

# Mark Scheme (Results)

# Summer 2014

Pearson Edexcel International A Level in Statistics 1 (WST01/01)

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### General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

### EDEXCEL IAL MATHEMATICS

#### **General Instructions for Marking**

- 1. The total number of marks for the paper is 75.
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.
- 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol  $\sqrt{}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- dep dependent
- indep independent
- dp decimal places
- sf significant figures
- **\*** The answer is printed on the paper
- The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. Ignore wrong working or incorrect statements following a correct answer.

5602				
$S_{yy} = 39418 - \frac{560^2}{8}$	M1			
$= \underline{218}$	Alcao	(2)		
$r = \frac{-710}{\sqrt{218} \times 2587.5}$	M1			
= -0.945344 <u>awrt</u> $-0.945$	A1	(2)		
As age increases, volume/blood (pumped) decreases (o.e.)	B1	(1)		
	B1ft			
For ft, if $-0.5 \le r \le 0.5$ "No since r is close to 0"	DIR	(1)		
-710 (allow $-284$ ) and $-710$				
$b = \frac{1}{2587.5} = -0.27439  (anow \frac{1}{1035}) \qquad awn = 0.27$	MIAI			
$a = \frac{360}{8}$ - 'their b'× $\frac{370}{8}$ [= 82.690] so $\underline{y = 82.7 - 0.274x}$	M1, A1			
$v = 82.7 - 0.274 \times 40 = 0.71.74 = awrt 72$	B1	(4)		
Should be reliable since interpolation (o.e.) $\frac{1}{2}$	B1			
	[12]	(2)		
Notes				
M1 for a correct expression for $S_{yy}$ A1 for 218 (condone 218.0)				
M1 for attempt at correct formula with their $S_{yy}$ (>0) and given $S_{xx}$ , $S_{yy}$ in the correct places				
Condone missing "-" for M1 $-0.95$ with no expression seen scores M1A0, awrt - 0.945 with no working scores M1A1				
B1 Must mention "age" and "volume" or "blood (pumped)" No ft.				
	) <u>correlation</u>	<u>on</u>		
'points lie close to a line' is B0 since there is no evidence of this.				
for a correct expression for b. Condone missing "-" st A1 for awrt $-0.27$ or allow exact fraction				
$M^{nd}$ M1 for a correct method for <i>a</i> . Follow through their value of <i>b</i>				
for a correct equation for y and x with $a = awrt 82.7$ and $b = awrt -0.274$	No fracti	ons		
$^{st}$ B1 for awrt 72	/ 1	1		
NB "it is reliable since it is in the range" is B0 since "it" is not explicit enough				
	ice <u>irre</u> leva	. <u>nt</u>		
	$= 218$ $r = \int \frac{-710}{\sqrt{218} \times 2587.5} = -0.945344$ awrt	$= 218$ A leao $r = \int \frac{-710}{\sqrt{n^{2}}18^{n} \times 2587.5} = -0.945344$ awrt0.945 A l M A A A A A A A A A A A A A A A A A A		

