \times\left(\frac{34}{3}+\frac{44}{3}\right) \times 2$ | 26 |  |
|  | Trapezium | OVQR | $\frac{1}{2} \times\left(3+\frac{44}{3}\right) \times 7$ | $\frac{371}{6}$ |  |
|  | EXAMPLES |  |  |  |  |
| (c) | WAY 1 |  |  |  |  |
|  | or$T R Q=\frac{1}{2} \times 7 \times\left(\frac{44}{3}-3\right)$ |  | A1ft: $O P Q T=\frac{1}{2}(2+7) \times 3$ or $T R Q=\frac{1}{2} \times 7 \times\left(\frac{44}{3}-3\right)$ |  | M1A1ft |
|  | $\frac{1}{2}(2+7) \times 3+\frac{1}{2} \times 7 \times\left(\frac{44}{3}-3\right)$ |  | dM1: Correct numerical combination of areas that have been calculated correctly |  | dM1A1 |
|  | $54 \frac{1}{3}$ |  | Any exact equivalent e.g. $\frac{163}{3}, \frac{326}{6}, 54 . \dot{3}$ |  | A1 |



$$
\begin{aligned}
& \frac{1}{2} \times(7+2) \times 3+\frac{1}{2} \times \frac{" 35 "}{3} \times 7 \\
& =\frac{27}{2}+\frac{245}{6}=\frac{326}{6}
\end{aligned}
$$

## WAY 2

|  | WAY 2 |  |  |
| :---: | :---: | :---: | :---: |
|  | $\begin{gathered} P Q R=\frac{1}{2} \times \sqrt{34} \times \frac{7}{3} \times \sqrt{34} \\ \text { or } \\ O P R=\frac{1}{2} \times \frac{44}{3} \times 2 \end{gathered}$ | M1: Correct method for $P Q R$ or $O P R$ |  |
|  |  | A1ft: $P Q R=\frac{1}{2} \times \sqrt{34} \times \frac{7}{3} \times \sqrt{34}$ or $O P R=\frac{1}{2} \times \frac{44}{3} \times 2$ | M1A1ft |
|  | $\frac{1}{2} \times \sqrt{34} \times \frac{7}{3} \times \sqrt{34}+\frac{1}{2} \times \frac{44}{3} \times 2$ | dM1: Correct numerical combination of areas that have been calculated correctly | dM1A1 |
|  | $\frac{1}{2} \times \sqrt{34} \times \frac{7}{3} \times \sqrt{34}+\frac{1}{2} \times \frac{4}{3} \times 2$ | A1: Fully Correct numerical expression for the area $O R Q P$ | dM1A1 |
|  | $54 \frac{1}{3}$ | Any exact equivalent e.g. $\frac{163}{3}, \frac{326}{6}, 54 . \dot{3}$ | A1 |



$$
\begin{aligned}
& \frac{1}{2} \times \frac{" 44 "}{3} \times 2+\frac{1}{2} \times \sqrt{34} \times " \frac{7}{3} \sqrt{34} " \\
& =\frac{88}{6}+\frac{238}{6}=\frac{326}{6}
\end{aligned}
$$

## WAY 3

$$
\begin{gathered}
S Q R=\frac{1}{2} \times 7 \times \frac{238}{15} \\
\text { or } \\
S P O=\frac{1}{2} \times \frac{6}{5} \times 2 \\
\frac{1}{2} \times 7 \times \frac{238}{15}-\frac{1}{2} \times \frac{6}{5} \times 2
\end{gathered}
$$

M1: Correct method for $S Q R$ or $S P O$
A1ft: $S Q R=\frac{1}{2} \times 7 \times \frac{238}{15}$ or $S P O=\frac{1}{2} \times \frac{6}{5} \times 2$
dM1: Correct numerical combination of areas that have been calculated correctly
A1: Fully Correct numerical expression for the area ORQP
Any exact equivalent e.g. $\frac{163}{3}, \frac{326}{6}, 54 . \dot{3}$


$$
\begin{aligned}
& \frac{1}{2} \times \frac{" 238 "}{15} \times 7-\frac{1}{2} \times \frac{" 6 "}{5} \times 2 \\
& =\frac{1666}{30}-\frac{6}{5}=\frac{1630}{30}
\end{aligned}
$$

