# MARK SCHEME for the May/June 2012 question paper for the guidance of teachers 

## 0580 MATHEMATICS

0580/41
Paper 4 (Extended), maximum raw mark 130

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## Abbreviations

| cao | correct answer only |
| :--- | :--- |
| cso | correct solution only |
| dep | dependent |
| ft | follow through after error |
| isw | ignore subsequent working |
| oe | or equivalent |
| SC | Special Case |
| www | without wrong working |
| art | anything rounding to |
| soi | seen or implied |


| Qu. | Answers | Mark | Part Marks |
| :---: | :---: | :---: | :---: |
| 1 (a) | 1134 | 3 | M2 for $\frac{504}{12} \times(12+7+8)$ soi by answer of 1130 or B1 for 27 or 42 or 294 or 336 seen |
| (b) (i) | 468.72 | 3 | M2 for $\frac{93}{100} \times 504$ oe soi by 468.7 or 469 or M1 for $\frac{7}{100} \times 504$ (implied by 35.28 ) |
| (ii) | 84 | 3 | M2 for $\frac{64.68}{77} \times 100$ or M1 for $(100-23) \%=64.68$ |
| (c) | 262.19 cao | 3 | M2 for $250 \times 1.016^{3}$ oe implied by answer 262.2 or better <br> or M1 for $250 \times 1.016^{n}$ oe $n>2$ seen |
| (d) | 12.5\% | 3 | M2 for $\frac{324-288}{288} \times 100$ or M1 for $\frac{324}{288} \times 100(112.5)$ or $\frac{36}{288}(0.125)$ |
| 2 (a) | 10.9 or $10.92 \ldots$ www 4 | 4 | M2 for $4^{2}+9^{2}-2 \times 4 \times 9 \times \cos 108$ |
|  |  |  | If M0, M1 for correct implicit statement <br> A1 for 119.249...(which can be 3 www) |
| (b) (i) | 5.16 or 5.162.... www 3 | 3 | M2 for $9 \times \cos 55$ oe in correct triangle |
|  |  |  | If M0, B1 for 55 or 35 in correct position soi |
| (ii) | (0) 53 | B2 | SC1 for answer 233 |


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| 3 (a) <br> (b) <br> (c) $(\mathbf{i})$ <br> (ii) <br> (d) | ```\(10.98(4) \quad 0 \quad-0.98(4)-1\) 9 points plotted smooth curve \(y=0.8\) drawn -1.1 to \(-1.2,-0.4\) to \(-0.5,1.55\) to 1.65 correct tangent drawn at \(x=-1.5\) 4 to 5.5``` | B3 <br> P3ft <br> C1 <br> B1 $1,1,1$ <br> T1 <br> B2 | B2 for 4 correct, $\mathbf{B 1}$ for 3 correct <br> B2 for 7 or 8 points correct <br> B1 for 5 or 6 points correct correct cubic shape through 8 or more points from -2 to 2 <br> Accept good freehand <br> To make the three possible intersections (otherwise the line must be from -2 to 2 ) <br> Allow slight daylight <br> dep on T1 <br> M1 for evidence rise/run with correct scales dep on T1 |
| :---: | :---: | :---: | :---: |
| 4 (a) <br> (b) <br> (c) <br> (d) (i) <br> (ii) <br> (e) | 90 <br> $\tan (A C B)=7 \div 10$ oe 34.9(9...) <br> same segment <br> 11.9 or $11.8(9 \ldots$.$) www 3$ <br> 38.6 (38.58 to 38.62 ) www 2 <br> 8.69 or $8.7(0)$ or 8.685 to $8.700 \ldots$ cao www 3 | B1 <br> M1 <br> A1 <br> B1 <br> 3 | Any longer method must reach equivalent stage <br> Allow same arc oe <br> M2 for $\frac{7 \times \sin 77}{\sin 35}$ <br> or M1 for implicit form <br> M1 for <br> $0.5 \times 7 \times$ their $(\mathrm{d})(\mathrm{i}) \times \sin (180-77-35)$ oe <br> Allow 68.00 to 68.01 for 68 <br> M2 for $12.3 \times\left(\frac{10}{\text { their } 11.9}\right)^{2}$ <br> or M1 for $\left(\frac{10}{\text { their } 11.9}\right)^{2}$ or reciprocal seen |
| 5 (a) (i) <br> (ii) <br> (iii) <br> (b) <br> (c) (i) | $\begin{aligned} & 2.8 \mathrm{cao} \\ & 3.8 \mathrm{cao} \\ & 1.8 \mathrm{cao} \\ & 6 \\ & 9,4,4 \end{aligned}$ | 1 <br> 1ft <br> 1 <br> 2 | accept 2 (h) 48, not 2.48 <br> accept 3 (h) 48 not 3.48 <br> ft their (a)(ii) -2 accept 1 (h) 48 and 1.48 <br> B1 for 2 correct |


