

## Tuesday 15 January 2019

| Morning (Time: 2 hours) | Paper Reference 4MA1/2HR |
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## Mathematics A

Level 1/2
Paper 2HR
Higher Tier


## You must have:

Total Marks
Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
- there may be more space than you need.
- Calculators may be used.
- You must NOT write anything on the formulae page.

Anything you write on the formulae page will gain NO credit.

## Information

- The total mark for this paper is 100.
- The marks for each question are shown in brackets - use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Pearson

## International GCSE Mathematics

Formulae sheet - Higher Tier

| Arithmetic series <br> Sum to $n$ terms, $S_{n}=\frac{n}{2}[2 a+(n-1) d]$ | Area of trapezium $=\frac{1}{2}(a+b) h$ |
| :---: | :---: |
| The quadratic equation <br> The solutions of $a x^{2}+b x+c=0$ where $a \neq 0$ are given by: $x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$ |  |
| Trigonometry | In any triangle $A B C$ <br> Sine Rule $\frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$ <br> Cosine Rule $a^{2}=b^{2}+c^{2}-2 b c \cos A$ <br> Area of triangle $=\frac{1}{2} a b \sin C$ |
| Volume of cone $=\frac{1}{3} \pi r^{2} h$ <br> Curved surface area of cone $=\pi r l$ | Volume of prism $=$ area of cross section $\times$ length |
| Volume of cylinder $=\pi r^{2} h$ Curved surface area of cylinder $=2 \pi r h$ | Volume of sphere $=\frac{4}{3} \pi r^{3}$ <br> Surface area of sphere $=4 \pi r^{2}$ |

## Answer ALL TWENTY THREE questions.

Write your answers in the spaces provided.
You must write down all the stages in your working.

1 The table gives information about the number of days that 100 cars were in an airport car park.

| Number of days (d) | Frequency |
| :---: | :---: |
| $0<d \leqslant 4$ | 16 |
| $4<d \leqslant 8$ | 18 |
| $8<d \leqslant 12$ | 19 |
| $12<d \leqslant 16$ | 27 |
| $16<d \leqslant 20$ | 20 |

(a) Write down the modal class.
(b) Work out an estimate for the mean number of days.

2 The diagram shows two solid toy bricks, Brick A and Brick B.


Brick A


Diagram NOT accurately drawn

Brick $\mathbf{A}$ is a triangular prism of length 5 cm .
The cross section of Brick $\mathbf{A}$ is an isosceles right-angled triangle with equal sides of length 6 cm .

Brick B is half a cylinder of length 5 cm .
The semicircular cross section of Brick B has diameter 6 cm .
The volume of Brick $\mathbf{A}$ is greater than the volume of Brick $\mathbf{B}$.
How much greater?
Give your answer correct to 1 decimal place.

3 Here are the first five terms of a number sequence $S$.

| 10 | 16 | 22 | 28 | 34 |
| :--- | :--- | :--- | :--- | :--- |

(a) Find an expression, in terms of $n$, for the $n$th term of this sequence.

The $n$th term of a sequence $T$ is given by $n^{2}-3$
There are numbers that are terms in both the sequence $S$ and the sequence $T$.
(b) Find one of these numbers.

4 On Saturday, Jacob walked 10800 steps.
On Sunday, he walked 7\% more steps than on Saturday.
Work out how many steps Jacob walked on Sunday.

5 The scale drawing shows the position of a hall and the position of a library.


Scale: 1 cm represents 20 metres

A post box is 140 metres from the library on a bearing of $220^{\circ}$
(a) Show the position of the post box on the scale drawing.

Mark the position with a cross $(\times)$ and label it $P$.
(b) Use your scale drawing to find
(i) the real distance, in metres, of the hall from the post box,
(ii) the bearing of the hall from the post box.


Diagram NOT accurately drawn

Pentagon $A B C D E$ is drawn inside the regular octagon $A B F G H I J K$.
The pentagon has exactly one line of symmetry.
Work out the value of $x$.

7 The diagram shows a trapezium.


Work out the value of $y$.
Give your answer correct to 1 decimal place.

$$
y=
$$

8 (a) Simplify fully $\frac{15 k^{4} m^{3}}{5 k m^{2}}$
(b) Solve the inequality $7<4 x-1 \leqslant 17$

9 Omar invests 6000 dirham for 4 years in a savings account. He will get $1.5 \%$ per year compound interest.

Work out the total amount of interest Omar will have received by the end of 4 years.
Give your answer correct to the nearest dirham.

