

1. A particle P of mass 2 kg is moving with velocity $(\mathbf{i} - 4\mathbf{j}) \text{ m s}^{-1}$ when it receives an impulse of $(3\mathbf{i} + 6\mathbf{j}) \text{ N s}$.

Find the speed of P immediately after the impulse is applied.

(5)



4.

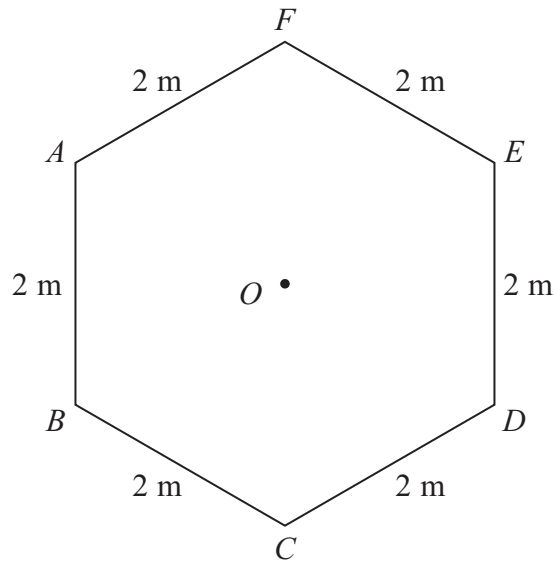


Figure 1

The uniform lamina $ABCDEF$ is a regular hexagon with centre O and sides of length 2 m, as shown in Figure 1.

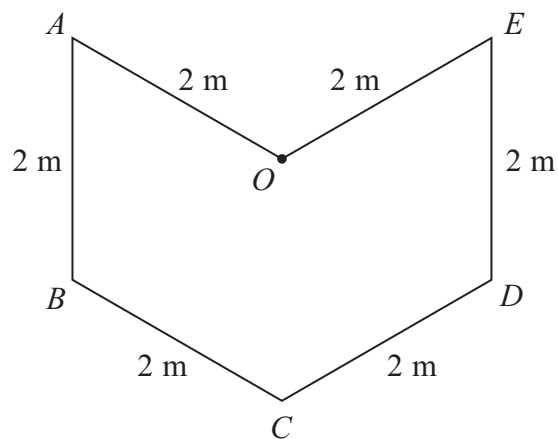


Figure 2

The triangles OAF and OEF are removed to form the uniform lamina $OABCDE$, shown in Figure 2.

(a) Find the distance of the centre of mass of $OABCDE$ from O . (5)

The lamina $OABCDE$ is freely suspended from E and hangs in equilibrium.

(b) Find the size of the angle between EO and the downward vertical. (6)



5.

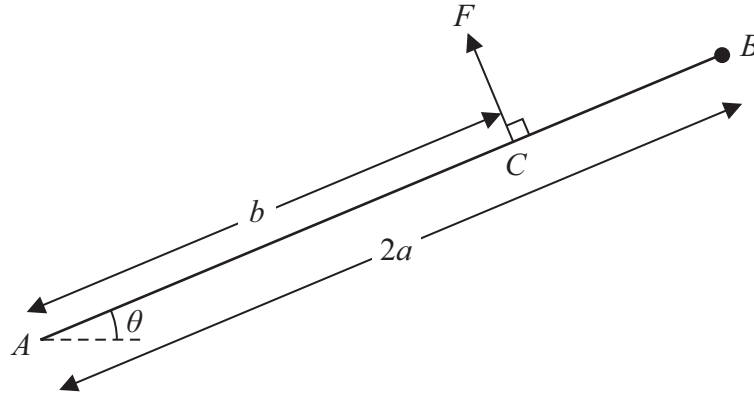


Figure 3

A uniform rod AB , of mass m and length $2a$, is freely hinged to a fixed point A . A particle of mass m is attached to the rod at B . The rod is held in equilibrium at an angle θ to the horizontal by a force of magnitude F acting at the point C on the rod, where $AC = b$, as shown in Figure 3. The force at C acts at right angles to AB and in the vertical plane containing AB .

(a) Show that $F = \frac{3amg \cos \theta}{b}$. (4)

- (b) Find, in terms of a , b , g , m and θ ,
- (i) the horizontal component of the force acting on the rod at A ,
 - (ii) the vertical component of the force acting on the rod at A .
- (5)

Given that the force acting on the rod at A acts along the rod,

(c) find the value of $\frac{a}{b}$. (4)



6.

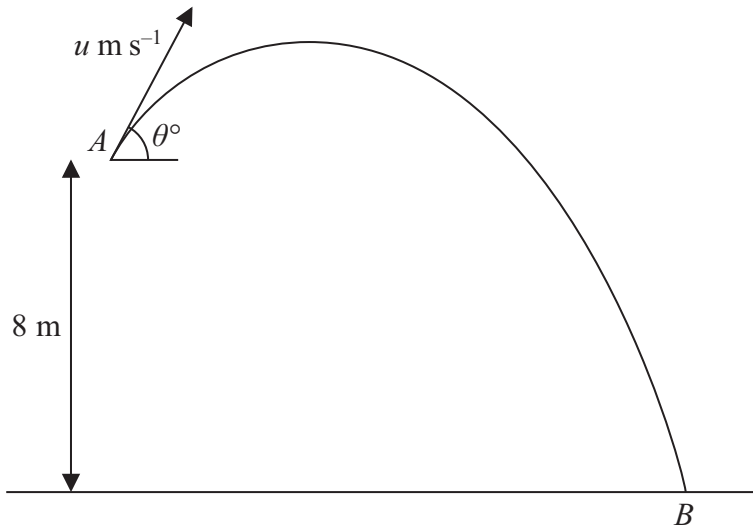


Figure 4

A ball is projected from a point A which is 8 m above horizontal ground as shown in Figure 4. The ball is projected with speed $u\text{ m s}^{-1}$ at an angle θ° above the horizontal. The ball moves freely under gravity and hits the ground at the point B . The speed of the ball immediately before it hits the ground is $2u\text{ m s}^{-1}$.

- (a) By considering energy, find the value of u . (5)

The time taken for the ball to move from A to B is 2 seconds. Find

- (b) the value of θ , (4)

- (c) the minimum speed of the ball on its path from A to B . (2)



7. Three particles P , Q and R lie at rest in a straight line on a smooth horizontal table with Q between P and R . The particles P , Q and R have masses $2m$, $3m$ and $4m$ respectively. Particle P is projected towards Q with speed u and collides directly with it. The coefficient of restitution between each pair of particles is e .

(a) Show that the speed of Q immediately after the collision with P is $\frac{2}{5}(1+e)u$. (6)

After the collision between P and Q there is a direct collision between Q and R .

Given that $e = \frac{3}{4}$, find

- (b) (i) the speed of Q after this collision,
(ii) the speed of R after this collision. (6)

Immediately after the collision between Q and R , the rate of increase of the distance between P and R is V .

- (c) Find V in terms of u . (3)