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| (ii) (d) | $\begin{aligned} & 12.53 .54 .55 .57 \\ & 20 \times 1+25 \times 2.5+18 \times 3.5+ \\ & \text { their } 9 \times 4.5+\text { their } 4 \times 5.5+\text { their } 4 \times \\ & 7 \\ & (=236) \\ & \div 80 \\ & 2.95 \text { cao } \end{aligned}$ <br> Axes suitably numbered or horizontal axis suitably numbered and area scale stated <br> 6 columns with correct relative widths heights: <br> 10 <br> 25, 18, their 9 , their 4 their $4 \div 2$ | M1 <br> M1 <br> M1 <br> A1 <br> 1 <br> 1 <br> 1 <br> 1 | At least 5 correct mid-values seen <br> $\sum f x$ where $x$ is in the correct interval <br> $(20+62.5+63+40.5+22+28)$ <br> Dependent on second method mark <br> Allow www 4 <br> e.g. $4 \mathrm{~cm}^{2}=10$ <br> no gaps, but condone reasonable freehand <br> if vertical axis not labelled use correct relative heights |
| :---: | :---: | :---: | :---: |
| 6 (a) (i) <br> (ii) <br> (iii) <br> (b) (i) <br> (ii) | $\begin{aligned} & (4 x-7)(2 x-1)=1 \\ & 8 x^{2}-14 x-4 x+7 \\ & 4 x^{2}-9 x+3=0 \\ & (x=) \frac{-(-9) \pm \sqrt{(-9)^{2}-4(4)(3)}}{2 \times 4} \\ & (x=) 0.41,1.84 \text { cao } \\ & 0.36 \text { or } 0.3720 \text { to } 0.3724 \text { or } 0.37 \\ & (x-4)(x+4) \\ & (2 x+3)(x+4)+(x+40)=2\left(x^{2}-16\right) \\ & \text { oe } \\ & 2 x^{2}+8 x+3 x+12 \text { or } \\ & 2 x^{3}+3 x^{2}-32 x-48 \\ & x=-7 \quad \text { www } 4 \end{aligned}$ | M1 <br> B1 <br> E1 <br> B2 <br> B1,B1 <br> B1ft <br> B1 <br> M2 <br> B1 <br> A1 | or $(4 x-7)(2 x-1)-1=0$ only allow $-18 x$ and/or $+6=0$ or $=-6$ <br> at least one more line e.g. $8 x^{2}-18 x+6=0$ with no errors or omissions seen <br> B1 for $\sqrt{(-9)^{2}-4(4)(3)}$ or better seen $(\sqrt{33})$ <br> B1 for $p=-(-9)$ and $r=2 \times 4$ or better as long as in the form $\frac{p+o r-\sqrt{q}}{r}$ <br> After B0B0, SC1 for 0.4 or 0.406 ( $929 \ldots$...) and 1.8 or $1.843(070 \ldots$ ) <br> ft their value to give positive $(4 x-7)$ <br> fractions cleared or could all still be over $\left(x^{2}-16\right)$ <br> or $(2 x+3)\left(x^{2}-16\right)+(x+40)(x-4)=2(x-4)\left(x^{2}-16\right)$ <br> Condone sign slips |


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| 9 (a) (i) | 14 | 1 |  |
| :---: | :---: | :---: | :---: |
| (ii) | $13-2 x$ | 2 | M1 for 7-2(x-3) |
| (iii) | $25 x^{2}-8$ final answer | 1 |  |
| (b) | $\frac{7-x}{2} \text { oe }$ | 2 | M1 for $2 x=7-y, x=\frac{7-y}{2}$ oe or $x=7-2 y, \quad 2 y=7-x$ oe i.e one step from answer |
| (c) | $9 x^{2}+30 x+17$ | 3 | M1 for $(3 x+5)^{2}-8$ seen B1 for $9 x^{2}+30 x+25$ |
| (d) | 7 cao | 3 | M2 for $3(3 x+5)+5=83$ or better or B1 for $3(3 x+5)+5$ oe |
| (e) | $x<-\frac{3}{8} \text { oe cao }$ | 3 | M1 for $2(3 x+5)<7-2 x$ oe B1 for $8 x *-3$ or $-8 x * 3$ <br> Do not accept $\frac{3}{-8}$ |
| 10 (a) | 2030 or 2040 or 2034 to 2036. (...) | 2 | $(V=) \frac{1}{3} \times \pi \times 9^{2} \times 24$ <br> Accept $648 \pi$ for 2 marks if final answer |
|  |  |  |  |
| (b) | (upper radius =) 3 | B1 | accept $9 \times \frac{8}{24}$ oe |
|  | (vol cut off $=$ ) $\frac{1}{3} \times \pi \times$ their $3^{2} \times 8$ | M1 | ( $=75.36$ to 75.41 ) their $r$ must be less than 9 |
|  | their (a) - their 75.39 | $\begin{aligned} & \text { M1 } \\ & \text { dep } \end{aligned}$ | [ alternate method M1 for ratio sides 1:3 <br> M1 ratio vols 1: 27 <br> M1 their $($ a $) \times 26 \div 27$ ] <br> $624 \pi$ implies B1 M2 or M3 |
|  | 1958 to 1964.(...) | E1 | must see a figure after decimal point if 1960 |
| (c) | $1960=5 \times \pi \times r^{2} \times 15$ soi | M1 |  |
|  | $r^{2}=1960 \div \pi \div 15 \div 5$ | M1 | implied by 8.318... |
|  | $\checkmark$ their 8.318 | M1 | dep on M1 M1 |
|  | 2.88 to 2.89 | E1 | SC2 for $5 \times \pi \times 2.9^{2} \times 15=1980$ to 1982 |

