

4. A particle P of mass m is moving in a straight line on a smooth horizontal table. Another particle Q of mass km is at rest on the table. The particle P collides directly with Q . The direction of motion of P is reversed by the collision. After the collision, the speed of P is v and the speed of Q is $3v$. The coefficient of restitution between P and Q is $\frac{1}{2}$.

(a) Find, in terms of v only, the speed of P before the collision. (3)

(b) Find the value of k . (3)

After being struck by P , the particle Q collides directly with a particle R of mass $11m$ which is at rest on the table. After this second collision, Q and R have the same speed and are moving in opposite directions. Show that

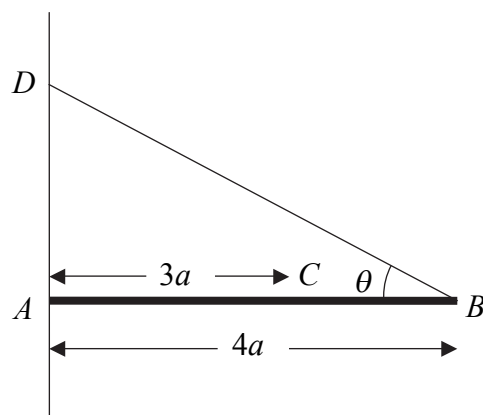
(c) the coefficient of restitution between Q and R is $\frac{3}{4}$, (4)

(d) there will be a further collision between P and Q . (2)



5.

Figure 2



A horizontal uniform rod AB has mass m and length $4a$. The end A rests against a rough vertical wall. A particle of mass $2m$ is attached to the rod at the point C , where $AC = 3a$. One end of a light inextensible string BD is attached to the rod at B and the other end is attached to the wall at a point D , where D is vertically above A . The rod is in equilibrium in a vertical plane perpendicular to the wall. The string is inclined at an angle θ to the horizontal, where $\tan \theta = \frac{3}{4}$, as shown in Figure 2.

(a) Find the tension in the string. (5)

(b) Show that the horizontal component of the force exerted by the wall on the rod has magnitude $\frac{8}{3}mg$. (3)

The coefficient of friction between the wall and the rod is μ . Given that the rod is in limiting equilibrium,

(c) find the value of μ . (4)



6. A particle P of mass 0.5 kg is moving under the action of a single force \mathbf{F} newtons. At time t seconds, $\mathbf{F} = (1.5t^2 - 3)\mathbf{i} + 2t\mathbf{j}$. When $t = 2$, the velocity of P is $(-4\mathbf{i} + 5\mathbf{j}) \text{ m s}^{-1}$.

(a) Find the acceleration of P at time t seconds. (2)

(b) Show that, when $t = 3$, the velocity of P is $(9\mathbf{i} + 15\mathbf{j}) \text{ m s}^{-1}$. (5)

When $t = 3$, the particle P receives an impulse \mathbf{Q} N s. Immediately after the impulse the velocity of P is $(-3\mathbf{i} + 20\mathbf{j}) \text{ m s}^{-1}$. Find

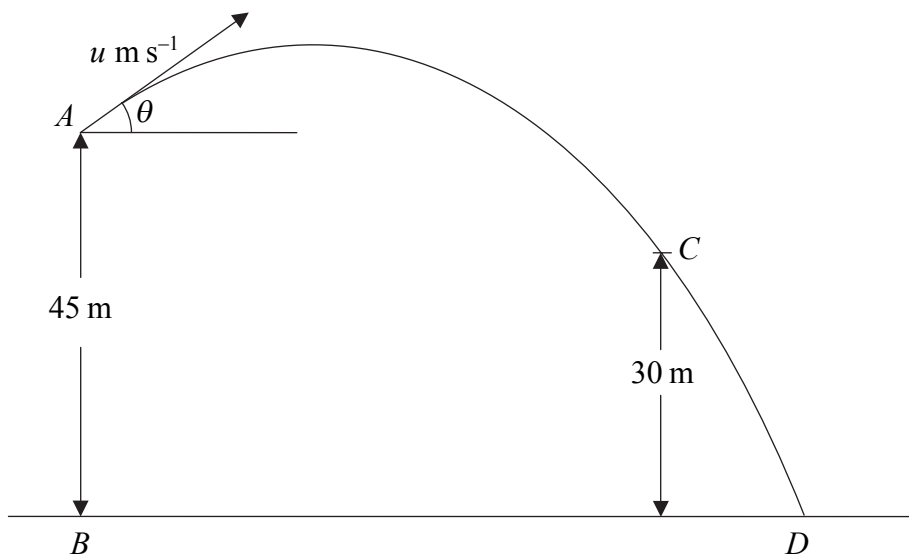
(c) the magnitude of \mathbf{Q} , (3)

(d) the angle between \mathbf{Q} and \mathbf{i} . (3)



7.

Figure 3



A particle P is projected from a point A with speed $u \text{ m s}^{-1}$ at an angle of elevation θ , where $\cos \theta = \frac{4}{5}$. The point B , on horizontal ground, is vertically below A and $AB = 45 \text{ m}$. After projection, P moves freely under gravity passing through a point C , 30 m above the ground, before striking the ground at the point D , as shown in Figure 3.

Given that P passes through C with speed 24.5 m s^{-1} ,

- using conservation of energy, or otherwise, show that $u = 17.5$,
(4)
- find the size of the angle which the velocity of P makes with the horizontal as P passes through C ,
(3)
- find the distance BD .
(7)



Leave
blank

Question 7 continued

Lined writing area for Question 7 continued, consisting of 30 horizontal lines.

(Total 14 marks)

Q7

TOTAL FOR PAPER: 75 MARKS

END

