

Mark Scheme (Results)

Summer 2014

Pearson Edexcel GCE in Core Mathematics 2 (6664_01)

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

PEARSON EDEXCEL GCE MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper or ag- answer given
- L or d... The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

General Principles for Core Mathematics Marking

(But note that specific mark schemes may sometimes override these general principles).

Method mark for solving 3 term quadratic:

1. Factorisation

$$(x^2 + bx + c) = (x + p)(x + q)$$
, where $|pq| = |c|$, leading to $x = ...$

$$(ax^2 + bx + c) = (mx + p)(nx + q)$$
, where $|pq| = |c|$ and $|mn| = |a|$, leading to $x = ...$

2. Formula

Attempt to use the correct formula (with values for a, b and c).

3. Completing the square

Solving
$$x^2 + bx + c = 0$$
: $\left(x \pm \frac{b}{2}\right)^2 \pm q \pm c = 0$, $q \neq 0$, leading to $x = \dots$

Method marks for differentiation and integration:

1. Differentiation

Power of at least one term decreased by 1. $(x^n \rightarrow x^{n-1})$

2. Integration

Power of at least one term increased by 1. $(x^n \rightarrow x^{n+1})$

Use of a formula

Where a method involves using a formula that has been learnt, the advice given in recent examiners' reports is that the formula should be quoted first.

Normal marking procedure is as follows:

<u>Method mark</u> for quoting a correct formula and attempting to use it, even if there are small errors in the substitution of values.

Where the formula is <u>not</u> quoted, the method mark can be gained by implication from <u>correct</u> working with values, but may be lost if there is any mistake in the working.

Exact answers

Examiners' reports have emphasised that where, for example, an exact answer is asked for, or working with surds is clearly required, marks will normally be lost if the candidate resorts to using rounded decimals.

Question Number	Scheme					Marks
Number	x 1	1.25	1.5	1.75	2	
	y 1.414	1.601	1.803	2.016	2.236	
1.(a)	{At $x = 1.25$,} $y = 1.601$ (only) $\begin{cases} 1.601 \text{ (May not be in the table and can score if seen as part of their working in (b))} \end{cases}$			B1 cao		
						[1]
	$\frac{1}{2} \times 0.25; \times \left\{1.\right\}$	414 + 2.236 + 2	(their 1.60	1+1.803 + 2.	.016)}	B1; M1 A1ft
	B1; for using $\frac{1}{2} \times 0.25$ or $\frac{1}{8}$ or equivalent.	M1: Structure of {}		A1ft: for the correct expression as shown following through candidate's y value found in part (a).		
	M1 requires the correct structure for the y values. It needs to contain first y value plus last y value and the second bracket to be multiplied by 2 and to be the summation of the remaining y values in the table with no additional values. If the only mistake is a copying error or is to omit one value from 2() bracket this may be regarded as a slip and the M mark can be allowed (nb: an extra repeated term, however, forfeits the M mark). M0 if any values used are x values instead of y values. A1ft: for the correct underlined expression as shown following through candidate's y value					
(b)	found in part (a). Bracketing mistakes: e.g. $\left(\frac{1}{2} \times \frac{1}{4}\right) (1.414 + 2.236) + 2 \left(\text{their } 1.601 + 1.803 + 2.016\right) (=11.29625)$					
	$\left(\frac{1}{2} \times \frac{1}{4}\right) 1.414 + 2.236 + 2 \text{ (their } 1.601 + 1.803 + 2.016 \text{)} (= 13.25275)$ Both score B1 M1 A0 unless the final answer implies that the calculation has been done correctly (then full marks could be given).					
	Alternative: Separate trapezia may be used, and this can be marked equivalently.					
	$\left[\frac{1}{8} (1.414 + 1.601) + \frac{1}{8} (1.601 + 1.803) + \frac{1}{8} (1.803 + 2.016) + \frac{1}{8} (2.016 + 2.236) \right]$					
	B1 for $\frac{1}{8}$ (aef), M1 for correct	structure, 1st A	T		on, ft their 1.601	
	$\left\{ = \frac{1}{8}(14.49) \right\} = 1.81125$		1.81 or a			A1
	Correct answer only in (b) scores no marks If required accuracy is not seen in (a), full marks can still be scored in (b) (e.g. uses 1.6)					
						[4]
						Total 5

