

# Mark Scheme (Results) January 2007



**GCE** Mathematics

Statistics (6683)

#### January 2007 6683 Statistics S1 Mark Scheme

Question number	Scheme	Marks	
1. (a)	(£) 17 Just <u>17</u>	B1 (1)	
(b)	$\sum t = 212$ and $\sum m = 61$ (Accept as totals under each column in qu.)	B1, B1	
	$S_{tm} = 2485 - \frac{61 \times 212}{10}$ , = 1191.8 awrt <u>1190</u> or 119 (3sf)	M1, A1	
	$S_{tt} = 983.6$ (awrt 984) and $S_{mm} = 1728.9$ (awrt 1730) (or 98.4 and 173)	A1, A1 (6)	
(c)	$r = \frac{1191.8}{\sqrt{983.6 \times 1728.9}}$	M1, A1f.t.	
	= 0.913922 awrt <u>0.914</u>	A1 (3)	
(d)	0.914 (Must be the same as (c) or awrt 0.914)	B1f.t. (  <i>r</i>   <1)	
	e.g. linear transformation, coding does not affect coefficient (or recalculate)	dB1 (2)	
(e)	0.914 suggests longer spent shopping the more spent. (Idea more time, more spent	) B1	
	0.178 different amounts spent for same time.	B1 (2)	
(f)	e.g. might spend short time buying 1 expensive item <u>OR</u> might spend a long time		
	checking for bargains, talking, buying lots of cheap items.	B1g (1)	
		15 marks	
(b)	M1 for one correct formula seen, f.t. their $\sum t$ , $\sum m$ [Use 1 <sup>st</sup> A1 for 1 correct, $\sum t$ ]	2 <sup>nd</sup> A1 for 2 etc]	
(c)	M1 for attempt at correct formula, $\frac{2485}{\sqrt{2101 \times 5478}}$ scores M1A0A0		
	A1ft f.t. their values for $S_{tt}$ etc from (b) but don't give for $S_{tt} = 5478$ etc (see all	oove)	
	Answer only (awrt 0.914) scores 3/3, 0.913 (i.e. truncation) can score M1A1ft by implication.		
(d)	2 <sup>nd</sup> B1 dependent on 1 <sup>st</sup> B1 Accept $\sum m = 261, \sum m^2 = 8541, \sum tm = 6725 \rightarrow 0.914$		
(e)	One mark for a sensible comment relating to each coefficient		
	For 0.178 allow "little or no link between time and amount spent". Must b	e in context.	
	Just saying 0.914 is strong +ve correlation between amount spent and time	shopping and	
	0.178 is weak correlation scores B0B0.		
(f)	B1g for a sensible, practical suggestion showing that other factors might affect	the amount spent.	
	E.g. different day (weekend vs weekday) or time of day (time spent queuin	g if busy)	

Question number	Scheme	Marks	
2. (a)	0.03  D  (0.0105) Correct tree shape	M1	
	0.35 $\overline{D}$ A, B and C and 0.35 and 0.25 0.06 D (0.015)	A1	
	0.25 B $D(x3)$ and 0.03, 0.06, 0.05	A1 (3)	
	$\overline{D}$ (May be implied by seeing		
	0.05 $D$ (0.02) $P(A \cap D)$ etc at the ends)		
	$\sim_{C}$		
	$\overline{D}$		
(b)(i)	$P(A \cap D) = 0.35 \times 0.03$ , $= 0.0105 \text{ or } \frac{21}{2000}$	M1, A1	
	P(C) = 0.4 (anywhere)	B1	
(ii)	$P(D) = (i) + 0.25x \ 0.06 + (0.4x \ 0.05)$	M1	
	$=$ <b><u>0.0455</u></b> or $\frac{91}{2000}$	A1 (5)	
(c)	$P(C D) = \frac{P(C \cap D)}{P(D)}, = \frac{0.4 \times 0.05}{(ii)}$	M1, A1ft	
	= 0.43956 or $\frac{40}{91}$ <u>0.44</u> or awrt <u>0.440</u>	A1 (3)	
	[Correct answers only score full marks in each part]	11 marks	
(a)	M1 for tree diagram, 3 branches and then two from each. At least one probabili	ity attempted.	
(b)	1 <sup>st</sup> M1 for 0.35x0.03. Allow for equivalent from <u>their tree diagram.</u>		
	B1 for $P(C) = 0.4$ , can be in correct place on tree diagram or implied by $0.4 \times 0.6$		
	$2^{nd}$ M1 for all 3 cases attempted and <u>some</u> correct probabilities seen, including +. C		
	Condone poor use of notation if correct calculations seen. E.g. $P(C   D)$ for		
(c)	M1 for attempting correct ratio of probabilities. There must be an attempt to su		
	values in a correct formula. If no correct formula and ration not correct ft so	core M0.	
	Writing $P(D C)$ and attempting to find this is M0.		
	Writing $P(D C)$ but calculating correct ratio – ignore notation and mark ratios.		
	<ul><li>A1ft must have their 0.4 x0.05 divided by their (ii).</li><li>If ratio is incorrect ft (0/3) unless correct formula seen and part of ratio is correct then M1.</li></ul>		
	In ratio is medirect it (0, 5) unless correct formula seen and part of failo is co		

