





2. At time  $t$  seconds ( $t \geq 0$ ), a particle  $P$  has position vector  $\mathbf{p}$  metres, with respect to a fixed origin  $O$ , where

$$\mathbf{p} = (3t^2 - 6t + 4)\mathbf{i} + (3t^3 - 4t)\mathbf{j}.$$

Find

(a) the velocity of  $P$  at time  $t$  seconds, (2)

(b) the value of  $t$  when  $P$  is moving parallel to the vector  $\mathbf{i}$ . (3)

When  $t = 1$ , the particle  $P$  receives an impulse of  $(2\mathbf{i} - 6\mathbf{j})$  N s. Given that the mass of  $P$  is 0.5 kg,

(c) find the velocity of  $P$  immediately after the impulse. (4)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

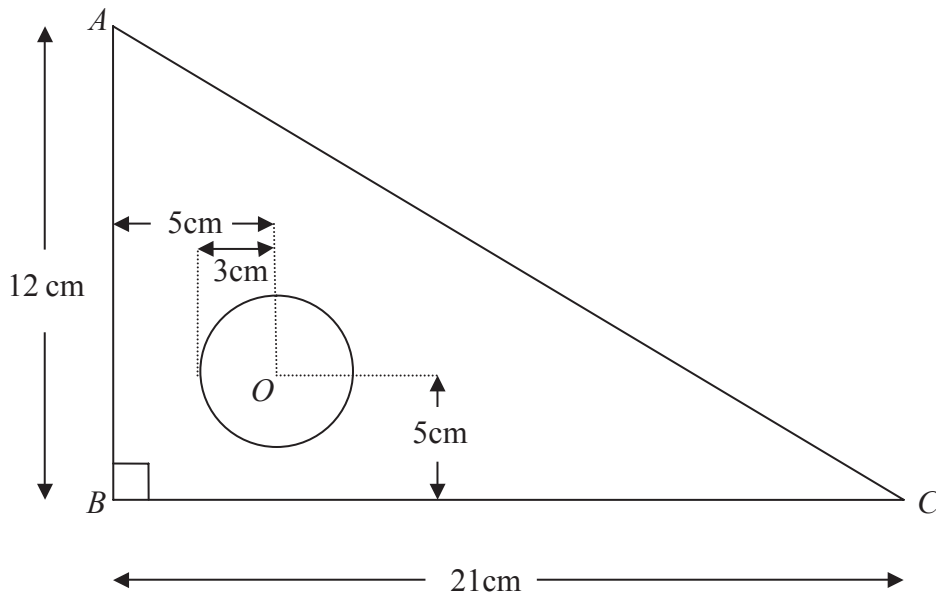
---

---

---



4.

**Figure 1**

A set square  $S$  is made by removing a circle of centre  $O$  and radius 3 cm from a triangular piece of wood. The piece of wood is modelled as a uniform triangular lamina  $ABC$ , with  $\angle ABC = 90^\circ$ ,  $AB = 12$  cm and  $BC = 21$  cm. The point  $O$  is 5 cm from  $AB$  and 5 cm from  $BC$ , as shown in Figure 1.

(a) Find the distance of the centre of mass of  $S$  from

(i)  $AB$ ,

(ii)  $BC$ .

**(9)**

The set square is freely suspended from  $C$  and hangs in equilibrium.

(b) Find, to the nearest degree, the angle between  $CB$  and the vertical.

**(3)**


---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---





**Question 4 continued**

Blank lined writing area for the answer to Question 4.



5.

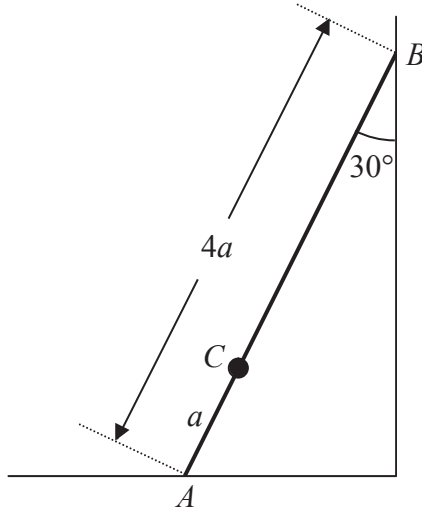


Figure 2

A ladder  $AB$ , of mass  $m$  and length  $4a$ , has one end  $A$  resting on rough horizontal ground. The other end  $B$  rests against a smooth vertical wall. A load of mass  $3m$  is fixed on the ladder at the point  $C$ , where  $AC = a$ . The ladder is modelled as a uniform rod in a vertical plane perpendicular to the wall and the load is modelled as a particle. The ladder rests in limiting equilibrium making an angle of  $30^\circ$  with the wall, as shown in Figure 2.

Find the coefficient of friction between the ladder and the ground.

(10)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---







6.

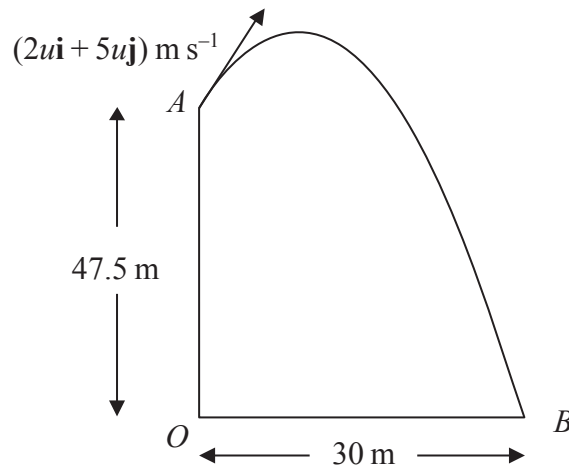


Figure 3

[In this question, the unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  are in a vertical plane,  $\mathbf{i}$  being horizontal and  $\mathbf{j}$  being vertical.]

A particle  $P$  is projected from the point  $A$  which has position vector  $47.5\mathbf{j}$  metres with respect to a fixed origin  $O$ . The velocity of projection of  $P$  is  $(2u\mathbf{i} + 5u\mathbf{j})\text{ m s}^{-1}$ . The particle moves freely under gravity passing through the point  $B$  with position vector  $30\mathbf{i}$  metres, as shown in Figure 3.

- (a) Show that the time taken for  $P$  to move from  $A$  to  $B$  is  $5\text{ s}$ . (6)
- (b) Find the value of  $u$ . (2)
- (c) Find the speed of  $P$  at  $B$ . (5)

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---

---







**Question 7 continued**

Lined writing area for the answer to Question 7 continued.