Question Number	Scheme		
	If there is no labelling, ma	rk (a) and (b) in that order	
	$f(x) = 2x^3 - 7x^2 + 4x + 4$		
	$f(2) = 2(2)^3 - 7(2)^2 + 4(2) + 4$	Attempts f(2) or f(-2)	M1
2. (a)	f(2) = 0 with no sign or substitution errors $(2(2)^3 - 7(2)^2 + 4(2) + 4 = 0 \text{ is sufficient})$ and for conclusion. Stating "hence factor" or "it is a factor" or a "tick" or "QED" or "no remainder" or "as required" are fine for the conclusion but not = 0 just underlined and not hence (2 or f(2)) is a factor. Note also that a conclusion can be implied from a preamble, eg: "If $f(2) = 0$, $(x - 2)$ is a factor"		A1
	Note: Long division scores no marks in part (a). The <u>factor theorem</u> is required.		
	$f(x) = \{(x-2)\}(2x^2 - 3x - 2)$	M1: Attempts long division by $(x-2)$ or other method using $(x-2)$, to obtain $(2x^2 \pm ax \pm b)$, $a \ne 0$, even with a remainder. Working need not be seen as this could be done "by inspection." A1: $(2x^2 - 3x - 2)$	[2] M1 A1
(b)	$= (x-2)(x-2)(2x+1) \text{ or } (x-2)^{2}(2x+1)$ or equivalent e.g. $= 2(x-2)(x-2)(x+\frac{1}{2}) \text{ or } 2(x-2)^{2}(x+\frac{1}{2})$	dM1: Factorises a 3 term quadratic. (see rule for factorising a quadratic in the General Principles for Core Maths Marking). This is dependent on the previous method mark being awarded but there must have been no remainder. Allow an attempt to solve the quadratic to determine the factors. A1: cao – needs all three factors on one line. Ignore following work (such as a solution to a quadratic equation.)	d M1 A1
	Note = $(x-2)(\frac{1}{2}x-1)(4x+2)$ would lose the last mark as it is not fully factorised		
	For correct answers onl	y award full marks in (b)	
			[4]
			Total 6

