



Mark Scheme (Results)

January 2019

Pearson Edexcel International Advanced Level In Statistics S1 (WST01/01)

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

PEARSON EDEXCEL IAL MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- M marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

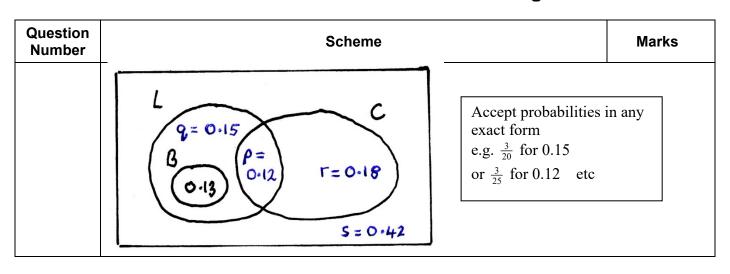
- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper or ag- answer given
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

5.	For misreading which does not alter the character of a question or materially simplify it, deduct two
	from any A or B marks gained, in that part of the question affected.

6. Ignore wrong working or incorrect statements following a correct answer.

January 2019 WST01 STATISTICS 1 Mark Scheme

Question Number	Scheme	Marks
1.(a)	B and C or "band" and "choir" but NOT $P(B)$ and $P(C)$	B1 (1)
(b)	[L and C independent implies] $P(L \cap C) = P(L) \times P(C) = 0.4 \times 0.3$ $p = \underline{0.12}$	M1 A1
(c)	$q = 0.4 - 0.13 - \text{their } p = \underline{0.15}$ $r = 0.3 - \text{their } p = \underline{0.18}$ $s = 1 - (0.4 + 0.3 - \text{their } p) \text{ or } 1 - (0.4 + \text{their } r) = \underline{0.42}$	(2) B1ft B1ft B1ft
(d)	$P(L \mid B \cup C) \text{ or } \frac{P(L \cap [B \cup C])}{P(B \cup C)} = ; \frac{0.13 + "0.12"}{0.13 + 0.3}$	(3) M1; A1ft
	$=\frac{25}{43}$	(3) [9 marks]
	Notes	
(a)	B1 for B and C indicated. Allow other non-trivial pairs e.g. B and $L \cap C$ bu	t not L and L'
(b)	Correct answers only to parts (b), (c) or (d) score all the relevant marks.	
(c)	1^{st} B1ft for 0.15 or a correct q allowing ft of their p 2^{nd} B1ft for 0.18 or a correct r allowing ft of their p 3^{rd} B1ft for 0.42 or a correct s allowing ft of their p or r (Labelled or on V	orobabilities.
(d)	1 st A1ft for a correct (or correct ft) probability ratio (num < denom)	
	2^{nd} A1 for $\frac{25}{43}$ or exact equivalent NB completed Venn diagram. (If answers conflict the script takes preference	over diagram)



Question Number	Scheme	Marks
2.(a)	$[E(X) =] (-2 \times 0.15) + (-1 \times a) + 0 + (1 \times a) + (3 \times 0.4) \text{ or } -0.3 - a + a + 1.2$	M1
	= 0.9	A1
		(2)
(b)	$ [E(X^2) =] \{ (-2)^2 \times 0.15 \} + \{ (-1)^2 \times a \} + \{ 1^2 \times a \} + \{ 3^2 \times 0.4 \} $	M1
(0)	or $0.6 + 2a + 3.6$	1011
	So $4.2 + 2a = 4.54$	dM1
	a = 0.17	A1
	Use of sum of probabilities = 1 e.g. $0.15 + 0.34 + 0.4 + b = 1$	M1
	b = 0.11	A1 (5)
(-)	$[V_{2}, V_{3}] = [1, 4, 5, 4, (4), -1, 0, 0)^{2} = [-2, 7, 2]$	(5)
(c)	$[Var(X) =] 4.54 - (their 0.9)^2 = 3.73]$	M1
	$Var(Y) = (-2)^2 Var(X)$	M1
	= 14.92 (accept 14.9)	A1
		(3)
	Notes	[10 marks]
	Correct answers with no working can score all the relevant ma	rks
(a)	M1 for an attempt at $E(X)$ i.e. at least 3 non-zero correct products seen	ii Ko.
	A1 for 0.9 or any exact equivalent	
(b)		
	2^{nd} dM1 dependent on 1^{st} M1 for using their E(X^2) and 4.54 to form a linear e	equation in a
	1st A1 for $a = 0.17$ or exact equivalent	1 . [0.1])
	3^{rd} M1 for use of sum of probabilities = 1 to form a linear equation for b (ft to	$neir \ a \in [0,1])$
	or for the equation $0.15 + 2a + b + 0.4 = 1$ or $2a + b = 0.45$	
	2^{nd} A1 for $b = 0.11$ or exact equivalent	
(c)	(c) 1^{st} M1 for a correct expression for $Var(X)$ (ft their 0.9 for $E(X)$)	
	Allow expression based on working out $E(X^2)$ and ft their $E(X)$, their $a \in [0,1]$, their $b \in [0,1]$
	2^{nd} M1 for $(-2)^2 \times (\text{their Var}(X))$ condone e.g. $-2^2 \text{Var}(X)$ if it later becomes	
	This can be awarded for the formula with $Var(X)$ not necessarily a valid If they state $Var(X) = E(X^2)$ or 4.54 then M0M1 is possible.	aiue.
	A1 for 14.92 (accept 14.9)	
	(w	
ALT	Dist of Y	-3
ALI	P(Y=y) 0.15 a b a	0.4
	1 st M1 for $E(Y) = 6$ "a" + 3 "b" - 0.15 or 1.2 and $E(Y^2) = 26$ "a" + 9 "b" +	10.95 <u>or</u> 16.36
	2^{nd} M1 for $\text{Var}(Y) = \text{``16.36''} - [\text{``1.2''}]^2$ allow ft of their $\text{E}(Y) \neq \text{their (a)}$ and I	
		but $E(Y^2) > 0$

