

3.

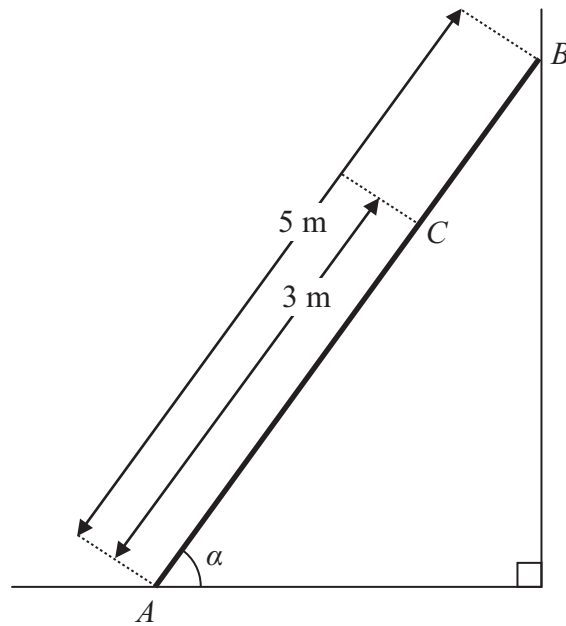


Figure 1

A ladder, of length 5 m and mass 18 kg, has one end A resting on rough horizontal ground and its other end B resting against a smooth vertical wall. The ladder lies in a vertical plane perpendicular to the wall and makes an angle α with the horizontal ground, where $\tan \alpha = \frac{4}{3}$, as shown in Figure 1. The coefficient of friction between the ladder and the ground is μ . A woman of mass 60 kg stands on the ladder at the point C , where $AC = 3$ m. The ladder is on the point of slipping. The ladder is modelled as a uniform rod and the woman as a particle.

Find the value of μ .

(9)



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Question 3 continued

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4. At time t seconds the velocity of a particle P is $[(4t - 5)\mathbf{i} + 3\mathbf{j}] \text{ m s}^{-1}$. When $t = 0$, the position vector of P is $(2\mathbf{i} + 5\mathbf{j}) \text{ m}$, relative to a fixed origin O .

(a) Find the value of t when the velocity of P is parallel to the vector \mathbf{j} . (1)

(b) Find an expression for the position vector of P at time t seconds. (4)

A second particle Q moves with constant velocity $(-2\mathbf{i} + c\mathbf{j}) \text{ m s}^{-1}$. When $t = 0$, the position vector of Q is $(1\mathbf{i} + 2\mathbf{j}) \text{ m}$. The particles P and Q collide at the point with position vector $(d\mathbf{i} + 14\mathbf{j}) \text{ m}$.

(c) Find

(i) the value of c ,

(ii) the value of d . (5)



5. The point A lies on a rough plane inclined at an angle θ to the horizontal, where $\sin \theta = \frac{24}{25}$. A particle P is projected from A , up a line of greatest slope of the plane, with speed $U \text{ m s}^{-1}$. The mass of P is 2 kg and the coefficient of friction between P and the plane is $\frac{5}{12}$. The particle comes to instantaneous rest at the point B on the plane, where $AB = 1.5 \text{ m}$. It then moves back down the plane to A .

(a) Find the work done against friction as P moves from A to B . (4)

(b) Use the work-energy principle to find the value of U . (4)

(c) Find the speed of P when it returns to A . (3)



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Question 5 continued

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Question 5 continued

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(Total 11 marks)

Q5

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P 4 1 4 8 0 A 0 1 9 2 8

6.

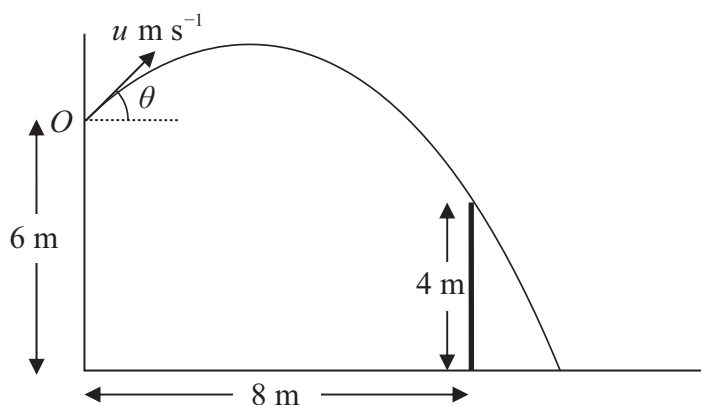


Figure 2

A ball is thrown from a point O , which is 6 m above horizontal ground. The ball is projected with speed $u \text{ m s}^{-1}$ at an angle θ above the horizontal. There is a thin vertical post which is 4 m high and 8 m horizontally away from the vertical through O , as shown in Figure 2. The ball passes just above the top of the post 2 s after projection. The ball is modelled as a particle.

(a) Show that $\tan \theta = 2.2$ (5)

(b) Find the value of u . (2)

The ball hits the ground T seconds after projection.

(c) Find the value of T . (3)

Immediately before the ball hits the ground the direction of motion of the ball makes an angle α with the horizontal.

(d) Find α . (5)



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Question 6 continued

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Question 6 continued

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(Total 15 marks)

Q6

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7. A particle A of mass m is moving with speed u on a smooth horizontal floor when it collides directly with another particle B , of mass $3m$, which is at rest on the floor. The coefficient of restitution between the particles is e . The direction of motion of A is reversed by the collision.

(a) Find, in terms of e and u ,

(i) the speed of A immediately after the collision,

(ii) the speed of B immediately after the collision.

(7)

After being struck by A the particle B collides directly with another particle C , of mass $4m$, which is at rest on the floor. The coefficient of restitution between B and C is $2e$. Given that the direction of motion of B is reversed by this collision,

(b) find the range of possible values of e ,

(6)

(c) determine whether there will be a second collision between A and B .

(3)