Question Number	Scheme			
3. (a)	$(2-3x)^6 = 64 + \dots$ 64 seen as the only constant term in their expansion.		B1	
	$\left\{ (2-3x)^6 \right\} = (2)^6 + \frac{{}^6C_1}{}(2)^5(-3\underline{x}) + \frac{{}^6C_2}{}(2)^4(-3\underline{x})^2 + \dots$			
	M1: $({}^{6}C_{1} \times \times x)$ or $({}^{6}C_{2} \times \times x^{2})$. For <u>either</u> the x term <u>or</u> the x^{2} term. Requires <u>correct</u>			
	binomial coefficient in any form with the corcoefficient (perhaps including powers of 2 and/o can be "listed" rather than adde	or -3) may be wrong or missing. The terms		
	$^{6}\text{C}_{1}2^{5} - 3x + {^{6}\text{C}}_{2}2^{4} - 3x^{2} + \dots$ Scores M0 u			
	1 2	A1: Either $-576x$ or $2160x^2$		
	2	(Allow + -576x here)		
	$= 64 - 576x + 2160x^2 + \dots$	A1: Both $-576x$ and $2160x^2$	A1A1	
		(Do not allow $+ -576x$ here)		
			[4]	
(a) Way 2	$(2-3x)^6 = 64 + \dots$	64 seen as the only constant term in their expansion.	B1	
		M1: $\binom{6}{1} \times \times x$ or $\binom{6}{1} \times \times x^2$. For		
	$\left(1 - \frac{3}{2}x\right)^6 = 1 + \frac{{}^6C_1}{2}\left(\frac{-3}{2}x\right) + \frac{{}^6C_2}{2}\left(\frac{-3}{2}x\right)^2 + \dots$	either the x term or the x^2 term. Requires correct binomial coefficient in any form with the correct power of x , but the other part of the coefficient (perhaps including powers of 2 and/or -3) may be wrong or missing. The terms can be "listed" rather than added. Ignore any extra terms.	<u>M1</u>	
		A1: Either $-576x$ or $2160x^2$		
	$= 64 - 576x + 2160x^2 +$	(Allow + -576x here)	A1A1	
	= 04 370x + 2100x +	A1: Both $-576x$ and $2160x^2$ (Do not allow $+ -576x$ here)	711711	
(b)	Candidate writes down $\left(1+\frac{x}{2}\right)\times\left(\text{their part}\right)$	(a) answer, at least up to the term in x).		
	(Condone missing brackets)			
	$\left(1+\frac{x}{2}\right)\left(64-576x+\right)$ or $\left(1+\frac{x}{2}\right)\left(64-576x+2160x^2+\right)$ or		M1	
	$\left(1 + \frac{x}{2}\right) 64 - \left(1 + \frac{x}{2}\right) 576x \text{ or } \left(1 + \frac{x}{2}\right) 64 - \left(1 + \frac{x}{2}\right) 576x + \left(1 + \frac{x}{2}\right) 2160x^2$			
	or $64 + 32x, -576x - 288x^2$,	$2160x^2 + 1080x^3$ are fine.		
		A1: At least 2 terms correct as shown. (Allow $+ -544x$ here)		
	$= 64 - 544x + 1872x^2 + \dots$	A1: $64 - 544x + 1872x^2$ The terms can be "listed" rather than	A1A1	
		added. Ignore any extra terms.	[3]	
			Total 7	
SC: If a candidate expands in descending powers of x, only the M marks are avail				
	e.g. $\{(2-3x)^6\} = (-3x)^6 + \frac{{}^6C_1(2)^2(-3x)^5}{} + \frac{{}^6C_2(2)^2(-3x)^4}{} + \dots$			

Question Number	Sche	me	Marks	
4.		$M1: x^n \to x^{n+1}$		
		A1: At least one of either $\frac{x^4}{6(4)}$ or $\frac{x^{-1}}{(3)(-1)}$.		
	$\left\{ \int \left(\frac{x^3}{6} + \frac{1}{3x^2} \right) dx \right\} = \frac{x^4}{6(4)} + \frac{x^{-1}}{(3)(-1)}$	A1: $\frac{x^4}{6(4)} + \frac{x^{-1}}{(3)(-1)}$ or equivalent.	M1A1A1	
		e.g. $\frac{x^4}{\frac{6}{4}} + \frac{x^{-1}}{\frac{3}{-1}}$ (they will lose the final mark		
		if they cannot deal with this correctly)		
	Note that some candidates may change	• 0 0 0		
	$\int \frac{x^3}{6} + \frac{1}{3x^2} dx = \int 3x^5 + 6dx $ in which case al	llow the M1 if $x^n \to x^{n+1}$ for their changed		
	function and allow the	M1 for limits if scored		
	$\left\{ \int_{1}^{\sqrt{3}} \left(\frac{x^3}{6} + \frac{1}{3x^2} \right) dx \right\} = \left(\frac{\left(\sqrt{3}\right)}{24} \right)$	$- + \frac{\left(\sqrt{3}\right)^{-1}}{-1(3)} - \left(\frac{\left(1\right)^{4}}{24} + \frac{\left(1\right)^{-1}}{-1(3)}\right)$	d M1	
	2^{nd} dM1: For using limits of $\sqrt{3}$ and 1 on an int way round. The 2^{nd} M1 is dependent	tegrated expression and subtracting the correct ent on the 1 st M1 being awarded.		
	•	$\frac{2}{3} - \frac{1}{9}\sqrt{3}$ or $a = \frac{2}{3}$ and $b = -\frac{1}{9}$.		
	$= \left(\frac{9}{24} - \frac{1}{3\sqrt{3}}\right) - \left(\frac{1}{24} - \frac{1}{3}\right) = \frac{2}{3} - \frac{1}{9}\sqrt{3}$	Allow equivalent fractions for <i>a</i> and/or <i>b</i> and 0.6 recurring and/or 0.1 recurring but do not	Alcso	
		allow $\frac{6-\sqrt{3}}{9}$		
	This final mark is cao and cso – there	e must have been no previous errors		
		•	Total 5	
	Common Errors (I	Usually 3 out of 5)		
	$\left\{ \int \left(\frac{x^3}{6} + \frac{1}{3x^2} \right) dx \right\} = \int \left(\frac{x^3}{6} + 3x \right) dx$			
	$\left\{ \int_{1}^{\sqrt{3}} \left(\frac{x^{3}}{6} + \frac{1}{3x^{2}} \right) dx \right\} = \left(\frac{\left(\sqrt{3}\right)^{4}}{24} + \frac{1}{3x^{2}} \right) dx $	$\frac{3(\sqrt{3})^{-1}}{-1} - \left(\frac{(1)^4}{24} + \frac{3(1)^{-1}}{-1}\right) dM1$		
	$=\left(\frac{9}{24}-\frac{3}{\sqrt{3}}\right)-\left(\frac{1}{24}\right)$	$+\frac{3}{-1} = \frac{10}{3} - \sqrt{3} A0$		
	$\left\{ \int \left(\frac{x^3}{6} + \frac{1}{3x^2} \right) dx \right\} = \int \left(\frac{x^3}{6} + \left(3x \right)^{-2} \right) dx = \frac{x^4}{6(4)} + \frac{\left(3x \right)^{-1}}{(-1)} \text{ M1A1A0}$			
	$\left\{ \int_{1}^{\sqrt{3}} \left(\frac{x^{3}}{6} + \frac{1}{3x^{2}} \right) dx \right\} = \left(\frac{\left(\sqrt{3}\right)^{4}}{24} + \frac{\left(3\sqrt{3}\right)^{-1}}{-1} \right) - \left(\frac{\left(1\right)^{4}}{24} + \frac{\left(3\times1\right)^{-1}}{-1} \right) dM 1$			
	$=\left(\frac{9}{24}-\frac{1}{3\sqrt{3}}\right)-\left(\frac{1}{24}\right)$			
	Note this is the correct answer	r but follows incorrect work.		