|  | WAY 4 |  |  |
| :---: | :---: | :---: | :---: |
|  | $P V Q=\frac{1}{2} \times 5 \times 3$ <br> or $Q U R=\frac{1}{2} \times 7 \times \frac{35}{3}$ | M1: Correct method for PVQ or QUR |  |
|  |  | A1ft: $P V Q=\frac{1}{2} \times 5 \times 3$ | M1A1ft |
|  |  | $\text { or } Q U R=\frac{1}{2} \times 7 \times \frac{35}{3}$ |  |
|  | OVUR $7 \times \frac{44}{3}-\frac{1}{2} \times 5 \times 3-\frac{1}{2} \times 7 \times \frac{35}{3}$ | dM1: Correct numerical combination of areas that have been calculated correctly | dM1 |
|  | OVUR $\times \frac{}{3}-\frac{1}{2} \times 5 \times 3-\frac{1}{2} \times 7 \times \frac{35}{3}$ | A1: Fully Correct numerical expression for the area ORQP | dM1 |
|  | $54 \frac{1}{3}$ | Any exact equivalent e.g. $\frac{163}{3}, \frac{326}{6}, 54 . \dot{3}$ | A1 |



$$
\begin{aligned}
& 7 \times \frac{44 "}{3}-\frac{1}{2} \times 5 \times 3-\frac{1}{2} \times \frac{" 35 "}{3} \times 7 \\
& =\frac{308}{3}-\frac{15}{2}-\frac{245}{6}=\frac{326}{6}
\end{aligned}
$$

|  | WAY 5 |  |  |
| :---: | :---: | :---: | :---: |
|  | $\begin{gathered} O W R=\frac{1}{2} \times \frac{44}{3} \times \frac{44}{5} \\ \text { or } \\ P W Q=\frac{1}{2} \times\left(\frac{44}{5}-2\right) \times 3 \end{gathered}$ | M1: Correct method for OWR or PWQ | M1A1ft |
|  |  | A1ft: $O W R=\frac{1}{2} \times \frac{44}{3} \times \frac{44}{5} \quad$ or $P W Q=\frac{1}{2} \times\left(\frac{44}{5}-2\right) \times 3$ |  |
|  | $\frac{1}{2} \times \frac{44}{3} \times \frac{44}{5}-\frac{1}{2} \times\left(\frac{44}{5}-2\right) \times 3$ | dM1: Correct numerical combination of areas that have been calculated correctly | dM1A1 |
|  |  | A1: Fully Correct numerical expression for the area $O R Q P$ |  |
|  | $54 \frac{1}{3}$ | Any exact equivalent e.g. $\frac{163}{3}, \frac{326}{6}, 54 . \dot{3}$ | A1 |



$$
\begin{aligned}
& \frac{1}{2} \times \frac{" 44 "}{5} \times \frac{" 44 "}{3}-\frac{1}{2} \times\left(\frac{44}{5}-2\right) \times 3 \\
& =\frac{968}{15}-\frac{51}{5}=\frac{163}{3}
\end{aligned}
$$

## WAY 6




$$
\begin{aligned}
& \frac{1}{2} \times 3 \times 2+\frac{1}{2} \times \frac{" 44^{\prime \prime}}{3} \times 7 \\
& =3+\frac{308}{6}=\frac{326}{6}
\end{aligned}
$$

|  | WAY 8 |  |  |
| :---: | :---: | :---: | :---: |
|  | $\frac{1}{2}\left\|\begin{array}{lllll}0 & \frac{44}{3} & 3 & 0 & 0 \\ 0 & 0 & 7 & 2 & 0\end{array}\right\|$ | M1: Uses the vertices of the quadrilateral to form a determinant $\left\|\begin{array}{lllll}0 & \frac{44}{3} & 3 & 0 & 0 \\ 0 & 0 & 7 & 2 & 0\end{array}\right\|$ | M1A1ft |
|  |  | A1ft: $\frac{1}{2}\left\|\begin{array}{lllll}0 & \frac{44}{3} & 3 & 0 & 0 \\ 0 & 0 & 7 & 2 & 0\end{array}\right\|$ |  |
|  | $\frac{1}{2}\left(\frac{44}{3} \times 7+3 \times 2\right)$ | dM1: Fully correct determinant method with no errors | dM1A1 |
|  |  | A1: Fully Correct numerical expression for the area $O R Q P$ |  |
|  | $54 \frac{1}{3}$ | Any exact equivalent e.g. $\frac{163}{3}, \frac{326}{6}, 54 . \dot{3}$ | A1 |

There will be other ways but the same approach to marking should be applied.



