CANDIDATE NAME


## CENTRE NUMBER

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CANDIDATE NUMBER


## MATHEMATICS

0580/22
Paper 2 (Extended)
May/June 2012
1 hour 30 minutes
Candidates answer on the Question Paper.
Additional Materials: Electronic calculator Geometrical instruments Mathematical tables (optional) Tracing paper (optional)

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use a pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.
DO NOT WRITE IN ANY BARCODES.

Answer all questions.
If working is needed for any question it must be shown below that question.
Electronic calculators should be used.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.
For $\pi$, use either your calculator value or 3.142 .
At the end of the examination, fasten all your work securely together.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total of the marks for this paper is 70 .

This document consists of 12 printed pages.

1 The ferry from Helsinki to Travemunde leaves Helsinki at 1730 on a Tuesday.
The journey takes 28 hours 45 minutes.
Work out the day and time that the ferry arrives in Travemunde.

Answer Day
Time

2
TRIGONOMETRY

From the above word, write down the letters which have
(a) exactly two lines of symmetry,

> Answer(a)
(b) rotational symmetry of order 2 .

3 For this question, $1<x<2$.
Write the following in order of size, smallest first.
$\frac{5}{x}$
$5 x$
$\frac{x}{5}$
$x-5$

Answer $\qquad$ < $\qquad$ $<$ $\qquad$ $<$

4
$1 \frac{1}{2}+\frac{1}{3}+\frac{1}{4}=\frac{p}{12}$

Work out the value of $p$.
Show all your working.

5 A lake has an area of 63800000000 square metres.
Write this area in square kilometres, correct to 2 significant figures.
$6 x$ is a positive integer and $15 x-43<5 x+2$.
Work out the possible values of $x$.

7


NOT TO SCALE

The perimeter of the rectangle is the same length as the circumference of the circle.
Calculate the radius, $r$, of the circle.

8 A car company sells a scale model $\frac{1}{10}$ of the size of one of its cars.
Complete the following table.

|  | Scale Model | Real Car |
| :--- | :---: | :---: |
| Area of windscreen $\left(\mathrm{cm}^{2}\right)$ | 135 |  |
| Volume of storage space $\left(\mathrm{cm}^{3}\right)$ |  | 408000 |

## 9



The line $A B$ represents the glass walkway between the Petronas Towers in Kuala Lumpur.
The walkway is 58.4 metres long and is 170 metres above the ground.
The angle of elevation of the point $P$ from $A$ is $78.3^{\circ}$.
Calculate the height of $P$ above the ground.
$\qquad$

Speed (m/min)


The diagram shows the speed-time graph for a boat journey.
(a) Work out the acceleration of the boat in metres/minute ${ }^{2}$.

Answer(a) $\qquad$ $\mathrm{m} / \min ^{2}$
(b) Calculate the total distance travelled by the boat. Give your answer in kilometres.
$11 y$ varies directly as the square of $(x-3)$.
$y=16$ when $x=1$.
Find $y$ when $x=10$.

12


A helicopter flies 8 km due north from $A$ to $B$. It then flies 5 km from $B$ to $C$ and returns to $A$. Angle $A B C=150^{\circ}$.
(a) Calculate the area of triangle $A B C$.

Answer(a) $\qquad$ $\mathrm{km}^{2}$
(b) Find the bearing of $B$ from $C$.

## Answer(b)

13 The taxi fare in a city is $\$ 3$ and then $\$ 0.40$ for every kilometre travelled.
(a) A taxi fare is $\$ 9$.

How far has the taxi travelled?

Answer(a)
km [2]
(b) Taxi fares cost $30 \%$ more at night.

How much does a $\$ 9$ daytime journey cost at night?

14

(a) Describe fully the single transformation that maps triangle $A$ onto triangle $B$.

Answer(a)
(b) Find the $2 \times 2$ matrix which represents this transformation.


15


The cumulative frequency diagram shows information about the heights of 60 tomato plants. Use the diagram to find
(a) the median,
$\qquad$
(b) the lower quartile,
Answer(b)
$\qquad$
(c) the interquartile range,
Answer(c)
(d) the probability that the height of a tomato plant, chosen at random, will be more than 15 cm .

> Answer(d)


The diagram shows the graph of $y=\frac{x}{2}+\frac{2}{x}$, for $0<x \leqslant 8$.
(a) Use the graph to solve the equation $\frac{x}{2}+\frac{2}{x}=3$.

$$
\text { Answer (a) } x=\text {.................. or } x=
$$

(b) By drawing a suitable tangent, work out an estimate of the gradient of the graph where $x=1$.

17 (a) Find the co-ordinates of the midpoint of the line joining $A(-8,3)$ and $B(-2,-3)$.
(b) The line $y=4 x+c$ passes through $(2,6)$.

Find the value of $c$.

$$
\begin{equation*}
\operatorname{Answer}(b) c= \tag{1}
\end{equation*}
$$

(c) The lines $5 x=4 y+10$ and $2 y=k x-4$ are parallel.

Find the value of $k$.

$$
\mathrm{f}(x)=(x+2)^{3}-5 \quad \mathrm{~g}(x)=2 x+10 \quad \mathrm{~h}(x)=\frac{1}{x}, x \neq 0
$$

Find
(a) $\mathrm{gf}(x)$,
(b) $\mathrm{f}^{-1}(x)$,

$$
\operatorname{Answer}(b) \mathrm{f}^{-1}(x)=
$$

(c) $\operatorname{gh}\left(-\frac{1}{5}\right)$.

19 Find the values of $x$ for which
(a) $\left(\begin{array}{cc}1 & 0 \\ 0 & 2 x-7\end{array}\right)$ has no inverse,
(b) $\left(\begin{array}{cc}1 & 0 \\ 0 & x^{2}-8\end{array}\right)$ is the identity matrix,

$$
\text { Answer (b) } x=\quad . . . . . . . . . . . . . . . \quad \text { or } x=
$$

(c) $\left(\begin{array}{cc}1 & 0 \\ 0 & x-2\end{array}\right)$ represents a stretch with factor 3 and the $x$ axis invariant.

$$
\begin{equation*}
\text { Answer (c) } x= \tag{2}
\end{equation*}
$$ publisher will be pleased to make amends at the earliest possible opportunity.