Question Number	Scheme		Mark
5.(a)	Area $BDE = \frac{1}{2}(5)^2(1.4)$	M1: Use of the correct formula or method for the area of the sector	
	$=17.5 \text{ (cm}^2)$	A1: 17.5 oe	
(h)	Douts (h) and (a) a	an he manked to gether	[2
(b)	Parts (b) and (c) can be marked together $6.1^{2} = 5^{2} + 7.5^{2} - (2 \times 5 \times 7.5 \cos DBC) \text{or} \cos DBC = \frac{5^{2} + 7.5^{2} - 6.1^{2}}{2 \times 5 \times 7.5} \text{(or equivalent)}$		
	M1: A correct statement involving the angle DBC		
	Angle $DBC = 0.943201$	awrt 0.943	A1
	Note that work for (b) may be	seen on the diagram or in part (c)	
(c)	Note that candidates may work in deg	grees in (c) (Angle $DBC = 54.04$ deg rees)	[2
		$\frac{1}{2}$ 5(7.5)sin(0.943)	
		Area $CBD = \frac{1}{2}5(7.5)\sin(\text{their } 0.943)$ or awrt	
	Angle $EBA = \pi - 1.4 - "0.943"$	15.2. (Note area of $CBD = 15.177$)	M1
	(Maybe seen on the diagram)	A correct method for the area of triangle <i>CBD</i> which can be implied by awrt 15.2	
	$\pi - 1.4$ – "their 0.943"		
	A value for angle <i>EBA</i> of awrt 0.8 (from 0.7985926536 or 0.7983916536) or value for angle		
	EBA of $(1.74159 \text{their angle } DBC)$ would imply this mark.		
	$AB = 5\cos(\pi - 1.4 - "0.943")$		
	or $AE = 5\sin(\pi - 1.4 - 0.943)$		
		$AB = 5\cos(\pi - 1.4 - \text{their } 0.943)$	
		$AB = 5\cos(0.79859) = 3.488577938$	
		Allow M1 for $AB = \text{awrt } 3.49$	
		Or	
		$AE = 5\sin(\pi - 1.4 - \text{their } 0.943)$	
		$AE = 5\sin(0.79859) = 3.581874365688$	
		Allow M1 for $AE = \text{awrt } 3.58$	M1
		It must be clear that $\pi - 1.4 - 0.943$ is	
		being used for angle EBA. Note that some candidates use the sin rule here but it must be used correctly – do not allow mixing of degrees and radians.	
	Area $EAB = \frac{1}{2}5\cos(\pi - 1.4 - 1.4)$	$(0.943'') \times 5\sin(\pi - 1.4 - (0.943''))$	
	This is dependent on the previous M1 and there must be no other errors in finding the area of triangle EAB		dM1
		area $EAB = \text{awrt } 6.2$	
	Area <i>ABCDE</i> = 15.1/.	+ 17.5 + 6.24 = 38.92	
		awrt 38.9	Alcs
	Note that a sign error in (b) can give the obt answer in (c) – this would lose the final mar	use angle (2.198) and could lead to the correct	Tota

