# Mark Scheme (Results) J anuary 2007 

## GCE Mathematics

Statistics (6683)

J anuary 2007
6683 Statistics S1
Mark Scheme

| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 1. (a) | (£) 17 Just $\underline{17}$ | B1 (1) |
| (b) | $\sum t=212$ and $\sum m=61 \quad$ (Accept as totals under each column in qu.) | B1, B1 |
|  | $S_{t m}=2485-\frac{61 \times 212}{10},=1191.8 \quad$ awrt $\underline{1190}$ or 119 (3sf) | M1, A1 |
|  | $S_{t t}=983.6$ (awrt 984) and $S_{m m}=1728.9$ (awrt 1730) (or 98.4 and 173) | A1, A1 (6) |
| (c) | $r=\frac{1191.8}{\sqrt{983.6 \times 1728.9}}$ | M1, A1f.t. |
|  | $=0.913922 \ldots$ awrt $\underline{\mathbf{0 . 9 1 4}}$ | A1 (3) |
| (d) | 0.914 (Must be the same as (c) or awrt 0.914) | B1f.t. ( $\|r\|<1$ ) |
|  | e.g. linear transformation, coding does not affect coefficient (or recalculate) | dB1 (2) |
| (e) | 0.914 suggests longer spent shopping the more spent. (Idea more time, more spent |  |
|  | 0.178 different amounts spent for same time. | B1 (2) |
| (f) | e.g. might spend short time buying 1 expensive item OR might spend a long time checking for bargains, talking, buying lots of cheap items. | B1g (1) |
|  |  | 15 marks |
| (b) | M1 for one correct formula seen, f.t. their $\sum t, \sum m$ [Use $1^{\text {st }} \mathrm{A} 1$ for 1 correct, $2^{\text {nd }} \mathrm{A} 1$ for 2 etc] |  |
| (c) | M1 for attempt at correct formula, $\frac{2485}{\sqrt{2101 \times 5478}}$ scores M1A0A0 |  |
|  | A1ft f.t. their values for $S_{t t}$ etc from (b) but don't give for $S_{t t}=5478$ etc (see ab | ove) |
|  | Answer only (awrt 0.914 ) scores 3/3, 0.913 (i.e. truncation) can score M1A1ft by | mplication. |
| (d) | $2^{\text {nd }} \text { B1 dependent on } 1^{\text {st }} \text { B1 Accept } \sum m=261, \sum m^{2}=8541, \sum t m=6725 \rightarrow 0.914$ |  |
| (e) | One mark for a sensible comment relating to each coefficient |  |
|  | For 0.178 allow "little or no link between time and amount spent". Must be in context. |  |
|  | 0.178 is weak correlation ...scores B0B0. |  |
| (f) | B1g for a sensible, practical suggestion showing that other factors might affect | he amount spent. if busy) |




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| :---: | :---: | :---: |
| 4. (a) | Positive skew (both bits) | B1 (1) |
| (b) | $19.5+\frac{(60-29)}{43} \times 10,=26.7093 \ldots . \quad \text { awrt } \underline{26.7}$ | M1, A1 (2) |
| (c) | $\mu=\frac{3550}{120}=29.5833 \ldots \quad$ or $29 \frac{7}{12} \quad$ awrt $\underline{29.6}$ | B1 |
|  | $\begin{aligned} & \sigma^{2}=\frac{138020}{120}-\mu^{2} \text { or } \sigma=\sqrt{\frac{138020}{120}-\mu^{2}} \\ & \sigma=16.5829 \ldots \text { or }(s=16.652 \ldots) \end{aligned}$ <br> awrt $\underline{16.6}$ (or $s=16.7$ ) | M1 <br> A1 (3) |
| (d) | $\frac{3(29.6-26.7)}{16.6}$ | M1A1ft |
|  | $\begin{array}{ll} =0.52 \ldots & \text { awrt } \mathbf{0 . 5 2 0} \text { (or with } s \text { awrt 0.518) } \\ & \text { (N.B. } 60.5 \text { in (b) ...awrt } 0.499 \text { [or with } s \text { awrt 0.497]) } \end{array}$ | A1 (3) |
| (e) | $0.520>0$ correct statement about their (d) being $>0$ or $<0$ <br> So it is consistent with (a) ft their (d) | $\begin{aligned} & \text { B1ft } \\ & \text { dB1ft } \end{aligned}$ |
| (f) | Use Median <br> Since the data is skewed or less affected by outliers/extreme values | $\begin{align*} & \mathrm{B} 1  \tag{2}\\ & \mathrm{~dB} 1 \end{align*}$ |
| (g) | If the data are symmetrical or skewness is zero or normal/uniform distribution ("mean =median" or "no outliers" or "evenly distributed" all score B0) | $\begin{array}{\|lc} \text { B1 } & \begin{array}{c} \text { (1) } \end{array} \\ & \mathbf{1 4} \text { marks } \end{array}$ |
| (b) | M1 for $(19.5$ or 20$)+\frac{(60-29)}{43} \times 10$ or better. Allow 60.5 giving awrt 26.8 for M1A1 Allow their $0.5 n$ [or $0.5(n+1)$ ] instead of 60 [or 60.5 ] for M1. |  |
| (c) | M1 for a correct expression for $\sigma, \sigma^{2}, s$ or $s^{2}$. NB $\sigma^{2}=274.99$ and $s^{2}=277.30$ Condone poor notation if answer is awrt16.6 (or 16.7 for $s$ ) |  |
| (d) | M1 for attempt to use this formula using their values to any accuracy. Condone missing 3. $1^{\text {st }}$ A1ft for using their values to at least 3sf. Must have the 3 . <br> $2^{\text {nd }} \mathrm{A} 1$ for using accurate enough values to get awrt 0.520 (or 0.518 if using $s$ ) <br> NB Using only 3 sf gives 0.524 and scores M1A1A0 |  |
| (e) | $1^{\text {st }}$ B1 for saying or implying correct sign for their (d). B1g and B1ft. Ignore "correlation" if seen. $2^{\text {nd }} \mathrm{B} 1$ for a comment about consistency with their (d) and (a) being positive skew, ft their (d) only This is dependent on $1^{\text {st }} \mathrm{B} 1$ : so if $(\mathrm{d})>0$, they say yes, if $(\mathrm{d})<0$ they say no. |  |
| (f) | $2^{\text {nd }} \mathrm{B} 1$ is dependent upon choosing median. |  |