Question number	Scheme	Marks	
3. (a)	N.B. Part (a) doesn't have to be in a table, could be a list $P(X = 1) = \dots$ etc	B1, B1, B1	
	x 1 2 3 4 5 6		
	$P(X = x)  \frac{1}{36}  \frac{3}{36}  \frac{5}{36}  \frac{7}{36}  \frac{9}{36}  \frac{11}{36}$		
	0.0278, 0.0833, 0.139, 0.194, 0.25, 0.306 (Accept awrt 3 s.f)	(3)	
(b)	$P(3) + P(4) + P(5) =, \frac{21}{36} \text{ or } \frac{7}{12}$ or awrt 0.583	M1, A1 (2)	
(c)	$E(X) = \frac{1}{36} + 2 \times \frac{3}{36} + \dots, = \frac{161}{36} \text{ or } 4.472 \text{ or } 4\frac{17}{36}$	M1, A1 (2)	
(d)	$E(X^{2}) = \frac{1}{36} + 2^{2} \times \frac{3}{36} + \dots, = \frac{791}{36} \text{ or full expression or } 21\frac{35}{36} \text{ or awrt } 21.97$	M1, A1	
	$\operatorname{Var}(X) = \frac{791}{36} - \left(\frac{161}{36}\right)^2$ , $= \underline{1.9714*}$	M1, A1c.s.o. (4)	
(e)	$Var(2-3X) = 9 \times 1.97$ or $(-3)^2 \times 1.97$ , = 17.73 awrt <u>17.7</u> or $\frac{2555}{144}$	M1, A1 (2) <b>13 marks</b>	
(a)	$1^{\text{st}}$ R1 for $r = 1$ 6 and at least one correct probability NR $3 = 1$ and $9 = 1$	•	
(a)	1 <sup>st</sup> B1 for $x = 1,, 6$ and at least one correct probability N.B. $\frac{3}{36} = \frac{1}{12}$ and $\frac{9}{36} = \frac{1}{4}$		
	2 <sup>nd</sup> B1 for at least 3 correct probabilities 3 <sup>rd</sup> B1 for a fully correct probability distribution.		
(b)	M1 for attempt to add the correct three probabilities, ft their probability distrib	ution	
(c)	M1 for a correct attempt at $E(X)$ . Minimum is as printed. Exact answer only s		
	[Division by 6 at any point scores M0, no ISW. Non-exact answers with no work	ing score M0.]	
(d)	1 <sup>st</sup> M1 for a correct attempt at E(X <sup>2</sup> ). Minimum as printed. $\frac{791}{36}$ or awrt 21.97 so	cores M1A1.	
	$2^{nd}$ M1 for their E(X <sup>2</sup> ) - (their E(X)) <sup>2</sup> .		
	$2^{\text{nd}}$ A1 cso needs awrt 1.97 and $\frac{791}{36} - \left(\frac{161}{36}\right)^2$ or $\frac{2555}{1296}$ or any fully correct expression	ssion seen.	
	Can accept <u>at least 4 sf</u> for both. i.e. 21.97 for $\frac{791}{36}$ , 4.472 for $\frac{161}{36}$ , 20.00 for $\left(\frac{1}{36}\right)$	$\left(\frac{61}{66}\right)^2$ .	
(e)	M1 for correct use of $Var(aX + b)$ formula or a <u>full</u> method.		
	NB $-3^2 \times 1.97$ followed by awrt 17.7 scores M1A1 <u>BUT</u> $-3^2 \times 1.97$ alone, or the state of t	followed by	
	– 17.7, scores M0A0.		