Question Number	Sc	cheme	Marks	
6(a)	s 20 . 160	M1: Use of a correct S_{∞} formula	3.54.1.4	
	$S_{\infty} = \frac{20}{1 - \frac{7}{8}} ; = 160$	A1: 160	M1A1	
	Accept correct	answer only (160)		
			[2]	
(b)	$20(1-(7)^{12})$	M1: Use of a correct S_n formula with $n = 12$		
	$S_{12} = \frac{20(1-(\frac{7}{8})^{12})}{1-\frac{7}{2}}$; = 127.77324	(condone missing brackets around 7/8)	M1A1	
	$1-\frac{7}{8}$	A1: awrt 127.8		
	T & I in (b) requires all 12 terms to be calc	ulated correctly for M1 and A1 for awrt 127.8		
()		T	[2]	
(c)	20/1 (7.1)	Applies S_N (GP only) with $a = 20$, $r = \frac{7}{8}$ and		
	$160 - \frac{20(1 - (\frac{7}{8})^N)}{1 - \frac{7}{2}} < 0.5$	"uses" 0.5 and their S_{∞} at any point in their	M1	
	$1-\frac{1}{8}$	working. (condone missing brackets around $7/8$)(Allow =, <, >, \geq , \leq) but see note below.		
	$(7)^N$ $(7)^N$ (0.5)	Attempt to isolate $+160\left(\frac{7}{8}\right)^N$ or $+\left(\frac{7}{8}\right)^N$ oe		
	$160\left(\frac{7}{8}\right)^{N} < (0.5) \text{ or } \left(\frac{7}{8}\right)^{N} < \left(\frac{0.5}{160}\right)$	(Allow =, $<$, $>$, \ge , \le) but see note below.	dM1	
	(0) (100)	Dependent on the previous M1		
		Uses the power law of logarithms or takes logs		
		base 0.875 correctly to obtain an equation or an inequality of the form		
	$N\log\left(\frac{7}{8}\right) < \log\left(\frac{0.5}{160}\right)$			
		$N\log\left(\frac{7}{8}\right) < \log\left(\frac{0.5}{\text{their }S_{\infty}}\right)$	M1	
		or	1.22	
		$N > \log_{0.875} \left(\frac{0.5}{\text{their } S_{\infty}} \right)$		
		(Allow =, $<$, $>$, \ge , \le) but see note below.		
	$N > \frac{\log(\frac{0.5}{160})}{\log(\frac{7}{8})} = 43.19823 \Rightarrow N = 44$	$N = 44$ (Allow $N \ge 44$ but not $N > 44$	A1 cso	
	Some candidates do not realise that the direc	e in a candidate's working loses the final mark. tion of the inequality is reversed in the final line full marks for using =, as long as no incorrect		
	Q ****		[4]	
	m	(M. 1: ()	Total 8	
		provement Method in (c):		
		or S_N with at least one value for $N > 40$		
		$0 - S_N$ or S_N with $N = 43$ or $N = 44$		
	3^{rd} M1: For evidence of examining $160 - S_N$ or S_N for both $N = 43$ and $N = 44$ with both			
	correct to 2 DP			
	Eg: $160 - S_{43} = \text{awrt } 0.51 \text{ and } 160 - S_{44} = \text{awrt } 0.45$			
	or $S_{43} = \text{awrt} 159.49 \text{ and } S_{44} = \text{awrt} 159.55$ $A1: N = 44 \text{ cso}$ Answer of $N = 44$ only with no working scores no marks			
	Allswei ui Iv – 44 uiii	y with he werking stores he marks		