Question Number	Scheme	Marks
3. (a)	$[W \sim N(64, 8^2)] P(W < 51) = P\left(Z < \frac{51 - 64}{8}\right) \text{ or } P(Z < -1.625)$ $= 1 - 0.9484 \text{(calc. } 1 - 0.9479187299)}$ $= \text{awrt } \underline{0.052}$	M1 M1 A1
(b)	Require: $P(W > 49 \mid W < 51)$ $= \frac{P(49 < W < 51)}{P(W < 51)} \text{or} \frac{P(-1.875 < Z < -1.625)}{P(Z < -1.625)}$ $= \frac{0.021684}{(a)}$	(3) M1 M1 A1ft
	= 0.4163 awrt <u>0.42</u>	A1 (4)
(c)	$[P(W > H) = 0.10 \Rightarrow] \frac{H - 64}{8} = 1.2816$ $H = 74.2528 \text{ awrt } \frac{74.3}{8}$	M1B1 A1 (3)
	Notes	[10 marks]
(a)	2 nd M1 for 1 – p where 0.9 st M1 for a correctly stated conditional probability. May be implied by correct ratio. 2 nd M1 for a correct ratio of probabilities in their W or Z (either version from scheme) (a) -P(W < 49) (a) or 1 - P(W < 49) (a) will score M1M1 1 st A1ft for a correct ratio of probabilities with their (a) on denominator and numerator in the range [0.0215, 0.0219]. Num > Denom is A0 2 nd A1 for a final answer of awrt 0.42 (dep on at least one other mark) Final answer of 5/12 will lose the final A1 unless awrt 0.42 is seen as well	
(b)		
Ans only		
(c)	M1 for standardising with H , 64 and 8 and setting equal to a z value where B1 for using $z = \pm 1.2816$ (or better e.g. calc: 1.2815515) can be with 8^2	instead of 8 etc
NB z = 1.28 Ans only Ans only	for awrt 74.3 (calc gives 74.25241253) award M1B0A1 for an answer of 74.24 or awrt 74.2 if B0 scored for $z = 1.28$ for an answer only of awrt 74.3 (can come from $z = 1.282$ etc) award M1B0A1	