Question	Scheme	Marl	<b>KS</b>	
2. (a)	Width = $\frac{5}{3} \times 1.5 = 2.5$ (cm)	B1		
	Area = $6 \times 1.5 = 9$ cm <sup>2</sup> has frequency = 12 so 1.5 cm <sup>2</sup> = 2 people (o.e.)	M1		
	Frequency of 10 corresponds to area of 7.5 so height = $3$ (cm)	A1	(3)	
(b)	$Q_{2} = [2.5+] \frac{(25/25.5-16)}{12} \times 3 = 4.75  (\text{or } 4.875 \text{ if use } n+1) \qquad \text{awrt } \underline{4.75}$ $[\overline{x} =] \frac{394}{50} = 7.88  (*)$ $[\sigma_{x} =] \sqrt{\frac{6500}{50} - \overline{x}^{2}} = \sqrt{67.9056}$	M1 A1	(2)	
(c)(i)	$\left[\overline{x} = \right] \frac{394}{50} = 7.88$ (*)	B1cso	(2)	
(ii)	$\left[\sigma_{x}=\right]\sqrt{\frac{6500}{50}-\overline{x}^{2}} = \sqrt{67.9056}$	M1A1		
	$= \underline{awrt \ 8.24}  (Accept \ s = awrt \ 8.32)$	A1	(4)	
	- 0	DIG		
(d)	$\overline{x} > Q_2$	B1ft	$(\mathbf{n})$	
	So <u>positive</u> (skew)	dB1	(2)	
(e) (i)	There is <u>no effect</u> on the mean	B1		
(ii)	The median will <u>increase</u>	B1		
(iii)	The standard deviation will <u>decrease</u>	B1	(3)	
	Notes	[14]		
(a)	M1 for forming a relationship between area and no. of people $\underline{or}$ "their width" $\times$ "their hei	ght"= 7.5		
	$\frac{\text{or for } \frac{3h}{10} = \frac{9}{12} \text{ oe}}{\text{A1}}$ A1 for height of 3 (cm) NOTE: the common incorrect answer width = 3 and height = 2.5 scores B0M1A0			
(b)	M1 for a correct fraction $\left\lceil \frac{9}{12} \text{ or } \frac{9.5}{12} \right\rceil \times 3$ . Ignore end point but must be +.			
	May be seen in an equivalent expression e.g. $\frac{(x-2.5)}{5.5-2.5} = \frac{25-16}{28-16}$			
	Allow use of $(n + 1)$ giving 4.875			
	NB May work down so look out for $[5.5] - \frac{28-25}{12} \times 3$ , etc.			
(c)(i)	B1 for $\frac{394}{50}$ or for fully correct expression seen $\frac{16 \times 1.25 + 12 \times 4 + 10 \times 8 + 8 \times 15.5 + 4 \times 30.5}{50}$			
(ii)	M1 for a correct expression must have 6500, 50 and 7.88. (square root not necess $1^{st}$ A1 for a correct expression which must have square root	ary for N	11)	
	$2^{nd}$ A1 for awrt 8.24 (use of <i>s</i> = awrt 8.32). Condone incorrect labelling if awrt 8.24 is four	10.		
( <b>d</b> )	1 <sup>st</sup> B1ft for a correct comparison of $\overline{x} = 7.88$ and their $Q_2$ (this may be seen embedded)	ded in		
	another formula i.e. 3(mean-median)/s.d.)			
	$Q_3 - Q_2 > Q_2 - Q_1$ is B0 unless $Q_1$ and $Q_3$ have been found. ( $Q_1 = 1.95/1.99$ , $Q_3 = 10.25/10.81$ )			
	2 <sup>nd</sup> dB1 Dependent on the 1 <sup>st</sup> B1 and for concluding "positive" skew.			
	Note: if their $Q_2 > 7.88$ , then B0. Positive correlation is B0.			

Question	Scheme				Mar	KS			
<b>3.</b> (a)	P(X = 1) = F(1) = 0.2				B1				
	e.g. P(.	e.g. $P(X = 3) = F(3) - F(1) = 0.3$				M1			
		$\frac{x}{P(X=x)}$	1 0.2	<u> </u>	5 0.4	7 <u>0.1</u>		A1 A1	
		$\mathbf{I}(\mathbf{X}, \mathbf{X})$	0.2	0.5	0	0.1			(4)
<b>(b)</b>	P(2 < X)	$X \le 6) = P(X =$	(3) + P(X = 5)	)				M1	(.)
	× ·	_ / 、		= <u>0.7</u>				A1	
									(2)
(c)	F(4) = 1	$P(X \le 4) = P(X)$	$K \le 3) = F(3)$	= <u>0.5</u>				B1	
								[7]	(1)
				Notes				[/]	
(a)	B1	for $P(X = 1)$	= 0.2  or P(1)						
( <b>u</b> )	M1								
		correct probability)							
	$1^{\text{st}}$ A1 for any two correct probabilities from P(X = 3) = 0.3, P(X = 5) = 0.4, P(X = 7) = 0.1								
	$2^{nd}$ A1 for a fully correct probability distribution.								
	For both A marks, condone missing/incorrect labels, but the probabilities must be								
	associated with the correct <i>x</i> -values								
(b)	M1 for $P(X = 3) + P(X = 5)$ (may ft their values) or $F(5) - F(1)$								
	A1	for 0.7 oe	~ / ~	-	<u> </u>				
(c)	B1	for 0.5 oe							

Question	Scheme	Marks
<b>4.</b> (a)	P(Y > 17) = 1 - P(Y < 17) = 0.4	B1 (1)
(b)	$P(Y < \mu) = 0.5 \text{ or } [P(\mu < Y < 17) =] 0.6 - 0.5 = 0.1$	M1 A1
(c)	$[P(Y < \mu   Y < 17) = ]$	(2)
	$\frac{P(Y < \mu)}{P(Y < 17)}$ or $\frac{0.5}{0.6}$	M1
	$=\frac{5}{6}$ awrt <u>0.833</u>	A1
		(2)
	Notes	[5]
(a)	B1 for 0.4 Note: do <b>not</b> isw if 0.6554 is given as answer after 0.4 has been seen.	
(b)	M1 for indicating $P(Y < \mu) = 0.5$ (may be seen on a diagram)	
(c)	M1 for a correct statement $\frac{P(Y < \mu)}{P(Y < 17)}$ or a correct ratio of probabilities May be implied by $\frac{P(Y < \mu)}{0.6}$ or $\frac{0.5}{P(Y < 17)}$	