Question Number	Scheme		
_	(i) $9\sin(\theta + 60^{\circ})$	$=4; 0 \le \theta < 360^{\circ}$	
7.	(ii) $2\tan x - 3\sin$	$x = 0; -\pi \le x < \pi$	
(i)	$\sin(\theta + 60^{\circ}) = \frac{4}{9}$, so $(\theta + 60^{\circ}) = 26.3877$	Sight of $\sin^{-1}\left(\frac{4}{9}\right)$ or awrt 26.4° or 0.461°	M1
	$(\alpha = 26.3877)$	Can also be implied for $\theta = \text{awrt} - 33.6$ (i.e. $26.4 - 60$)	1411
	So, $\theta + 60^{\circ} = \{153.6122, 386.3877\}$	$\theta + 60^{\circ}$ = either "180 – their α " or "360° + their α " and not for θ = either "180 – their α " or "360° + their α ". This can be implied by later working. The candidate's α could also be in radians but do not allow mixing of degrees and radians.	M1
		A1: At least one of	
	and $\theta = \{93.6122, 326.3877\}$	awrt 93.6° or awrt 326.4°	A1 A1
		A1: Both awrt 93.6° and awrt 326.4°	
		nust come from correct work	
		ns outside the range. et the final A1for any extra solutions in range	
	in an otherwise runy correct solution deduct the final 711101 any extra solutions in runge		
(ii)	$2\left(\frac{\sin x}{\cos x}\right) - 3\sin x = 0$	Applies $\tan x = \frac{\sin x}{\cos x}$	M1
	Note: Applies $\tan x = \frac{\sin x}{\cos x}$ can be implied	1 by $2\tan x - 3\sin x = 0 \Rightarrow \tan x (2 - 3\cos x)$	
	$2\sin x - 3\sin x$	$ in x \cos x = 0 $	
	$\sin x(2-3)$	$3\cos x) = 0$	
	$\cos x = \frac{2}{3}$	$\cos x = \frac{2}{3}$	A1
	$x = \text{awrt}\{0.84, -0.84\}$	A1: One of either awrt 0.84 or awrt -0.84 A1ft: You can apply ft for $x = \pm \alpha$, where $\alpha = \cos^{-1} k$ and $-1 \le k \le 1$	A1A1ft
	In this part of the solution, if there are a	ny extra answers in range in an otherwise	
		withhold the A1ft.	
	$\{\sin x = 0 \Rightarrow\} x = 0 \text{ and } -\pi$ $\{\sin x = 0 \Rightarrow\} x = 0 \text{ and } -\pi$ Both $x = 0 \text{ and } -\pi$ or awrt -3.14 from $\sin x = 0$ In this part of the solution, ignore extra solutions in range.		B1
	Note solutions are: $x = \{-3.1415, -0.8410, 0, 0.8410\}$		
	Ignore extra solutions outside the range		
	For all answers in degrees in (ii) M1A1A0A1ftB0 is possible		
	Allow the use of θ	in place of x in (ii)	
			[5] Total 9
			10(817