Question Number	Scheme	Marks
4.(a)	Width: 15 minutes is 0.5 cm so 60 mins will be $4 \times 0.5 = 2$ (cm)	B1
	Height: freq of 25 represented by $6 \times 0.5 = 3$ (cm ²) so freq of 24 is $\frac{24}{25} \times 3$	M1
	So height = $\frac{1}{"2"} \times \frac{24}{25} \times 3 = \underline{1.44}$ (cm)	A1
		(3)
(b)	$[Q_2 =] \{30\} + \frac{(50 - [25 + 17])}{28} \times 30$ or e.g. $\frac{60 - 30}{70 - 42} = \frac{m - \{30\}}{50 - 42}$	M1
	= 38.571 awrt <u>38.6</u>	A1 (2)
(c)	Use of midpoints to get $\sum fx = 5070$ (allow 5000 to 1 sf)	M1
	$\begin{bmatrix} \overline{t} & \text{or } \overline{x} \end{bmatrix} = \underline{50.7}$	A1
	455 510 5	(2)
(d)	$[\sigma] = \sqrt{\frac{455512.5}{100}} - "50.7"^2 \text{or} \sqrt{1984.635}$	M1
	= 44.5492 awrt <u>44.5</u>	A1
(e)	\overline{t} or $\overline{x} > Q_2$ [allow "50.7" > "38.6" or formula] so <u>positive</u> (skew)	B1 (2)
,		(1)
(f)(i)	Median: no change Since e.g. all 18 values or all changes are still below the median	B2/1/0
(ii)	Mean: will be smaller	B2/1/0
(iii)	Since e.g. changes will reduce total of x (7×7.5 not 25×7.5 in 1 st class) Standard deviation: will be greater	B1
	Since e.g. (18 zeros means) data more spread out	(3) [13 marks]
	Notes	[10 marks]
(a)		
(b)	M1 for $+\frac{8}{28} \times 30$ (o.e.) May work down e.g. $\{60\} - \frac{20}{28} \times 30$ or if using $(n+1)$	_ = =
	A1 for awrt 38.6 (accept $\frac{270}{7}$) or (if using $(n + 1)$ for 39.107 or awrt 39.1)	
(c)	M1 for $\sum fx = 5000$ (to 1 sf) or a fully correct expression using midpoints	
	A1 for 50.7 or exact equivalent e.g. $\frac{5070}{100}$	
(d)	M1 for a correct expression including square root (ft their mean) A1 for awrt 44.5 (or 44.55) (allow use of $s = 44.77367$ or awrt 44.8)	
(e)	B1 for positive skew <u>plus</u> a suitable correct reason [allow use of values provided Allow correct use of quartiles but must see $Q_1 = 15$ and $Q_3 = 72.5$	ded(c) > (b)]
(f)(i)~(iii)	B2 for all 3 correct statements B1 for only 2 correct statements (B1B0) 3^{rd} B1 dep on B2 for at least one suitable reason. (Allow calculation of \overline{x} or Do not accept comments like "median not affected by extreme values"	,
NB	With 18 zeros $\Sigma fx = 4935$, $\overline{x} = 49.35$, $\Sigma fx^2 = 454500$, $\sigma = 45.930$, $s = 46.161$	• • • • • • • • • • • • • • • • • • • •

Question Number	Scheme	Marks
5.(a)	$\left[\overline{x} = \frac{96}{80} = \right] \underline{1.2}$	B1
(b)	$P(S=2) = 3 \times 0.4^2 \times 0.6$ = <u>0.288</u>	(1) M1 A1
(c)	$P(S = 0) = 1 - (0.496 + "0.288")$ or $0.6^3 = 0.216$	B1ft (1)
(d)(i)	$p_1 = 0.25$ and $p_2 = 0.4$ and $p_3 = 0.55$	M1
(ii)	$P(T=3) = p_1 \times p_2 \times p_3 = 0.25 \times 0.4 \times 0.55 = \underline{0.055 \text{ (*)}}$ $P(T=1) = \underline{0.25} \times 0.6 \times 0.45 + 0.75 \times \underline{0.4} \times 0.45 + 0.75 \times 0.6 \times \underline{0.55}$ $\underline{\text{or}} = 0.0675 + 0.135 + 0.2475$	A1cso M1A1
	= <u>0.45 (*)</u>	A1 cso (5)
(e)	$P(T=0) = 0.75 \times 0.6 \times 0.45 $ (or equivalent expression for $P(T=2)$) $= \underline{0.2025} $ (Allow $\frac{81}{400}$)	M1 A1
	$P(T=2) = 1 - (0.505 + "0.2025") = 0.2925$ (Allow $\frac{117}{400}$)	A1ft (3)
(f)	Estimate probs from the data: (or frequencies for S and T)	M1
	Ting's model is always closer	A1 A1
	So choose Ting's model $S(f)$ 17.28 34.56 23.04 5.12 $T(f)$ 16.2 36 23.4 4.4	$\begin{bmatrix} A1 \\ (3) \\ [15 marks] \end{bmatrix}$
	Notes	
(a)	B1 for 1.2 or any exact equivalent Mark (b) and (c) together (M1 is for a full method for P(S = 2)	
(b)	M1 for $k \times 0.4^2 \times 0.6$ (including $k = 1$) where $k \in \mathbb{Z}^+$ or $3 \times p^2 \times (1 - p)$ for so	$\operatorname{me} p \in (0, 1)$
	A1 for 0.288 or an exact equivalent e.g. $\frac{36}{125}$	
(c)	Correct answers in table can score all marks in (b) and (c). Table takes B1ft for $P(S=0)$ based on sum of probabilities = 1 i.e. $0.216 \text{ or } 1 - (0.496 + \text{their})$	
(d)	2 nd A1 for at least 2 correct products seen	(T = 3) Beware: $(1 - p_3) = 0.45$ is $2^{\text{nd}} M0$
(e)	M1 for a correct product for $P(T=0)$ or all 3 correct products for $P(T=2)$ 1st A1 for either correct probability (correctly labelled or placed in the table 2nd A1ft for a correct 4th probability or a 4th probability that makes the sum =	(ft their p_i)
(f)	M1 for attempt at calculating probs from the data <u>or</u> freqs $S(f)$ and $T(f)$ (at 1^{st} A1 for all figs correct(2sf) and comparison of probs (or frequencies) for the 2^{nd} A1 for clearly choosing Ting's model (dependent on M1A1 scored) e.g. "Ting's is best because probabilities (or frequencies) are always closer" sc	ne 2 models
SC (A0A0)	B1 choose Ting because probabilities (of frequencies) are always closer see	

