

Mark Scheme (Results)

January 2012

International GCSE Mathematics (4MAO) Paper 4H

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Apart from Questions 3, 13(b) and 17(f) (where the mark scheme states otherwise), the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

Question	Working	Answer	Mark	Notes
1.	$\frac{4.2}{1.12}$		2	M1 for 4.2 or 1.12 or 0.6 or $\frac{15}{4}$
		3.75		A1
				Total 2 marks

2.	135		3	M1
	$\overline{180}$			
	0.75 oe			A1
		45		A1 cao
				Total 3 marks

r-					
3.	4x = 7 or 4x = 2 + 5 or $7x - 3x = 7 \text{ oe}$ or $4x - 7 = 0 \text{ oe}$		3	M2	for correct rearrangement with x terms on one side and numbers on the other AND collection of terms on at least one side or for $4x - 7 = 0$ oe M1 for $7x - 3x = 2 + 5$ oe ie correct rearrangement with x terms on one side and numbers on the other
		$1\frac{3}{4}$ oe		A1	Award full marks for a correct answer if at least 1 method mark scored
					Total 3 marks
	•				
4.	1 7 7		3	B2	for 1 7 7 in any order B1 for three positive whole numbers with either a median of 7 or a sum of 15 SC Award B1 for 0 7 8
		6		B1	cao
					Total 3 marks
	•		•	•	
5.	One correct point plotted or stated		4	B1	May appear in table
	2nd correct point plotted or stated			B1	May appear in table
	Correct line be	tween $x = -2$ and $x = 4$		B2	B1 for a line joining two correct, plotted points
					Total 4 marks

6. (a)	1 + 7 or 8		2	M1			SC If M0 A0, award B1 for 4:28
		28		A1	cao		
(b)	32 × 45 or 1440 or 14.4(0)m		3	M1			1
	" <u>1440"</u> 72			M1	dep		
		20		A1	cao		
						To	tal 5 marks
7.	Fully correct factor tree or repeated division or 2, 2, 2, 5, 5 or $2 \times 2 \times 2 \times 5 \times 5$		3	M2		factor tree or rewith 2 and 5 as	
		$2^3 \times 5^2$		A1	Also acc	cept 2 ³ .5 ²	
						To	tal 3 marks
8.	$y^{3+n-1} = y^6 \text{ oe or } y^{3+n} = y^7 \text{ oe}$ or $3+n-1=6$ oe or $y^n = \frac{y^7}{y^3}$ or $y^n = \frac{y^6}{y^2}$ or $y^n = y^4$		2	M1		SC if M0, aw an answer of	
		4		A1	cao		
						To	tal 2 marks

9. (a)	Complete, correct expression which, if correctly evaluated, gives 48 eg $4 \times \frac{1}{2} \times 6 \times 4, \ 2 \times \frac{1}{2} \times 12 \times 4, \ \frac{1}{2} \times 12 \times 8$		3	M2 M1 for correct expression for area of one relevant triangle $eg \frac{1}{2} \times 6 \times 4, \frac{1}{2} \times 6 \times 4 \sin 90^{\circ},$ $\frac{1}{2} \times 8 \times 6, \frac{1}{2} \times 12 \times 4$
		48		A1 cao
(b)	$4^2 + 6^2 = 16 + 36 = 52$		3	M1 for squaring and adding
	$\sqrt{4^2+6^2}$			M1 (dep) for square root
		7.21		A1 for answer which rounds to 7.21
				(7.211102)
				Total 6 marks

10. (i)	$-1\frac{1}{2} < x \le 2$	4	B2 Also accept $-\frac{3}{2} < x \le 2$ or answer
			expressed as two separate inequalities
			-
			B1 for $-1\frac{1}{2} < x$ or $-\frac{3}{2} < x$
			or $x \le 2$ (these may be as part of a
			double-ended inequality)
			$or -\frac{6}{4} < x \le \frac{8}{4}$
(ii)	-1 0 1 2		B2 B1 for 4 correct and 1 wrong
			or for 3 correct and 0 wrong
			Total 4 marks

	or 75,150,225,300,375,450 and 90,180,270,360,450	450	A	Also award for $\frac{75 \times 90}{15}$
(t			2 M	11 75×90
		15	A	1
11. (ε	75 = 3×5^2 and $90 = 2 \times 3^2 \times 5$ or 1,3,5,15,25,75 and 1,2,3,5,6,9,10,15,18,30,45,90 or 3×5		2 M	Need not be products of powers; accept products or lists ie 3,5,5 and 2,3,3,5 Prime factors may be shown as factor trees or repeated division