Question Number	Scheme			Marks
8.	Graph of $y = 3^x$ and solving	$3^{2x} - 9(3^x) + 18$	B = 0	
(a)			the three criteria correct. notes below.)	B1
		(See	e criteria correct. notes below.)	B1
	y ↑	curve for $x \ge 0$ positive <i>y</i> -axis.	er 1: Correct shape of and at least touches the er 2: Correct shape of	
	(0,1)	curve for $x < 0$ axis or have any	o. Must not touch the x-y turning points. er 3: (0, 1) stated or in	
	O x	Allow (1, 0) rat marked in the "	tked on the y-axis. ther than (0, 1) if correct" place on the y-	
		axis.		[2]
(b)	$(3^{x})^{2} - 9(3^{x}) + 18 = 0$ or $y = 3^{x} \Rightarrow y^{2} - 9y + 18 = 0$	Forms a quadratic of the correct form in 3^x or in "y" where "y" = 3^x or even in x where "x" = 3^x		M1
	$y = 3^x \Rightarrow y^2 - 9y + 18 = 0$ { $(y-6)(y-3) = 0$ or $(3^x - 6)(3^x - 3) = 0$ }			
	$y = 6$, $y = 3$ or $3^x = 6$, $3^x = 3$	Both $y = 6$ an	d $y = 3$.	A1
	$\left\{3^x = 6 \Rightarrow\right\} x \log 3 = \log 6$	A valid method where $k > 0$, $k = 0$		
	or $x = \frac{\log 6}{\log 3}$ or $x = \log_3 6$	to give either	$x \log 3 = \log k \text{ or}$ $x = \frac{\log k}{\log 3} \text{ or } x = \log_3 k$	dM1
	x = 1.63092	awrt 1.63		Alcso
	Provided the first M1A1 is scored, the second			
	<i>x</i> = 1	x = 1 stated as a working.	a solution from <i>any</i>	B1
				[5]
				Total 7

Question	Scheme Marks				
Number	M 1 () 1 () ()				
0 (a)	Mark (a) and (b) together Uses the addition form of Pythagoras				
9. (a)					
	on $6\sqrt{5}$ and 4. Condone missing				
	$OQ^2 = (6\sqrt{5})^2 + 4^2 \text{ or } OQ = \sqrt{(6\sqrt{5})^2 + 4^2} \{=14\} \text{brackets on } (6\sqrt{5})^2$	M1			
	(Working or 14 may be seen on the diagram)				
	$y_Q = \sqrt{(\text{their } OQ)^2 - 11^2}$				
	$y_Q = \sqrt{14^2 - 11^2}$ Must include $\sqrt{\text{and is dependent on}}$ the first M1 and requires OQ > 11	dM1			
	$=\sqrt{75} \text{ or } 5\sqrt{3}$ $\sqrt{75} \text{ or } 5\sqrt{3}$	A1cso			
(b)	M1: $(x \pm 11)^2 + (y \pm \text{their } k)^2 = 4^2$				
	Equation must be of this form and must use x and y not other letters. k could be their last answer to part (a). Allow their $k \neq 0$ or just the letter k .	- M1A1			
	A1: $(x-11)^2 + (y-5\sqrt{3})^2 = 16$ or $(x-11)^2 + (y-5\sqrt{3})^2 = 4^2$				
	NB $5\sqrt{3}$ must come from correct				
	Work in (a) and allow awrt 8.66 Allow in expanded form for the final A1				
	1				
	e.g. $x^2 - 22x + 121 + y^2 - 10\sqrt{3}y + 75 = 16$				
		[2]			
		Total 5			
	Watch out for:				
	(a) $OQ = \sqrt{(6\sqrt{5})^2 + 4^2} = \sqrt{46} \text{ M1}$				
	$y_Q = \sqrt{46 - 11^2} \text{ M0 (OQ} < 11)$				
	$y_Q = \sqrt{75} \text{ A0}$				
	(b) $(x-11)^2 + (y-5\sqrt{3})^2 = 16 \text{ M1A0}$				