\begin{tabular}{|c|c|}
\hline Question number \& Scheme Marks \\
\hline \begin{tabular}{l}
5. (a) \\
(b) \\
(c) \\
(d)
\end{tabular} \& Time is a continuous variable or data is in a grouped frequency table
Area is proportional to frequency or \(A \propto f\) or \(A=k f\)
\[
3.6 \times 2=0.8 \times 9
\]
1 child represented by 0.8
(Total \(=\frac{24}{0.8},=\underline{\mathbf{3 0}}\) \begin{tabular}{ll} 
B1 \\
M1 1 \\
A1 cso
\end{tabular} \\
\hline (b)
(c)

(d) \& | $1^{\text {st }} \mathrm{B} 1$ for one of these correct statements. |
| :--- |
| "Area proportional to frequency density" or "Area $=$ frequency" is B0 |
| $1^{\text {st }} \mathrm{M} 1$ for a correct combination of any 2 of the 4 numbers: 3.6, 2, 0.8 and 9 |
| e.g. $3.6 \times 2$ or $\frac{3.6}{0.8}$ or $\frac{0.8}{2}$ etc BUT e.g. $\frac{3.6}{2}$ is M0 |
| $2^{\text {nd }}$ M1 dependent on $1^{\text {st }}$ M1 and for a correct combination of 3 numbers leading to $4^{\text {th }}$. |
| May be in separate stages but must see all 4 numbers |
| A1cso for fully correct solution. Both Ms scored, no false working seen and comment required. |
| M1 for $\frac{24}{0.8}$ seen or implied. | <br>

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| Question number | Scheme | Marks |
| :---: | :---: | :---: |
| 6. (a) | Used to simplify or represent a real world problem <br> Cheaper or quicker or easier (than the real situation) or more easily modified <br> To improve understanding of the real world problem <br> Used to predict outcomes from a real world problem (idea of predictions) <br> (3 or 4) Model used to make predictions. (Idea of predicted values based <br> (4 or 3) (Experimental) data collected | (any two lines)  <br> B1  <br> B1  <br> B1  <br> B1  <br>   <br> B1 (3) <br>  5 marks |
| (a) (b) | $1^{\text {st }} \mathrm{B} 1$ For one line <br> $2^{\text {nd }} B 1$ For a second line <br> Be generous for $1^{\text {st }} \mathrm{B} 1$ but stricter for B 1 B 1 <br> $1^{\text {st }} \& 2^{\text {nd }} \mathrm{B} 1 \quad$ These two points can be interchanged. <br> Idea of values from (experimental) data and predicted values based on the model. <br> $1^{\text {st }} \mathrm{B} 1$ for predicted values from model e.g. "model used to gain suitable data" <br> $2^{\text {nd }} \mathrm{B} 1$ for data collected. Idea of experimental data but "experiment" needn't be explicitly seen <br> $3^{\text {rd }}$ B1 This should be stage 7. Idea of refinement or revision or adjustment |  |