Question	Scheme	Marks				
<b>5.</b> (a)	-2a + (0) + 2a + 4c = 0.8 or $4c = 0.8$	M1				
	<u>c = 0.2</u>	A1				
		(2)				
(b)	4a + (0) + 4a + 16c = 5 or $8a + 16c = 5$	M1				
	$8a + 3.2 = 5$ so $\underline{a = 0.225}$ or $\frac{9}{40}$	A1				
		N/1				
	$2a+b+c=1$ so $b=1-"0.2"-2\times"0.225"$	M1 A1ft				
	<u><b>b</b></u> = <b>0.35</b> or $\frac{7}{20}$					
		(4)				
(c)	$Var(X) = 5 - 0.8^2$ , $= 4.36$	M1A1				
		(2)				
( <b>d</b> )	$[5 - 3E(X) = 5 - 3 \times 0.8] = 2.6$	B1				
		(1)				
(e)	$3^{2}$ Var $(X) = 9 \times 4.36$ , or $[E(Y^{2}) - (E(Y))^{2}] = 46 - 2.6^{2} = 39.24$ awrt 39.2	M1, A1				
( <b>f</b> )	$Y \ge 0 \implies 5 - 3X \ge 0 \implies 5 \ge 3X$	(2) M1				
(1)	$X \le 1\frac{2}{3}$	A1				
	$[P(Y \ge 0) = P(X \le 0) =] P(X = -2) + P(X = 0) \text{ or } a + b$	M1				
	$=$ <u><b>0.575</b></u> or $\frac{23}{40}$	A1ft				
	<u>40</u>					
		(4) [15]				
	Notes					
(a)	M1 for forming an equation using $E(X) = 0.8$ with at least 2 non-zero products correct					
(b)	1 <sup>st</sup> M1 for forming an equation using $E(X^2) = 5$ with at least 2 non-zero terms corre	ct. ft their c				
	1 <sup>st</sup> A1 for 0.225 or any equivalent fraction					
	$2^{nd}$ M1 for forming an equation for b using the sum of their prob <sup>2</sup> =1, (award M1 if the $2^{nd}$ A16 for 0.25 are avalaged for the that their 2 and 16 for 0.25 are avalaged for the theter their 2 and 16 for 0.25 are avalaged for the theter the transmission of transmission of the	eir(2a+b+c)=1)				
	$2^{nd}$ A1ft for 0.35 or a value of b such that their $2a+b+c=1$ (where a, b and c are all	probabilities)				
(c)	M1 for a correct expression $5-0.8^2$ (Division by 4 at any stage is M0)					
(e)	M1 for $9 \times Var(X)$ ft their Var(X). Condone $-3^2$ if +9 is used later Correct answer with no incorrect working seen in (f) scores 4/4					
( <b>f</b> )	1 <sup>st</sup> M1 for attempting to solve the inequality in X as far as $p \ge qX$ with one of p	or q correct				
	1 <sup>st</sup> A1 for $X \le 1\frac{2}{3}$ or $X \le 0$ or $X \le $ awrt 1.7	-				
	$2^{nd}$ M1 for P(X = 0) + P(X = -2) Allow letters " $a + b$ " here or ft their values.					
	$2^{nd}$ A1ft for their $(a + b)$ or 0.575 (where a, b and $a+b$ are all probabilities)					
Alt-	1 <sup>st</sup> M1 for attempting to convert X into Y (at least 1 y-value correct) (maybe see	n earlier)				
Method	$1^{\text{st}}$ A1 for 11, 5, -1 and -7 all correct	,				
	$2^{nd}$ M1 for P(Y=11) + P (Y=5) $2^{nd}$ A1ft for their $(a + b)$ or 0.575 (where a b and $a+b$ are all probabilities)					
	$2^{nd}$ A1ft for their $(a + b)$ or 0.575 (where a, b and $a+b$ are all probabilities)					