12.	(a)	Rotation	3	B1			
		90°		B1	Also accept quarter turn or -270° (B0 for 90° clockwise)	indepe award the ans a singl	
		(0,0)		B1	Also accept origin, O	transfo	ormation
	(b)	R correct	1	B1			
	(c)	Rotation 90°	2	B1	Accept quarter t -270° instead o		As for (a)
		(3, 1)		B1	ft from their R is a translation of correct R		
						Tot	al 6 marks

13.	(a)	4y = 10 - 3x or $-4y = 3x - 10$		3	M1	May be implied by second M1 or
						by $y = -\frac{3}{4}x + c$ even if value of c
						is incorrect.
						or finds coordinates of 2 points on
						the line eg $(0, 2.5)$, $x = 2$, $y = 1$,
						table, diagram.
		$y = \frac{5}{2} - \frac{3}{4}x$ oe or $y = \frac{10}{4} - \frac{3}{4}x$ oe			M1	or for clear attempt to evaluate
		$y = \frac{1}{2} - \frac{1}{4}x$ de or $y = \frac{1}{4} - \frac{1}{4}x$ de				vert diff for their pts
		or $y = \frac{10 - 3x}{4}$ oe				horiz diff
		or $y = \frac{1}{4}$ oe				
			3		A 1	Award 3 marks for correct answer
			$-\frac{1}{4}$		A1	if either first M1scored or no
			•			working shown.
						SC If M0, award B1 for $-\frac{3}{4}x$

13	(b)	eg $9x + 12y = 30$	eg $15x + 20y = 50$		5	M1	for coefficients of x or y the same
		10x - 12y = 46	15x - 18y = 69				or for correct rearrangement of
							one equation followed by correct substitution in the other
							$eg \ 5x - 6\left(\frac{10 - 3x}{4}\right) = 23$
		,	v = _ 1				
		x = 4	$y=-\frac{1}{2}$			A1	cao dep on M1
						M1	(dep on 1st M1) for substituting
							for other variable
				$x = 4, y = -\frac{1}{2}$		A1	Award 4 marks for correct values
				$x - 4, y = -\frac{1}{2}$		AI	if at least first M1 scored
				(4 1)		B1	Award 5 marks for correct answer
				$(4, -\frac{1}{2})$		DI	if at least first M1 scored
							ft from their values of x and y
							Total 8 marks

14. (a)	55 11	5 155 177 190 200	1	B1	cao
(b)		Points correct	2	B1	$\pm \frac{1}{2}$ sq ft from sensible table ie
					clear attempt to add frequencies
		Curve		B1	ft from points if 4 or 5 correct
		or			or ft correctly from sensible table
		line segments			or if points are plotted consistently
					within each interval at the correct
					heights
					Accept curve which is not joined
					to the origin
(c)	26 indicated on cf graph		2	M1	for 26 indicated on cf graph
					accept 26-27 inc
		approx 60 from		A1	If M1 scored, ft from cf graph
		correct graph			If M1 not scored, ft only from
					correct curve & if answer is
					correct ($\pm \frac{1}{2}$ sq tolerance) award
					M1 A1
					Total 5 marks
15.		-4 < x < 4	2	B2	B1 for $x < 4$ or $x > -4$ or $x < \pm 4$
					or $x < \sqrt{16}$
					SC B1 for $-4 \le x \le 4$
					Total 2 marks