Question number	Scheme	Marks	
4. (a)	Positive skew (both bits)	B1 (1	l)
(b)	$19.5 + \frac{(60-29)}{43} \times 10, = 26.7093$ awrt <u>26.7</u>	M1, A1 (2	2)
	(N.B. Use of 60.5 gives 26.825 so allow awrt 26.8)		
(c)	$\mu = \frac{3550}{120} = 29.5833$ or $29\frac{7}{12}$ awrt <b>29.6</b>	B1	
	$\sigma^2 = \frac{138020}{120} - \mu^2$ or $\sigma = \sqrt{\frac{138020}{120} - \mu^2}$	M1	
	$\sigma = 16.5829$ or (s = 16.652) awrt <u>16.6</u> (or s = 16.7)	A1 (3)	)
(d)	$\frac{3(29.6 - 26.7)}{16.6}$	M1A1ft	
	= 0.52	A1 (3	)
(e)	0.520 > 0correct statement about their (d) being >0 or < 0	B1ft dB1ft (2	2)
(f)	Use <u>Median</u> Since the data is skewed <u>or</u> less affected by outliers/extreme values	B1 dB1 (2	2)
(g)	If the data are <u>symmetrical</u> or <u>skewness is zero</u> or <u>normal/uniform distribution</u> ("mean =median" or "no outliers" or "evenly distributed" all score B0)	B1 ( 14 mar	1) r <b>ks</b>
(b)	M1 for (19.5 or 20) + $\frac{(60-29)}{43}$ ×10 or better. Allow 60.5 giving awrt 26.8 for	M1A1	
	Allow their $0.5n$ [or $0.5(n+1)$ ] instead of 60 [or 60.5] for M1.		
(c)	M1 for a correct expression for $\sigma$ , $\sigma^2$ , $s$ or $s^2$ . NB $\sigma^2 = 274.99$ and $s^2 = 277.30$ Condone poor notation if answer is awrt16.6 (or 16.7 for $s$ )	)	
(d)	M1 for attempt to use this formula using their values to any accuracy. Condone $1^{st}$ A1ft for using their values to at least 3sf. Must have the 3. $2^{nd}$ A1 for using accurate enough values to get awrt 0.520 (or 0.518 if using <i>s</i> ) NB Using only 3 sf gives 0.524 and scores M1A1A0	e missing 3.	
(e)	<ul> <li>1<sup>st</sup> B1 for saying or implying correct sign for their (d). B1g and B1ft. Ignore "correlation" if seen.</li> <li>2<sup>nd</sup> B1 for a comment about consistency with their (d) and (a) being positive skew, ft their (d) only This is dependent on 1<sup>st</sup> B1: so if (d)&gt;0, they say yes, if (d)&lt;0 they say no.</li> </ul>		
(f)	2 <sup>nd</sup> B1 is dependent upon choosing median.		

Question number	Scheme	Mark	<s< th=""></s<>
5. (a)	Time is a <u>continuous</u> variable <u>or</u> data is in a <u>grouped</u> frequency table	B1	(1)
(b)	Area is proportional to frequency or $A \propto f$ or $A = kf$	B1	(1)
(c)	$3.6 \times 2 = 0.8 \times 9$	M1 dM1	
	1 child represented by 0.8	A1 cso	(3)
(d)	$(\text{Total}) = \frac{24}{0.8}, = \underline{30}$	M1, A1	(2)
		7 m	arks
(b)	<ul> <li>1<sup>st</sup> B1 for one of these correct statements.</li> <li>"Area proportional to frequency density" or "Area = frequency" is B0</li> </ul>		
(c)	1 <sup>st</sup> M1 for a correct combination of any 2 of the 4 numbers: 3.6, 2, 0.8 and 9 e.g. $3.6 \times 2$ or $\frac{3.6}{0.8}$ or $\frac{0.8}{2}$ etc BUT e.g. $\frac{3.6}{2}$ is M0		
	2 <sup>nd</sup> M1 dependent on 1 <sup>st</sup> M1 and for a correct combination of 3 numbers leading to	$o 4^{th}$ .	
	May be in separate stages but must see all 4 numbers		
	A1cso for fully correct solution. Both Ms scored, no false working seen and <u>com</u>	ment require	<u>ed.</u>
(d)	M1 for $\frac{24}{0.8}$ seen or implied.		