Question Number	Scheme	Marks
6.(a)	Mean, median, average, marks, results score: on P2 (y) is lower than P1 (x) o.e. Spread, dispersion, range, st. dev, var(iance): on P2 is more than P1 o.e	B1 B1 (2)
(b)(i) (ii)	e.g. (38, 0) doesn't follow the pattern/trend <u>or</u> out of range of other points <u>or</u> far from (best fit) line / other points (o.e.) The student was absent when paper 2 was taken (o.e.)	B1 B1
(c)	New $\overline{x} = \frac{35.75 \times 16 - 38}{15}$ or $\frac{534}{15}$, $= 35.6$ New $\overline{y} = \frac{25.75 \times 16}{15} = 27.46$ awrt $\frac{27.5}{15}$ (allow $\frac{412}{15}$)	(2) M1, A1 B1
	New $\sum xy = 15837 - 38 \times 0$ so no change	(3) B1
(ii)	$S_{xy} = 15837 - \frac{(35.75 \times 16 - 38) \times (25.75 \times 16)}{15} \underline{\text{or}} -\frac{"534" \times "412"}{15} \underline{\text{or}} -\frac{220008}{15} \\ = \underline{1169.8} \ (*)$	M1 A1cso (3)
(e)	$r = \frac{1169.8}{\sqrt{965.6 \times 1561.7}}$, = 0.9526079 awrt 0.953	M1, A1 (2)
(f)	$b = \frac{1169.8}{965.6}$ [= 1.21147], $a = "27.5" - "b" \times "35.6"$ [= -15.6618] y = -15.6/7 + 1.2x $b = awrt$ 1.2, $a = awrt$ -15.6 or -15.7	M1, M1 A1, A1
(g)	(Value of r increased from 0.746 to 0.953) so points lie closer to a st. line	(4) B1 (1)
(h)	$y = "1.21" \times 38 - "15.66"$ or awrt <u>30</u>	B1ft (1) [18 marks]
	Notes	[To marks]
(a)	for a correct comment on 1 st B1: mean etc 2 nd B1: spread etc, one of these 5 te	rms seen
(b)	1 st B1 for a suitable explanation (saying an "extreme point" is B0) 2 nd B1 for a suitable comment e.g. teacher didn't mark it, wrongly recorded/plotted (o.e.)	
(c)		
(d)(i) (ii)		
(e)	M1 for a correct method (implied by ans = awrt 0.95) A1 for awrt 0.953	
(f)	1^{st} M1 for a correct expression for b 2^{nd} M1 for a correct expr' seen for a (ft means in (c)) 1^{st} A1 for b = awrt 1.2 2^{nd} A1 for a = awrt -15.6 or -15.7 a and b must be in an x , y eq'n	
(g)	B1 for a suitable comment e.g. <u>linear</u> relationship <u>stronger</u> or <u>stronger linear</u> co	orrelation
(h)	B1ft for awrt 30 or ft expression using $x = 38$ in their equation (need not be eval	uated)

