

Mark Scheme (Results)

January 2018

Pearson Edexcel International GCSE Mathematics A (4MAO) Higher Paper 3H



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#### **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
  - Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

### Types of mark

- o M marks: method marks
- o A marks: accuracy marks
- o B marks: unconditional accuracy marks (independent of M marks)

#### **Abbreviations**

- o cao correct answer only
- o ft follow through
- o isw ignore subsequent working
- o SC special case
- o oe or equivalent (and appropriate)
- o dep dependent
- o indep independent
- o eeoo each error or omission

#### • No working

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score no marks.

## • With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme. If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

Any case of suspected misread loses A (and B) marks on that part, but can gain the M marks. If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If there is a choice of methods shown, then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.

If there is no answer on the answer line then check the working for an obvious answer.

### • Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

#### • Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another.

Intern	ationa	l GCSE Maths			
Ques	tion	Working	Answer	Mark	Notes
1	(a)	1 400 000÷125 000 oe <b>or</b> 14÷125 000 <b>or</b> 14×1000×100(=1 400 000) <b>or</b> 125 000÷1000÷100(=1.25)	11.2	2	M1 for a first step; can be implied by an answer with digits 112
		123 000 : 1000 : 100(-1.23)			A1
	(b)	$(4.8 \times 1000 \times 100) \div 19.2$ oe <b>or</b> $4.8 \div (19.2 \div 1000 \div 100)$ oe	25 000	2	M1 for division by 19.2; can be implied by an answer with digits 25  A1
2	(a)		2.2587(80006)	2	M1 for 11.245 or 2.204 or 5.102087 or 2.2587 rounded or truncated to 2 or more decimal places
	(b)		2.3	1	B1ft ft from (a) as long as from at least 3sf
3	(a)	$(-7)^2 + 7 \times 5$ or $-7 \times -7 + 7 \times 5$ oe or 49	84	2	M1 for correct substitution <b>or</b> correct evaluation of $(-7)^2$ NB: accept 7(5) in place of 7 × 5
	(b)	$100 = 11^{2} + 7q \text{ oe or}$ $A - p^{2} = 7q$ $100 = 11^{2} + 7q \text{ oe or } -7 = 11^{2} - 100 \text{ oe}$		3	M1 for correct substitution <b>or</b> rearrangement  M1 isolating 7q in a correct equation
			-3		A1 cao

Question	Working	Answer	Mark	Notes
<b>4</b> (a)	$(80+1) \div 2 (=40.5(th))$ or $80 \div 2 (=40(th))$	4	2	M1 <b>or</b> listing numbers and attempt to find median A1
(b)	1×5, 2×12, 3×16, 4×32, 5×15 or 5, 24, 48, 128, 75 or 280 "280"÷80	3.5 oe	3	<ul><li>M1 for at least 4 correct products – may be seen by side of table (products may not be evaluated);</li><li>M1 dep</li></ul>
	200 ÷00			Allow division by their $\sum f$ provided addition or total under column seen
				A1 condone rounding to 4 if 3.5 <b>or</b> 280 ÷ 80 is present
(c)	$\frac{32}{80} + \frac{12}{80}$ or $\frac{32+12}{80}$	$\frac{44}{80}$	2	M1 or for $\frac{44}{n}$ where $n > 44$ or $\frac{m}{80}$ where $m < 80$
				A1 for $\frac{44}{80}$ oe <b>or</b> 0.55 <b>or</b> 55%
5 (a)	$3-6y=2y-7$ or $1-2y=\frac{2y}{3}-\frac{7}{3}$	1.25 oe	3	M1 for multiplying out brackets in a correct equation <b>or</b> dividing all terms by 3
	e.g. $-6y-2y=-7-3$ or $3+7=2y+6y$ or			M1 for isolating the terms in y ft from $3-2y=2y-7$ or $1-6y=2y-7$
	-8y = -10 or $8y = 10$			A1 dep on M1 awarded

Question	Working	Answer	Mark	Notes
5 (b)		$-3 < x \leqslant 4$	2	B2 also accept $x > -3$ and $x \le 4$ or $4 \ge x > -3$ If not B2 then award  B1 for a double-ended inequality which is correct at one end (ignore the other end) eg. $-3 < x < 4$ , $-3 \le x \le 4$ , $-3 < x > 4$ or for an answer of $x > -3$ oe or $x \le 4$ oe  or the wrong variable in an otherwise correct inequality eg. $-3 < y \le 4$ SC: Award B1 for $-3 \le x < 4$
(c)	e.g. $2m \ge 8-13$	$m \geqslant -2.5$ oe	2	M1 for isolating terms in $m$ (in an equation or inequality) e.g. $2m \ge -5$ or $-2.5$ oe A1 must be an inequality