		T		ı	T
16.	(a)	$\frac{3}{8} + \frac{2}{8}$ oe		2	M1
			$\frac{5}{8}$		A1
	(b)(i)	$\frac{2}{8} \times \frac{1}{7}$ appearing once only		5	M1 Sample space method –
			$\frac{2}{56}$ or $\frac{1}{28}$		A1 for $\frac{2}{56}$ or $\frac{1}{28}$ or for 0.036 or for answer rounding to 0.036 award 2 marks for correct answer; otherwise no marks
	(ii)	$\frac{2}{8} \times \frac{3}{7} + \frac{3}{8} \times \frac{2}{7} \text{ or } 2 \times \frac{2}{8} \times \frac{3}{7} \text{ oe}$			M1 for one correct product M1 for completely correct expression
			12 56		A1 for $\frac{12}{56}$ oe inc $\frac{3}{14}$ or for 0.21 or for answer rounding to 0.21
					Note for (b)(ii): sample space method – award 3 marks for correct answer; otherwise no marks SC M1 for $\frac{2}{8} \times \frac{3}{8}$ or $\frac{3}{8} \times \frac{2}{8}$ M1 (dep) for $\frac{2}{8} \times \frac{3}{8} + \frac{3}{8} \times \frac{2}{8}$ oe SC Sample space method – award 2
					marks for $\frac{12}{64}$ oe; otherwise no marks
					Total 7 marks

4=	()	T		1		1
17.	(a)		2	1		cao
	(b)		<i>x</i> < 6	2		cao B1 for eg $x \le 6$
						or2, -1, 0, 1, 2, 3, 4, 5
						$SC B1 \text{ for } x \ge 6$
	(c)		7	1	B1	cao
	(d)	g(0) = 15		2	M1	for 15 seen
			3		A1	cao If M0, award B1 for ±3 oe
	(e)	k = 12		3	M1	May be stated or indicated on
						diagram. May be implied by one
						correct solution.
			-0.7 or -0.8 3.8		A2	A1 for solution rounding to
						−0.7 or −0.8
						A1 for solution rounding to 3.8
	(f)	tan drawn at $x = 3.5$		3	M1	tan or tan produced passes
						between points $(3, 3 \le y \le 6)$ and
						$(4, 11 \le y \le 14)$
		vertical difference			M1	finds theirvertical difference
		horizontal difference				horizontal difference
						for two points on tan
						or finds their
						vertical difference
						horizontal difference
						for two points on curve, where one
						of the points has an <i>x</i> -coordinate
						between 3 and 3.5 inc and the
						other point has an <i>x</i> -coordinate
						between 3.5 and 4 inc
			6.5 – 11 inc		A1	dep on both M marks
						Total 12 marks

18.	$(\cos x^{\circ} =) \frac{4^{2} + 6^{2} - 8^{2}}{2 \times 4 \times 6}$ or $8^{2} = 4^{2} + 6^{2} - 2 \times 4 \times 6 \cos x^{\circ}$		3	M1	for correct substitution in Cosine Rule
	$(\cos x^{\circ} =) -0.25 \text{ oe}$			A1	
		104.5		A1	for value rounding to 104.5 (104.4775)
					Total 3 marks

19. (a)	7	10 (12) 8	2	B2	for all correct B1 for 2 or 3 correct
(b)(i)		10	2	B1	cao
(ii)		25		B1	cao
					Total 4 marks

20.		$\pi \times r \times 9 = 100$ oe		5	M1
		(r =) 3.53677			A1 for 3.53
					or for value rounding to 3.54
					$(3.14 \rightarrow 3.53857)$
		$\sqrt{9^2-"3.53"^2}$			M1
		(h =) 8.2759			A1 for 8.27
					or for value rounding to 8.28
			108		A1 for answer rounding to 108
					$(\pi \rightarrow 108.40$
					$3.14 \rightarrow 108.45$
					If both M1s scored, award 5
					marks for an answer which rounds
					to 108
					Total 5 marks
21.	(a)		$8y^6$	2	B2 B1 for 8 B1 for y^6
	(b)	$2^p \times (2^3)^q = 2^p \times 2^{3q} = 2^{p+3q}$	p+3q	2	B2 B1 for 2^{3q} seen
					Total 4 marks
22.	(a)(i)		3 a + 3 b oe	3	B1
	(ii)		$2\mathbf{a} + 2\mathbf{b}$ oe		B1 Accept eg $\frac{2}{3}(3\mathbf{a} + 3\mathbf{b})$
	(iii)		a + 2 b oe		B1 Accept eg $2\mathbf{a} + 2\mathbf{b} - \mathbf{a}$
	(b)	$\overrightarrow{DF} = 2\mathbf{a} + 4\mathbf{b} \text{ oe}$		2	M1 Also award for $\overrightarrow{EF} = \mathbf{a} + 2\mathbf{b}$ oe
			$ \begin{array}{c} $		A1 Also award A1 for an acceptable explanation in words.
					Total 5 marks

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