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Mark Scheme (Results)

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International GCSE Mathematics
(4MA0) Paper 4H

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Apart from Questions 3, 13(b) and 17(f) (where the mark scheme states otherwise), the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

| Question | Working | Answer | Mark | Notes |
| :--- | :--- | ---: | :---: | :--- |
|  |  |  |  |  |
| $\mathbf{1 .}$ | $\frac{4.2}{1.12}$ |  | 2 | M1 for 4.2 or 1.12 or 0.6 or $\frac{15}{4}$ |
|  |  | 3.75 |  | A1 |
|  |  |  |  |  |


| 2. | $\frac{135}{180}$ |  | 3 | M1 |
| :--- | :--- | :--- | :--- | :--- |
|  | 0.75 oe |  |  | A1 |
|  |  |  | 45 |  |
| A1 cao |  |  |  |  |
|  |  |  |  |  |



| 6. (a) | $1+7$ or 8 |  | 2 | M1 | 8 may be denominator of fraction or coefficient in an equation such as $8 x=32$ | SC <br> If M0 A0, <br> award B1 <br> for 4:28 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 28 |  | A1 | cao |  |
| (b) | $32 \times 45$ or 1440 or 14.4(0)m |  | 3 | M1 |  |  |
|  | $\frac{" 1440 "}{72}$ |  |  | M1 | dep |  |
|  |  | 20 |  | A1 | cao |  |
|  |  |  |  |  |  | l 5 marks |


| 7. | Fully correct factor tree or repeated division <br> or $2,2,2,5,5$ or $2 \times 2 \times 2 \times 5 \times 5$ | 3 | M2M1 for factor tree or repeated <br> division with 2 and 5 as factors |  |
| :--- | :--- | :--- | :--- | :--- |
|  |  | $2^{3} \times 5^{2}$ |  | A1 Also accept $2^{3} .5^{2}$ |
|  |  |  |  | Total 3 marks |


| 8. | $y^{3+n-1}=y^{6}$ oe or $y^{3+n}=y^{7}$ oe <br> or $3+n-1=6$ oe <br> or $y^{n}=\frac{y^{7}}{y^{3}}$ or $y^{n}=\frac{y^{6}}{y^{2}}$ or $y^{n}=y^{4}$ | 2 | M1 | SC if M0, award B1 for <br> an answer of $y^{4}$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  | 4 |  | A1 cao |  |


| 9. (a) | Complete, correct expression which, if correctly evaluated, gives 48 eg $4 \times \frac{1}{2} \times 6 \times 4,2 \times \frac{1}{2} \times 12 \times 4, \frac{1}{2} \times 12 \times 8$ |  | 3 | $\begin{array}{ll} \hline \text { M2 } & \text { M1 for correct expression for area } \\ \text { of one relevant triangle } \\ \text { eg } \frac{1}{2} \times 6 \times 4, \frac{1}{2} \times 6 \times 4 \sin 90^{\circ}, \\ & \frac{1}{2} \times 8 \times 6, \frac{1}{2} \times 12 \times 4 \\ \hline \end{array}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 48 |  | A1 | cao |
| (b) | $4^{2}+6^{2}=16+36=52$ |  | 3 | M | for squaring and adding |
|  | $\sqrt{4^{2}+6^{2}}$ |  |  |  | (dep) for square root |
|  |  | 7.21 |  | A1 | for answer which rounds to 7.21 (7.211102...) |
|  |  |  |  |  | Total 6 marks |


| 10. (i) |  | $-1 \frac{1}{2}<x \leq 2$ | 4 | B2Also accept $-\frac{3}{2}<x \leq 2$ or answer <br> expressed as two separate <br> inequalities <br> B1 for $-1 \frac{1}{2}<x$ or $-\frac{3}{2}<x$ <br> or $x \leq 2$ (these may be as part of a <br> double-ended inequality) <br> or $-\frac{6}{4}<x \leq \frac{8}{4}$ |
| :---: | :---: | :---: | :---: | :---: |
| (ii) |  |  | $-1 \quad 0 \quad 12$ | 2 |


| 11. (a) | $\begin{aligned} & 75=3 \times 5^{2} \text { and } 90=2 \times 3^{2} \times 5 \\ & \text { or } 1,3,5,15,25,75 \text { and } \\ & 1,2,3,5,6,9,10,15,18,30,45,90 \\ & \text { or } 3 \times 5 \end{aligned}$ |  | 2 |  | Need not be products of powers; accept products or lists ie 3,5,5 and 2,3,3,5 <br> Prime factors may be shown as factor trees or repeated division |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 15 |  | $\begin{aligned} & \mathrm{A} 1 \\ & \hline \text { M1 } \end{aligned}$ | Also award for $\frac{75 \times 90}{15}$ |  |
| (b) | $\begin{aligned} & 2 \times 3^{2} \times 5^{2} \text { oe eg } 6 \times 3 \times 5^{2} \\ & \text { or } 75,150,225,300,375,450 \\ & \text { and } 90,180,270,360,450 \end{aligned}$ |  | 2 |  |  |  |
|  |  | 450 |  | A1 |  |  |
|  |  |  |  | Total 4 marks |  |  |
|  |  |  |  |  |  |  |
| 12. (a) |  | Rotation | 3 | B1 |  | These marks are independent but award no marks if the answer is not a single transformation |
|  |  | $90^{\circ}$ |  | B1 | Also accept quarter turn or $-270^{\circ}$ (B0 for $90^{\circ}$ clockwise) |  |
|  |  | $(0,0)$ |  | B1 | Also accept <br> origin, $O$ transfo |  |
| (b) |  | R correct | 1 | B1 |  |  |
| (c) |  | Rotation $90^{\circ}$ | 2 | B1 | Accept quarter turn or $-270^{\circ}$ instead of $90^{\circ}$ | As for (a) |
|  |  | $(3,1)$ |  | B1 ft from their $\mathbf{R}$ if it is a translation of the correct $\mathbf{R}$ |  |  |
|  |  |  |  |  |  | al 6 marks |