Question	Working	Answer	Mark	Notes
<b>6</b> (a)	$(QR^2 = )10.6^2 - 5.9^2 (= 77.55)$	0.01	3	M1 for squaring and subtracting.
	$(QR^{2} =)10.6^{2} - 5.9^{2} (= 77.55)$ $(QR =)\sqrt{10.6^{2} - 5.9^{2}} \text{ or } \sqrt{"77.55"}$	8.81		M1 dep
				A1 for 8.806 – 8.81
(b)	E.g. $\sin R = \frac{5.9}{10.6}$ or $\cos R = \frac{8.81}{10.6}$ or $\tan R = \frac{5.9}{8.81}$	33.8	3	M1 correct trig statement for angle <i>PRQ</i> or for angle <i>QPR</i>
	E.g. $\sin^{-1}\left(\frac{5.9}{10.6}\right)$ or $\cos^{-1}\left(\frac{'8.81'}{10.6}\right)$ or $\tan^{-1}\left(\frac{5.9}{'8.81'}\right)$			M1 complete method to find angle <i>PRQ</i>
				A1 for 33.8 – 33.82125
(c)		12.45	1	B1 12.45 or 12.449

Question	Working	Answer	Mark		Notes
7	(-2, 11)(-1, 8)(0, 5)(1, 2) (2, -1)(3, -4)	Correct line between $x = -2$ and $x = 3$	3	B3	for a correct line between $x = -2$ and $x = 3$ If not B3 then award B2 for a correct line through at least 3 of $(-2, 11) (-1, 8) (0, 5) (1, 2) (2, -1) (3, -4)$ OR for all of $(-2, 11) (-1, 8) (0, 5) (1, 2) (2, -1) (3, -4)$ plotted, not joined  If not B2 then award B1 for for at least 2 correct points stated or calculated (may be in a table) OR for a line with a gradient of $-3$ OR for a line drawn with a negative gradient through $(0, 5)$ NB: No mark should be awarded for a line through $(0, 5)$ and $(3, 0)$
8	arc centre B cutting BA and BC at (say) P and Q ANI arcs centres P and Q of equal radii which intersect at (R must fall within guidelines) bisector drawn with all necessary arcs		2	M1 A1	dep SC: B1 for bisector within guidelines with no arcs

Question	Working	Answer	Mark	Notes
9	4x + 28 + x - 13 = 180	18	4	M1 for a correct equation in $x$
	x = 33 360 ÷ ("33" – 13) oe			A1 for the correct value of x  M1 (dep on M1) for a correct calculation to find n ft "33"
				A1
10	$m = -4 \text{ or}$ $2y + 8x = k  (k \neq 5)$	y = -4x + 11	3	M1 for recognising gradient = $-4$ e.g. an answer of $y = -4x + c$ with $c \ne 2.5$
	$3 = \text{``}-4\text{''} \times 2 + c \text{ or}$ y - 3 = ``-4''(x - 2)  or c = 11			M1 (indep) for correct method to find $c$ using their gradient or $2 \times 3 + 8 \times 2 = k$
				A1 oe eg $y - 3 = -4 \times (x - 2)$ , $2y + 8x = 22$ NB L = $-4x + 11$ oe scores M1 M1 A0