Question number	Scheme		Marks	
6. (a)	To improve understanding of the real world problem		(any two lines) B1 B1 (2)	
(b)	(3 or 4)	Model used to make predictions. (Idea of predicted values based on the model)	B1	
	(4 or 3)	(Experimental) data collected	B1	
	(7)	Model is refined.	B1 (3) <b>5 marks</b>	
(a)	1 <sup>st</sup> B1 For on	ne line		
~ /	$2^{nd}$ B1 For a s			
		nerous for 1 <sup>st</sup> B1 but stricter for B1B1		
(b)	1 <sup>st</sup> & 2 <sup>nd</sup> B1	These two points can be interchanged. Idea of values from (experimental) data and predicted values based	on the model.	
	1 <sup>st</sup> B1 for pre	edicted values from model e.g. "model used to gain suitable data"		
	$2^{nd}$ B1 for data collected. Idea of experimental data but "experiment" needn't be explicitly			
	3 <sup>rd</sup> B1	This should be stage 7. Idea of refinement or revision or adjustmen	ıt	

Question number	Scheme	Marks	
7. (a)	$P(X < 91) = P(Z < \frac{91 - 100}{15})$ Attempt standardisation	M1	
	= P(Z < -0.6)	A1	
	= 1 - 0.7257	M1	
	= 0.2743 awrt <u>0.274</u>	A1 (4)	
(b)	1 - 0.2090 = 0.7910 0.791	B1	
	P(X > 100+k) = 0.2090 or $P(X < 100+k) = 0.7910$ (May be implied)	M1	
	Use of tables to get $z = 0.81$	B1	
	$\frac{100 + k - 100}{15}$ ,=0.81 (ft their z = 0.81, but must be z not prob.)	M1, A1ft	
	<u><math>k = 12</math></u>	A1 cao (6)	
		10 marks	
(a)	1 <sup>st</sup> M1 for attempting standardisation. $\pm \frac{(91 - \mu)}{\sigma \text{ or } \sigma^2}$ . Can use of 109 instead of 91. Use of 90.5 etc is M 1 <sup>st</sup> A1 for -0.6 (or +0.6 if using 109)		
	$2^{nd}$ M1 for 1 – probability from tables. Probability should be > 0.5)		
(b)	1 <sup>st</sup> B1 for 0.791 seen or implied.		
	$1^{\text{st}}$ M1 for a correct probability statement, but must use X or Z correctly. Shown of		
	$2^{nd}$ B1 for awrt 0.81 seen (or implied by correct answer - see below) (Calculator gives 0.80989 $2^{nd}$ M1 for attempting to standardise e.g. $\frac{100 + k - 100}{15}$ or $\frac{k}{15}$		
	$\frac{X-100}{15}$ scores 2 <sup>nd</sup> M0 until the 100+ k is substituted to give k, but may imply 1 <sup>st</sup> M	1 if <i>k</i> = 112.15 seen	
	1 <sup>st</sup> A1ft for correct equation for k (as written or better). Can be implied by $k = 12$	2.15 (or better)	
	$2^{nd}$ A1 for $k = 12$ only.		
	Answers only		
	k = 112 or 112.15 or better scores 3/6 (on EPEN give first 3 marks)		
	k = 12.15 or better (calculator gives $12.148438$ ) scores 5/6 (i.e loses last	A1 only)	
	k = 12 (no incorrect working seen) scores 6/6		
NB	Using 0.7910 instead of 0.81 gives 11.865 which might be rounded to 12. This sh	nould score no	
	more than B1M1B0M1A0A0.		