| 13. (a) | $4 y=10-3 x$ or $-4 y=3 x-10$ |  | 3 |  | May be implied by second M1 or by $y=-\frac{3}{4} x+c$ even if value of $c$ is incorrect. or finds coordinates of 2 points on the line eg ( $0,2.5$ ), $x=2, y=1$, table, diagram. |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $y=\frac{5}{2}-\frac{3}{4} x$ oe or $y=\frac{10}{4}-\frac{3}{4} x$ oe or $y=\frac{10-3 x}{4}$ oe |  |  |  | or for clear attempt to evaluate $\frac{\text { vert diff }}{\text { horiz diff }}$ for their pts |
|  |  | $-\frac{3}{4}$ |  | A1 | Award 3 marks for correct answer if either first M1scored or no working shown. <br> SC If M0, award B1 for $-\frac{3}{4} x$ |


| 13 (b) | $\begin{array}{r} \hline \text { eg } 9 x+12 y=30 \\ 10 x-12 y=46 \end{array}$ | $\begin{aligned} \text { eg } 15 x+20 y & =50 \\ 15 x-18 y & =69 \end{aligned}$ |  | 5 | M1 for coefficients of $x$ or $y$ the same or for correct rearrangement of one equation followed by correct substitution in the other $\text { eg } 5 x-6\left(\frac{10-3 x}{4}\right)=23$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $x=4$ | $y=-\frac{1}{2}$ |  |  | A1 cao dep on M1 |
|  |  |  |  |  | M1 (dep on 1st M1) for substituting for other variable |
|  |  |  | $x=4, \quad y=-\frac{1}{2}$ |  | A1 Award 4 marks for correct values if at least first M1 scored |
|  |  |  | (4, $-\frac{1}{2}$ ) |  | B1 Award 5 marks for correct answer if at least first M1 scored ft from their values of $x$ and $y$ |
|  |  |  |  |  | Total 8 marks |


| 14. (a) |  | 55115155177190200 | 1 | B1 | cao |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) |  | Points correct | 2 | B1 | $\pm 1 / 2 \mathrm{sq} \mathrm{ft}$ from sensible table ie clear attempt to add frequencies |
|  |  | Curve or line segments |  | B1 | ft from points if 4 or 5 correct or ft correctly from sensible table or if points are plotted consistently within each interval at the correct heights Accept curve which is not joined to the origin |
| (c) | 26 indicated on cf graph |  | 2 | M | for 26 indicated on cf graph - accept 26-27 inc |
|  |  | approx 60 from correct graph |  | A1 | If M1 scored, ft from cf graph If M1 not scored, ft only from correct curve \& if answer is correct ( $\pm 1 / 2$ sq tolerance) award M1 A1 |
|  |  |  |  | Total 5 marks |  |
| 15. <br> $-4<x<4$ <br> 2 <br> B2 B1 for $x<4$ or $x>-4$ or $x< \pm 4$ <br> or $x<\sqrt{16}$ <br> SC B1 for $-4 \leq x \leq 4$ |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  | Total 2 marks |


| $16 .$ <br> (a) | $\frac{3}{8}+\frac{2}{8}$ oe |  | 2 | M1 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $\frac{5}{8}$ |  | A1 |  |  |
| (b)(i) | $\frac{2}{8} \times \frac{1}{7}$ appearing once only |  | 5 | M1 |  | Sample space <br> method - <br> award 2 <br> marks for <br> correct <br> answer; <br> otherwise no marks |
|  |  | $\frac{2}{56}$ or $\frac{1}{28}$ |  | A1 | $\begin{aligned} & \text { for } \frac{2}{56} \text { or } \frac{1}{28} \\ & \text { or for } 0.036 \\ & \text { or for answer } \\ & \text { rounding to } 0.036 \end{aligned}$ |  |
| (ii) | $\frac{2}{8} \times \frac{3}{7}+\frac{3}{8} \times \frac{2}{7}$ or $2 \times \frac{2}{8} \times \frac{3}{7}$ oe |  |  | M1 for one correct product <br> M1 for completely correct expression |  |  |
|  |  | $\frac{12}{56}$ |  | A1 for $\frac{12}{56}$ oe inc $\frac{3}{14}$ or for 0.21 or for answer rounding to 0.21 |  |  |
|  |  |  |  | Note for (b)(ii): sample space method award 3 marks for correct answer; otherwise no marks <br> SC M1 for $\frac{2}{8} \times \frac{3}{8}$ or $\frac{3}{8} \times \frac{2}{8}$ <br> M1 (dep) for $\frac{2}{8} \times \frac{3}{8}+\frac{3}{8} \times \frac{2}{8}$ oe <br> SC Sample space method - award 2 marks for $\frac{12}{64}$ oe; otherwise no marks |  |  |
|  |  |  |  | Total 7 marks |  |  |