Question	Working	Answer	Mark		N	otes
11	$eg \frac{23}{100} \times 330 \text{ oe } (=75.9)$	151	3	M1	for $\frac{23}{100} \times 330$ oe or 75.9	M2 for $330 \times 0.77^3$ or $330 \times 0.77^4$ (=116.00))
	$\frac{23}{100} \times (330 - \text{``75.9''}) \ (= 58.443)$ $\frac{23}{100} \times (330 - \text{``75.9''} - \text{``58.443''}) \ (= 45.00)$			M1	for a complete method (condone 4 years rather than 3)	If not M2 then award M1 for $330 \times 0.77$ (=254.1(0)) or $330 \times 0.77^2$ (=195.65(7))
	330 – "75.9" – "58.443" – "45.00"			A1	accept $(1 - 0.23)$ as equivale for $150.6 - 151$ SC If no other marks gained, aw or $330 \times 0.31$ oe $(=102.3)$ or	vard B1 for 330 × 0.69 oe (=227.7)
12	e.g. $\frac{4(x+4)}{12} + \frac{3(2x+3)}{12} (=7)$ $\mathbf{OR} \frac{4(x+4) + 3(2x+3)}{12} (=7)$ $\mathbf{OR} 4(x+4) + 3(2x+3) = 7 \times 3 \times 4$ e.g. $4x + 16 + 6x + 9 = 7 \times 12$ $\mathbf{OR} 10x + 25 = 7 \times 12$	5.9 oe	3	M1 M1 A1	for dealing with fractions e.g. express LHS as the sum 12 or a multiple of 12 (if bra or express LHS as a single frac	of 2 fractions with denominator of ackets expanded, condone 1 error)  tion with denominator of 12 or a expanded, condone 1 error) or a multiple of 12 one 1 error))  and expanding brackets

Question	Working	Answer	Mark	Notes
13 (a)		35 700 000	1	B1
(b)	$(3.57 \times 10^7) \div (1.35 \times 10^4) (= 2644(.44))$ or $35700000 \div 13500$ oe	$2.6 \times 10^{3}$	2	M1 <b>or</b> for 2600 – 2644.4
				A1 must be in standard form <b>and</b>
				in the range $2.6 \times 10^3 - 2.64 \times 10^3$
14	11 - 3	8	2	M1 for identifying 3 and 11 as LQ and UQ may be circled in list
				A1
15	E.g. $AOC = 360 - 2 \times 90 - 76 \ (=104)$ or $AOC = 180 - 76 \ (=104)$ oe	52	3	M1 for a method to find angle AOC
	"104" ÷ 2			M1 (dep) for complete method to find angle <i>ABC</i> A1

Question	Working	Answer	Mark		Notes
16	eg $100x = 34.545$ and $x = 0.345$ $100x - x = 34.545 - 0.345$	Shown by an algebraic method	2	M1	for two decimals that, when subtracted will leave a non-recurring value, <b>and</b> intention to subtract (must show recurring dots or at least 2 of 54 or 45)
				A1	must see a correct fraction prior to $\frac{19}{55}$ or division must be clearly shown
	Alternative scheme eg $10x = 0.45$ $1000x = 45.45$ 1000x - 10x = 45.45 - 0.45			M1	for two decimals that, when subtracted will leave a non-recurring value, <b>and</b> intention to subtract
	$990x = 45  \mathbf{x} = \frac{45}{990}  0.345 = \frac{3}{10} + \frac{45}{990}$	Shown by an algebraic method		A1	for a complete method
17	$x^2 = \frac{2b - a}{7 - am}$		4	M1	for squaring both sides
	$7 - am$ $x^2 (7 - am) = 2b - a$			M1	for multiplying by $7 - am$ in a correct equation allow $x^2 \times 7 - am = 2b - a$ $7 - am \times x^2 = 2b - a$
	$7x^2 - 2b = amx^2 - a$ or $a - amx^2 = 2b - 7x^2$			M1	for isolating terms in $a$ in a correct equation
		$a = \frac{7x^2 - 2b}{mx^2 - 1}$ oe		A1	or for $a = \frac{2b - 7x^2}{1 - mx^2}$ oe with $a$ as the subject

Question	Working	Answer	Mark	Notes
<b>18</b> (a)	$\frac{7}{\sqrt{132}} = \frac{h}{\sqrt{297}} \text{ oe or } 7 \times \frac{\sqrt{297}}{\sqrt{132}} \text{ oe or } 7 \div \frac{\sqrt{132}}{\sqrt{297}}$	10.5 oe	2	for a correct linear scale factor $ \frac{\sqrt{297}}{\sqrt{132}} \underbrace{\frac{\sqrt{132}}{\sqrt{297}}}_{\text{oe}} $ A1
(b)	e.g. $567 \div \left( \frac{3}{2} \right)^3$ or $567 \times \left( \frac{2}{3} \right)^3$	168	2	M1 for a fully correct method NB: scale factor may not be simplified and could be ft from (a) dep on M1 scored in (a) A1
<b>19</b> (a)	33 ÷ 10 (=3.3) , 39 ÷ 15 (=2.6), 36 ÷ 20 (=1.8),12 ÷ 15 (=0.8) fd 3.3, 2.6, 1.8, 0.8		3	M1 for use of area e.g. correct method for any 2 frequency densities or any 2 correct bars of different widths  M1 for at least 3 correct fd or
		A fully correct histogram		at least 3 correct bars  A1 for a correct histogram, with a linear scale on fd axis or a key
(b)	$0.75 \times 36 + 12 \ (=39)$	$\frac{39}{120}$	2	M1 for a fully correct method to find number of people who travelled more than 30 km  A1 for $\frac{39}{120}$ oe e.g. 0.325, 32.5%
	Alternative method E.g. "3.3" × 2 + "2.6" × 3 + "1.8" × 4 + "0.8" × 3 (= 24) and "1.8" × 3 + "0.8" × 3 (= 7.8)	$\frac{39}{120}$		M1 dep on at least M1 in (a) ft from their graph using area  A1 for $\frac{39}{120}$ oe e.g. 0.325, 32.5%