10 (a) Simplify fully $\left(16 x^{8} y^{6}\right)^{\frac{1}{2}}$
(b) Solve $\frac{8-2 x}{3}-\frac{2 x-3}{2}=4$

Show clear algebraic working.

$$
x=
$$

(c) Make $f$ the subject of $m=\sqrt{\frac{1}{3} e f}$

11 The straight line $\mathbf{L}_{1}$ has equation $x+2 y=4$
The straight line $\mathbf{L}_{2}$ passes through the points $(-1,-7)$ and $(7,9)$
Michael says that the lines $\mathbf{L}_{1}$ and $\mathbf{L}_{2}$ are perpendicular.
Is Michael correct?
You must show clearly how you get your answer.

12 Freddie recorded the number of runs he scored in each of 11 cricket matches.
Here are his results.

| 4 | 0 | 21 | 32 | 51 | 6 | 102 | 69 | 17 | 9 | 42 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Find the interquartile range of his results.

13 Carlos, Flavia and Tazia shared $£ 861$ between themselves.
The amount of money Flavia got is $65 \%$ of the amount of money Carlos got.
The amount of money Tazia got is $22 \%$ more than the amount of money Carlos got.
Work out how much money Carlos got.

14 (a) Given that $a=3^{x}$ and $b=3^{y}$
express in terms of $a$ or $b$ or $a$ and $b$,
(i) $3^{2 x}$
(ii) $3^{x+4 y}$
(iii) $3^{y-1}$
$a=3^{x}$ and $b=3^{y}$
$a b=2187$
$a^{2} b=177147$
(b) Work out the value of $x$ and the value of $y$. Show your working clearly.

$$
x=
$$

$$
\begin{equation*}
y= \tag{3}
\end{equation*}
$$

15 Barney has a biased coin.
When the coin is thrown once, the probability that the coin will land heads is 0.3
Barney throws the coin 4 times.
(a) Work out the probability that the coin will land heads exactly 3 times.
(b) Work out the probability that the coin will land heads at least once.

16120 people who visited a sports centre were asked if they went swimming (S), played basketball $(B)$ or used the gym ( $G$ ).

Their answers showed that
28 people went swimming
16 people played basketball
27 people used the gym
3 people went swimming and played basketball
5 people played basketball and used the gym
7 people went swimming and used the gym
2 people went swimming, played basketball and used the gym
(a) Using this information, complete the Venn diagram to show the number of people in each region of the Venn diagram.


One of the people who went swimming is chosen at random.
(b) Find the probability that this person also played basketball.
$17 P=e f$
$e=4.8$ correct to 2 significant figures.
$f=0.26$ correct to 2 significant figures.
(a) Work out the lower bound for the value of $P$.

Show your working clearly.
Give your answer correct to 3 significant figures.
$Q=\frac{t}{w}$
$t=2.73$ correct to 3 significant figures.
$w=0.04$ correct to 1 significant figure.
(b) Work out the upper bound for the value of $Q$.

Show your working clearly.
Give your answer correct to 2 significant figures.

18 Here is the graph of $y=\sin x^{\circ}$ for $0 \leqslant x \leqslant 360$

(a) On the grid above, sketch the graph of $y=\sin (x+90)^{\circ}$ for $0 \leqslant x \leqslant 360$

In $0 \leqslant x \leqslant 360$, the graph of $y=\sin \left(\frac{x}{2}\right)^{\circ}+3$ has a maximum at the point $A$.
(b) Write down the coordinates of $A$.
(2)
$19 A B C D$ is a quadrilateral.


Find the area of quadrilateral $A B C D$.
Give your answer correct to 3 significant figures.

20 (a) Write $3 x^{2}-12 x+7$ in the form $a(x+b)^{2}+c$

The line $\mathbf{L}$ is the line of symmetry of the curve with equation $y=3 x^{2}-12 x+7$
(b) Using your answer to part (a) or otherwise, write down an equation of $\mathbf{L}$.

21 The curve with equation $y=(10 x-3)(x+1)$ and the line with equation $y-6 x=0$ intersect at the points $A$ and $B$.

Find the coordinates of the midpoint of $A B$.
Show your working clearly.


Diagram NOT accurately drawn
$O P Q$ is a sector of a circle, centre $O$
$O A B$ is a sector of a circle, centre $O$
$A$ is the point on $O P$ such that $O A: A P=3: 2$
$B$ is the point on $O Q$ such that $O B: B Q=3: 2$
Angle $P O Q=45^{\circ}$
The area of the shaded region is $\frac{81}{2} \pi \mathrm{~cm}^{2}$
Work out the perimeter of the shaded region.
Give your answer in terms of $\pi$.

23 The 10th term of an arithmetic series, $S$, is 66
The sum of the first 20 terms of $S$ is 1290
Find the 5th term of $S$.
Show your working clearly.