Question Number	Scheme		Marks	
10. (a)	$\frac{1}{2}(9x+6x)4x$ or $2x\times15x$ or $\left(\frac{1}{2}4x\times(9x-6x)+6x\times4x\right)$ or $6x^2+24x^2$ or $\left(9x\times4x-\frac{1}{2}4x\times(9x-6x)\right)$ or $36x^2-6x^2$	or $2x \times 15x$		
	$\Rightarrow 30x^2y = 9600 \Rightarrow y = \frac{9600}{30x^2} \Rightarrow y = \frac{320}{x^2} *$	intermediate step and no err "y =" is required.		
(b)	$(S =) \frac{1}{2} (9x + 6x) 4x + \frac{1}{2} (9x + 6x) 4x + 6xy + 9xy + 5xy + 4xy$			
	M1: An attempt to find the area of six faces of the $(9x + 6x)4x$ or $60x^2$ and the 4 other faces may be 6			
	included. There must be attempt at the areas of two trapezia that are dimensionally correct. A1: Correct expression in any form. Allow just $(S =) 60x^2 + 24xy$ for M1A1			
	$y = \frac{320}{x^2} \Rightarrow (S =) 30x^2 + 30x^2 + 24x \left(\frac{320}{x^2}\right)$			
	Substitutes $y = \frac{320}{x^2}$ into their expression for S (may be done earlier). S should have at least			
	one x^2 term and one xy term but there may be other terms which may be dimensionally incorrect.			
	So, $(S =) 60x^2 + \frac{7680}{x} *$	Correct solution "S = " is not re		
		•	[4]	

10(c)	$\frac{dS}{dx} = 120x - 7680x^{-2} \left\{ = 120x - \frac{7680}{x^2} \right\}$	M1: Either $60x^2 \rightarrow 120x$ or $\frac{7680}{x} \rightarrow \frac{\pm \lambda}{x^2}$ A1: Correct differentiation (need not be	M1
		A1: Correct differentiation (need not be simplified).	A1 aef
	$120x - \frac{7680}{x^2} = 0$ $\Rightarrow x^3 = \frac{7680}{120}; = 64 \Rightarrow x = 4$	simplified). M1: $S' = 0$ and "their $x^3 = \pm$ value" or "their $x^{-3} = \pm$ value" Setting their $\frac{dS}{dx} = 0$ and "candidate's ft <i>correct</i> power of $x = a$ value". The power of x must be consistent with their differentiation . If inequalities are used this mark cannot be gained until candidate states value of x or S from their x without inequalities. $S' = 0$ can be implied by $120x = \frac{7680}{x^2}$. Some may spot that $x = 4$ gives $S' = 0$ and provided they clearly show $S'(4) = 0$ allow this mark as long as S' is correct. (If S' is incorrect this method is allowed if their derivative is clearly zero for their value of x) A1: $x = 4$ only ($x^3 = 64 \Rightarrow x = \pm 4$ scores A0) Note that the value of x is not explicitly required so the use of $x = \sqrt[3]{64}$ to give $S = 2880$ would	M1A1cso
	Note some candidates stop here and do	imply this mark. o not go on to find S – maximum mark is 4/6	
		Substitute candidate's value of $x \neq 0$ into a	
	$\{x=4,\}$	formula for S. Dependent on both previous M	ddM1
	$S = 60(4)^2 + \frac{7680}{4} = 2880 \text{ (cm}^2\text{)}$	marks.	
	$3 - 00(4) + \frac{1}{4} = 2000 \text{ (CIII)}$	2880 cso (Must come from correct work)	A1 cao and cso
			[6]

10(d)		M1: Attempt $S''(x^n \to x^{n-1})$ and considers	
		sign.	
		This mark requires an attempt at the second	
		derivative and some consideration of its sign.	
		There does not necessarily need to be any	
	.2	substitution. An attempt to solve $S'' = 0$ is M0	
	$\frac{d^2S}{dx^2} = 120 + \frac{15360}{x^3} > 0$	A1: $120 + \frac{15360}{x^3}$ and > 0 and conclusion.	M1A1ft
	⇒ Minimum	Requires a correct second derivative of	
		$120 + \frac{15360}{x^3}$ (need not be simplified) and a	
		valid reason (e.g. > 0), <u>and</u> conclusion.	
		Only follow through a correct second derivative	
		i.e. x may be incorrect but must be positive	
		and/or S'' may have been <u>evaluated</u> incorrectly.	
	A correct S'' followed by $S''("4") = "360"$ th	nerefore minimum would score no marks in (d)	
	A correct S'' followed by S''("4") = "360" w	hich is positive therefore minimum would score	
	bot	h marks	
			[2]
	Note parts (c) and (d) can be marked together.	
			Total 14