| 17. (a) |  | 2 | 1 | B1 | cao |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (b) |  | $x<6$ | 2 |  | $\begin{aligned} & \text { cao B1 for eg } x \leq 6 \\ & \text { or } \ldots-2,-1,0,1,2,3,4,5 \\ & \text { SC B1 for } x \geq 6 \end{aligned}$ |
| (c) |  | 7 | 1 | B1 | cao |
| (d) | $\mathrm{g}(0)=15$ |  | 2 | M1 | for 15 seen |
|  |  | 3 |  | A1 | cao If M0, award B1 for $\pm 3$ oe |
| (e) | $k=12$ |  | 3 | M1 | May be stated or indicated on diagram. May be implied by one correct solution. |
|  |  | -0.7 or -0.83 .8 |  | A2 | A1 for solution rounding to -0.7 or -0.8 <br> A1 for solution rounding to 3.8 |
| (f) | tan drawn at $x=3.5$ |  | 3 | M1 | tan or tan produced passes between points ( $3,3 \leq y \leq 6$ ) and $(4,11 \leq y \leq 14)$ |
|  | vertical difference horizontal difference |  |  |  | finds their $\frac{\text { vertical difference }}{\text { horizontal difference }}$ for two points on tan or finds their $\frac{\text { vertical difference }}{\text { horizontal difference }}$ for two points on curve, where one of the points has an $x$-coordinate between 3 and 3.5 inc and the other point has an $x$-coordinate between 3.5 and 4 inc |
|  |  | $6.5-11$ inc |  | A1 | dep on both M marks |
|  |  |  |  |  | Total 12 marks |


| 18. | $\left(\cos x^{\circ}=\right) \frac{4^{2}+6^{2}-8^{2}}{2 \times 4 \times 6}$ <br> or $8^{2}=4^{2}+6^{2}-2 \times 4 \times 6 \cos x^{\circ}$ |  | 3 |  | for correct substitution in Cosine Rule |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\left(\cos x^{\circ}=\right)-0.25$ oe |  |  | A1 |  |
|  |  | 104.5 |  |  | for value rounding to 104.5 (104.4775...) |
|  |  |  |  |  | Total 3 marks |



| 20. | $\pi \times r \times 9=100$ oe |  | 5 | M1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | ( $r=$ ) 3.53677... |  |  |  | for 3.53 or for value rounding to 3.54 (3.14 $\rightarrow 3.53857 \ldots$...) |
|  | $\sqrt{9^{2}-" 3.53 \ldots{ }^{2}}$ |  |  | M1 |  |
|  | ( $h=$ ) 8.2759... |  |  |  | for 8.27 or for value rounding to 8.28 |
|  |  | 108 |  |  | for answer rounding to 108 $(\pi \rightarrow 108.40 \ldots$ <br> $3.14 \rightarrow 108.45 \ldots$ ) <br> If both M1s scored , award 5 marks for an answer which rounds to 108 |
|  |  |  |  |  | Total 5 marks |


| 21. (a) |  | $8 y^{6}$ | 2 | B2 | B1 for 8 B1 for $y^{6}$ |
| :--- | :--- | ---: | ---: | ---: | :--- |
| (b) | $2^{p} \times\left(2^{3}\right)^{q}=2^{p} \times 2^{3 q}=2^{p+3 q}$ | $p+3 q$ | 2 | B2 $\quad$ B1 for $2^{3 q}$ seen |  |
|  |  |  |  |  |  |


| 22. (a)(i) |  | $3 \mathbf{a}+3 \mathbf{b}$ oe | 3 | B1 |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| (ii) |  | $2 \mathbf{a}+2 \mathbf{b}$ oe |  | B1 | Accept eg $\frac{2}{3}(3 \mathbf{a}+3 \mathbf{b})$ |
| (iii) |  | $\mathbf{a}+2 \mathbf{b}$ oe |  | B1 | Accept eg $2 \mathbf{a}+2 \mathbf{b}-\mathbf{a}$ |
| (b) | $\overrightarrow{D F}=2 \mathbf{a}+4 \mathbf{b} \text { oe }$ |  | 2 | M1 | Also award for $\overrightarrow{E F}=\mathbf{a}+2 \mathbf{b}$ oe |
|  |  | $\begin{array}{r} \overrightarrow{D F}=\overrightarrow{D E} \text { oe } \\ \quad \text { eg } \overrightarrow{D E}=\overrightarrow{E F} \end{array}$ |  | A1 | Also award A1 for an acceptable explanation in words. |
|  |  |  |  |  | Total 5 marks |

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