Question	Working	Answer	Mark	Notes
<b>20</b> (a)	$ \sqrt{25 \times 2} + \sqrt{64 \times 2} - \sqrt{100 \times 2} $ or $5\sqrt{2} + 8\sqrt{2} - 10\sqrt{2}$ or $3\sqrt{2}$	3	2	<ul> <li>M1 for at least 2 out of 3 correct products from those shown or for 3√2</li> <li>A1</li> </ul>
(b)	E.g. $\frac{5\sqrt{a} + a}{10\sqrt{a}} \times \frac{\sqrt{a}}{\sqrt{a}} \text{ or } \frac{5\sqrt{a}}{10\sqrt{a}} + \frac{a}{10\sqrt{a}} \text{ or } \frac{\sqrt{a}(5 + \sqrt{a})}{10\sqrt{a}}$	$\frac{1}{2} + \frac{1}{10}\sqrt{a}$	2	<ul> <li>M1 √a for multiplying numerator and denominator by √a (or a multiple of √a) or splitting fraction into 2 parts or taking out √a as a common factor</li> <li>A1 from correct working NB. individual fractions need not be in their simplest form</li> </ul>
21	$((10a-b)+(2a-5b))((10a-b)-(2a-5b))$ Or $(10a-b+2a-5b)(10a-b-2a+5b)$ $(12a-6b)(8a+4b)$ Alternative $(100a^2-10ab-10ab+b^2) \text{ or } 4a^2-10ab-10ab+25b^2 \text{ or } -4a^2+10ab+10ab-25b^2$	24(2a-b)(2a+b) $24(2a-b)(2a+b)$	3	<ul> <li>M1 first stage in using difference of 2 squares allow -2a - 5b in place of -(2a - 5b)</li> <li>M1 simplifying 2 correct brackets</li> <li>A1 fully factorised expression from correct working</li> <li>M1 expanding one bracket correctly</li> </ul>
	$96a^2 - 24b^2$			M1 simplifying 2 correct expansions  A1 fully factorised expression from correct working

Question	Working	Answer	Mark	Notes
22	$\sqrt[5]{\frac{32}{3125}} \left( = \frac{2}{5} \text{ oe} \right)$	$\frac{240}{3125}$	3	M1 a correct method to find probability of getting one head
	$\left( \frac{2}{5} \right)^4 \times \left( 1 - \frac{2}{5} \right) $ oe $\left( = \frac{48}{3125} $ oe $\right)$			M1 (dep) for the probability of getting one combination of 4 heads and 1 tail
				A1 oe eg $\frac{48}{625}$ , 0.0768
23 (a)	-4-2	1.6	2	M1 A1 oe
	$\left(\operatorname{gf}(x) = \right) \frac{4\left(\frac{3x}{x-2}\right)}{5} \text{ oe or } \frac{4\left(\frac{3\times-4}{-4-2}\right)}{5}$			
(b)	$\frac{3 \times \frac{4x}{5}}{\frac{4x}{5} - 2}$	$\frac{6x}{2x-5}$	3	M1 for a correct first expression for $fg(x)$
	E.g. $\frac{12x}{4x-10}$ oe			M1 for a correct unsimplified fraction of the form $\frac{ax}{bx-c}$ where
	10			a, b and c are integers A1 cao
				SC: Award B2 for $\frac{3x}{x-2.5}$