Question	Scheme	Marks
6. (a)	$P(S) = 0.31 + p$ , $P(D) = 0.35$ , $P(S \cap D) = 0.14$	M1
	(0.31 + p)(0.35) = 0.14 oe	M1
	P(S) = 0.4  or  0.31 + p = 0.4  or  0.35p = 0.0315	A1
	p = 0.09	A1
	$P(G = M = D) = 1 = -1 = (0.17 + 0.10 + 0.15 + 0.00 + 0.04) = -\pi = 0.49$	(4)
(b)	$P(S \cup M \cup D) = 1$ so $q = 1 - (0.17 + 0.10 + 0.15 + 0.06 + 0.04) - p$ or $0.48 - p$	M1
	q = 0.39	$\begin{vmatrix} A1ft \\ (2) \end{vmatrix}$
		(2)
(c)(i)	$P(D \cap S \cap M) = 0.10$	
	$[P(D \mid S \cap M] =] \frac{P(D \cap S \cap M)}{P(S \cap M)} = \frac{0.10}{0.27}$	M1
	10	
	$=\frac{10}{27}$ or awrt <b>0.370</b>	A1
(ii)		
()	$[P(D \mid S' \cap M] =] \frac{P(D \cap S' \cap M)}{P(S' \cap M)} = \frac{0.15}{0.54}$	M1
	$=\frac{5}{18}$ or awrt <b><u>0.278</u></b>	A1
		(4)
( <b>d</b> )	27 order $S \cap M$ so expect $27 \times \frac{10}{27}D$ or 36 order $S' \cap M$ so expect $36 \times \frac{5}{18}D$	M1
	So expect <u>20 (desserts)</u>	Alcao
		(2)
		[12]
	Notes	
(a)	1 <sup>st</sup> M1 for attempting P(S), P(D) and P(S $\cap$ D) with at least 2 correct.	
	These may be seen in a conditional probability.	
	NB $P(S   D) = \frac{0.14}{0.35}$ and $P(D S) = \frac{0.14}{0.31 + p}$	
	$2^{nd}$ M1 using the independence condit' and their values to form a suitable equation :	
	1 <sup>st</sup> A1 for $P(S) = 0.4 \text{ or } 0.31 + p = 0.4 \text{ or } 0.35p = 0.0315$ (i.e. one move from $p =$	)
(b)	M1 for using sum of probabilities = 1 and ft their $p$	
	A1ft for $0.48 -$ "their p" (provided $0 <$ their $p < 0.48$ )	
(c)	1 <sup>st</sup> M1 for a correct ratio of probabilities <u>or</u> a correct ratio expression with at least o	
	probability substituted. (M0 if numerator is $P(D) \times P(S \cap M)$ or numerator>	denominator)
	$1^{\text{st}} A1$ for $\frac{10}{27}$ or awrt 0.370	
		n a la anna at
	2 <sup>nd</sup> M1 for a correct ratio of probabilities <u>or</u> a correct ratio expression with at least or probability substituted. (M0 if numerator is $P(D) \times P(S' \cap M)$ or numerator>	
		actioninator)
	$2^{nd} A1$ for $\frac{5}{18}$ or awrt 0.278	
	10	
( <b>d</b> )	M1 for at least one correct calculation ft their probabilities from (c).	
	i.e. either 27×their (c)(i) or 36×their (c)(ii)	

Questio		Marks			
<b>7.</b> (a	$P\left[P(D > 50) = \right] P\left(Z > \frac{50 - 32}{12}\right)$	M1			
	=1-P(Z<1.5) or $1-0.9332$	M1			
	= <b>awrt <u>0.0668</u> or 6.68%</b>	Alcso			
(b		(3) B1			
	$\frac{d-32}{12} = 0.65$ (calc gives 0.65014 or 0.65012)	M1A1			
	$d = \underline{39.8}$	A1 (4)			
(0	$0.0668 \times 0.191^2 = 0.0024369$	M1			
	[]×3	M1			
	= 0.00731079 = awrt 0.0073	Al			
		(3)			
	Notes	[10]			
(a	$1^{st}$ M1for standardising with 50, 32 and 12. Allow ± $2^{nd}$ M1for 1 – P(Z < 1.5) seen i.e. a correct method for finding P(Z > 1.5) e.g. 1 – tables valueA1csofor awrt 0.0668 with both Ms scored and no incorrect working seen. Condone incomplete notation and condone use of different letters for Z.				
(b	B1 for awrt 0.2578 (calc = $0.257807$ ) or awrt 0.7422 (calc = $0.742192$ ) may be implied by $z = awrt 0.65$				
	M1 for standardising with 32 and 12, i.e. $\pm \frac{d-32}{12}$ (equating to a probability is M	(0)			
	$1^{\text{st}} \text{A1}$ for $z = \text{awrt } 0.65$ and a correct equation in <i>d</i> (with compatible signs) $2^{\text{nd}} \text{A1}$ for awrt 39.8				
(0	$1^{\text{st}} \text{ M1}  \text{for } 0.0668 \times 0.191^2 \text{ or sight of awrt } 0.0024 \text{ (may be seen embedded in part an expression, e.g. '}n \times 0.0668 \times 0.191^2\text{'}\text{)} \text{ (condone } 6.68\% \times 19.1\% \times 19.1\% \text{ if the final answer given is } < 1\text{)}$	of			
	$2^{nd}$ M1for any expression of the form $3pq^2$ where p and q are both probabilitiesA1for awrt 0.0073allow awrt 0.73% but 0.73 is A0				

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