Question	Working		Answer	Mark		Notes	
(c)	$y = \frac{3x}{x-2}$ $y(x-2) = 3x$ $xy-3x = 2y \text{ or }$ $x(y-3) = 2y$	$x = \frac{3y}{y-2}$ $x(y-2) = 3y$ $xy - 3y = 2x \text{ or } y(x-3)$ $= 2x$	$\frac{2x}{x-3}$	3	M1	for writing function in the form $y = \frac{3x}{x-2} \text{ or } x = \frac{3y}{y-2} \text{ and multiplying both sides by the denominator isolating terms in } x \text{ (or } y)$	
					A1	oe must be in terms of $x$	
24	$\overrightarrow{BX} = \frac{3}{2} \times 4\mathbf{a} = (6\mathbf{a}) \text{ or}$ $\overrightarrow{CX} = \frac{5}{2} \times 4\mathbf{a} = (10\mathbf{a}) \text{ or}$ $\overrightarrow{AX} = \frac{3}{2} \times 4\mathbf{a} + 3\mathbf{c} = (6\mathbf{a} + 3\mathbf{c}) \text{ or}$ $\overrightarrow{OY} = \overrightarrow{OC} + \overrightarrow{CY} \text{ or } \overrightarrow{OY} = \overrightarrow{OC} + 2\overrightarrow{AX}$		9 <b>c</b> + 12 <b>a</b>	3	M1	correct vector, in terms of <b>a</b> and/or <b>c</b> for $\overrightarrow{BX}$ or $\overrightarrow{CX}$ or $\overrightarrow{AX}$ (need not be simplified)  or $\overrightarrow{OY} = \overrightarrow{OC} + \overrightarrow{CY}$ or $\overrightarrow{OY} = \overrightarrow{OC} + 2\overrightarrow{AX}$ (accept 3 <b>c</b> in place of $\overrightarrow{OC}$ and their $\overrightarrow{CY}$ and their $\overrightarrow{AX}$ if clearly stated in terms of <b>a</b> and <b>c</b> )	
	$\overrightarrow{CY}(\text{or }2\overrightarrow{AX}) = 2(-4\mathbf{a}$ 12 <b>a</b> )	+3c + 4a + 6a) ( = $6c +$			M1 A1	correct vector for $\overrightarrow{CY}(\text{or }2\overrightarrow{AX})$ (need not be simplified) implies the award of both method marks for $9\mathbf{c} + 12\mathbf{a}$ or $3(3\mathbf{c} + 4\mathbf{a})$	

Question	Working	Answer	Mark		Notes
25	e.g. angle $AOB = 360 \div 5$ (=72) <b>or</b> angle $ABC = 108$ <b>or</b> angle $OBC = 54$ <b>or</b> angle $COM = 36$	63.1	5	M1	for correct use of angles in a pentagon
	e.g. $AO = \frac{4}{\cos(54)}$ (= 6.8(05)) oe			M1	for a method to find AO (or BO etc) or OM
	$OM = 4 \tan(54) (= 5.5(055))$ oe e.g. $\tan APO = \frac{"6.8"}{10} $ (angle $APO = 34(.2)$			M1	for a method to find angle APO or angle OPM <b>OR</b>
	e.g. $\tan OPM = \frac{"5.5"}{10}$ (angle $OPM = 28.8$ or 29)				for a method to find angle <i>PAO</i> (55.8) <b>AND</b> angle <i>PMO</i> (61.1)
	"34.2" + "28.8" <b>OR</b> 180 - "55.8" - "61.1"			M1	for a complete method
				A1	for answer in the range $62.9 - 63.2$
	Alternative e.g. angle $AOB = 360 \div 5$ (=72) or angle $ABC = 108$ or angle $OBC = 54$ or angle $COM = 36$	63.1	5	M1	for correct use of angles in a pentagon
	e.g. $AO = \frac{4}{\cos(54)} (= 6.8(05))$ oe			M1	f for a method to find AO (or BO etc) or OM
	$OM = 4 \tan(54) (= 5.5(055))$ oe e.g. $AP = \sqrt{10^2 + 6.8^2}$ <b>AND</b> $MP = \sqrt{10^2 + 5.5^2}$			M1	for a method to find AP (or BP etc) AND MP
	$(= 12.(09) \qquad (= 11.(415)$ $\cos APM = \frac{12.09^2 + 11.415^2 - 12.31^2}{2 \times 12.09 \times 11.415}$ e.g.			M1	for a complete method
				A1	for answer in the range $62.9 - 63.2$